

# Millicharged particles from proton bremsstrahlung in the atmosphere

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The 2022 Shanghai Particle Physics and Cosmology Symposium:  
Neutrino and Dark Matter Physics (SPCS 2022)  
2022.11.18

# Content

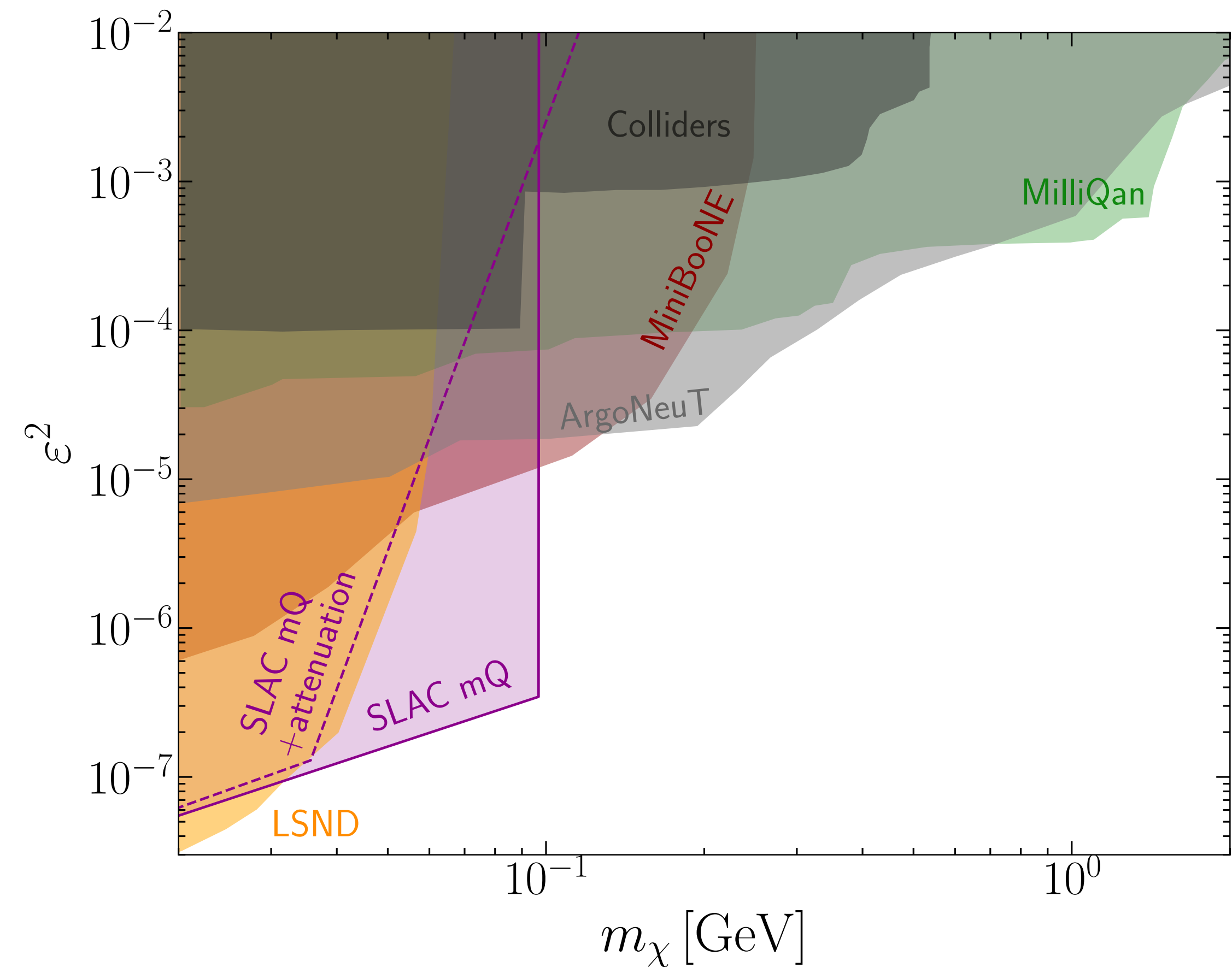
- Motivation
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# Motivation

- Millicharged particles (MCPs) are well-motivated beyond the Standard Model particles with small electric charge:

$$\mathcal{L}_{\text{int}} = \varepsilon e A_\mu \bar{\chi} \gamma^\mu \chi$$

- The collision between cosmic ray protons and the atmosphere can copiously produce MCPs.
- MCPs produced in atmosphere can be detected by underground detectors.



# Meson Decay

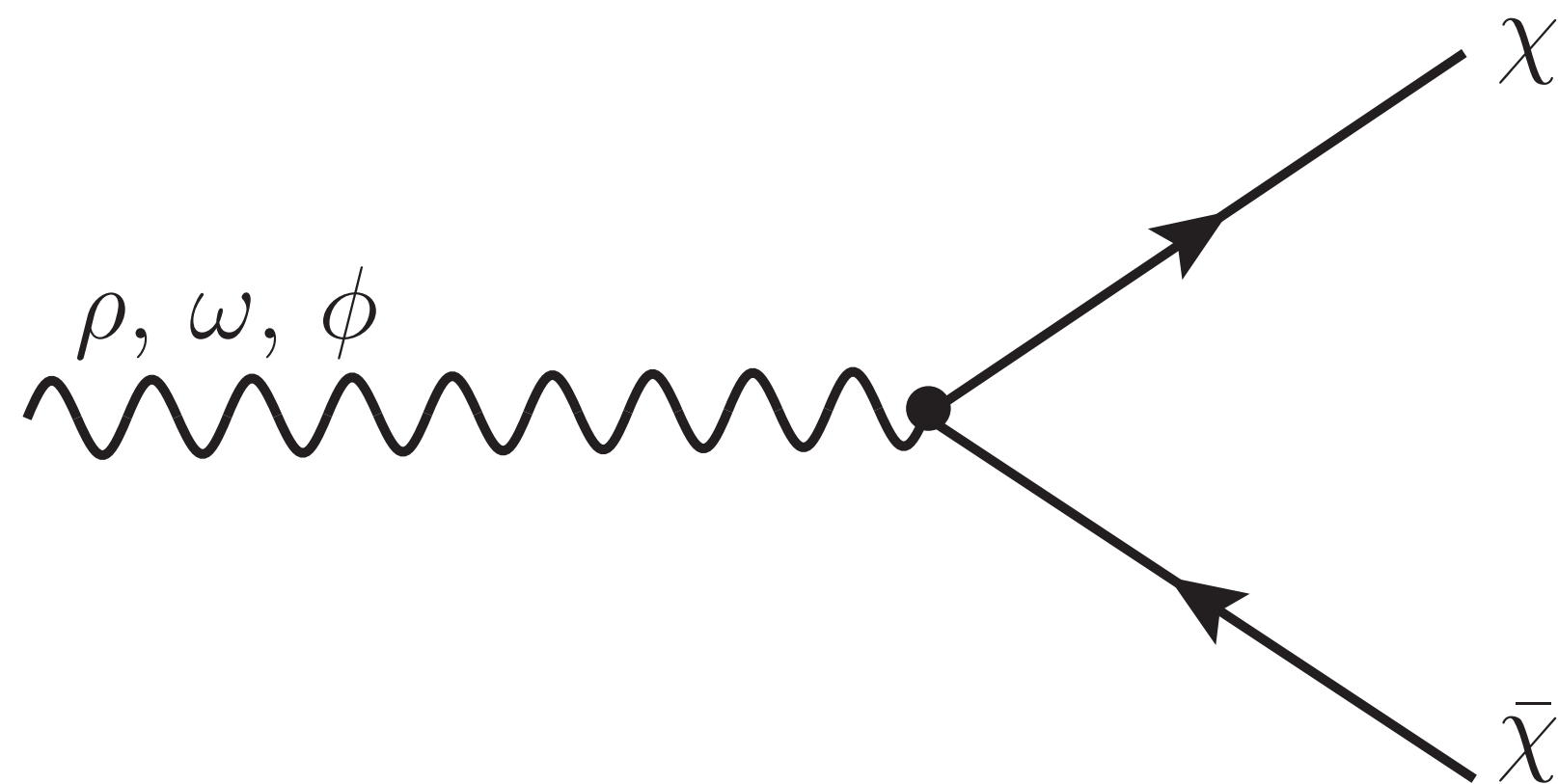
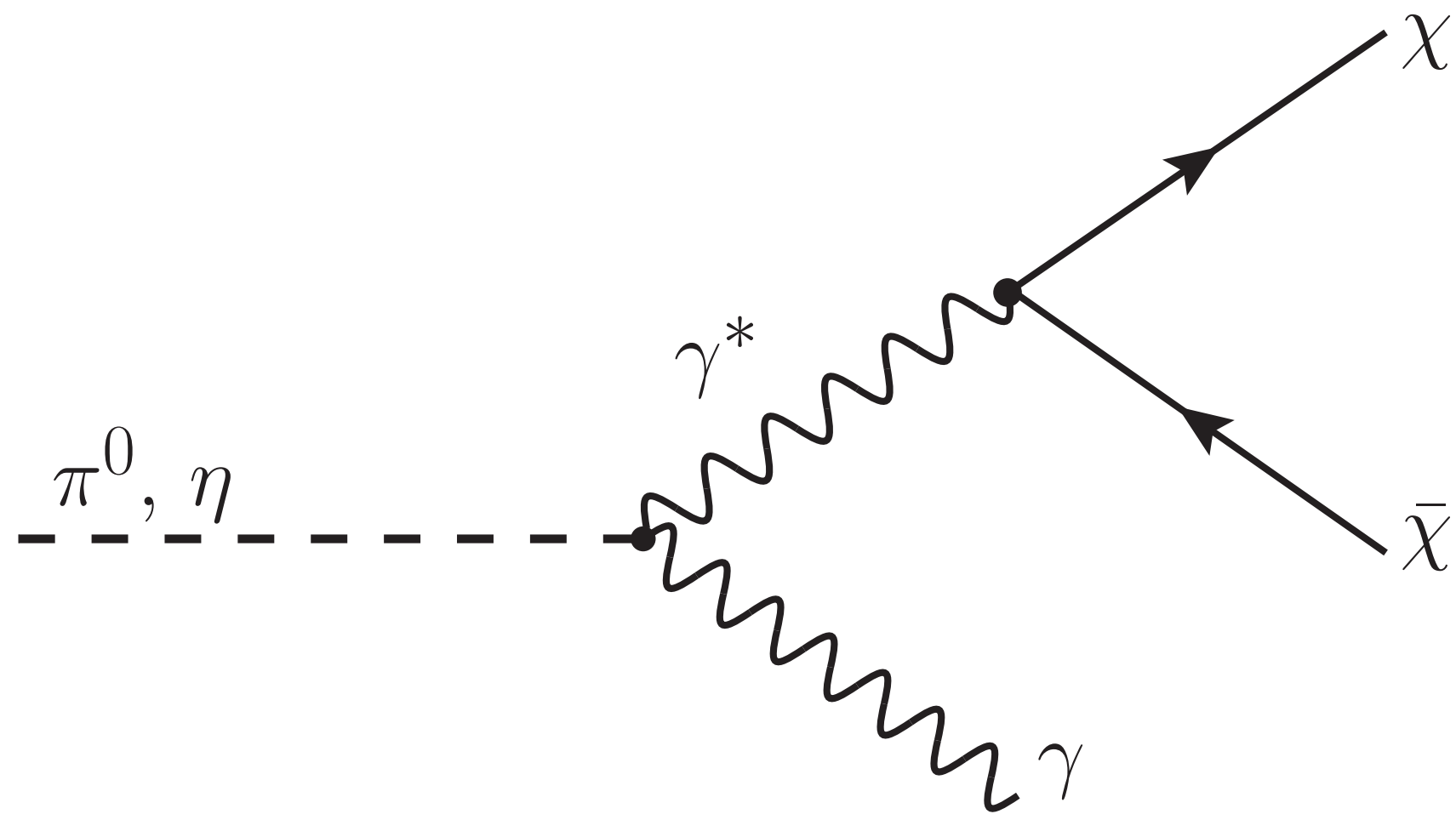
- In previous studies, the MCPs are produced via meson decay.

Plestid et al., 2022.11732

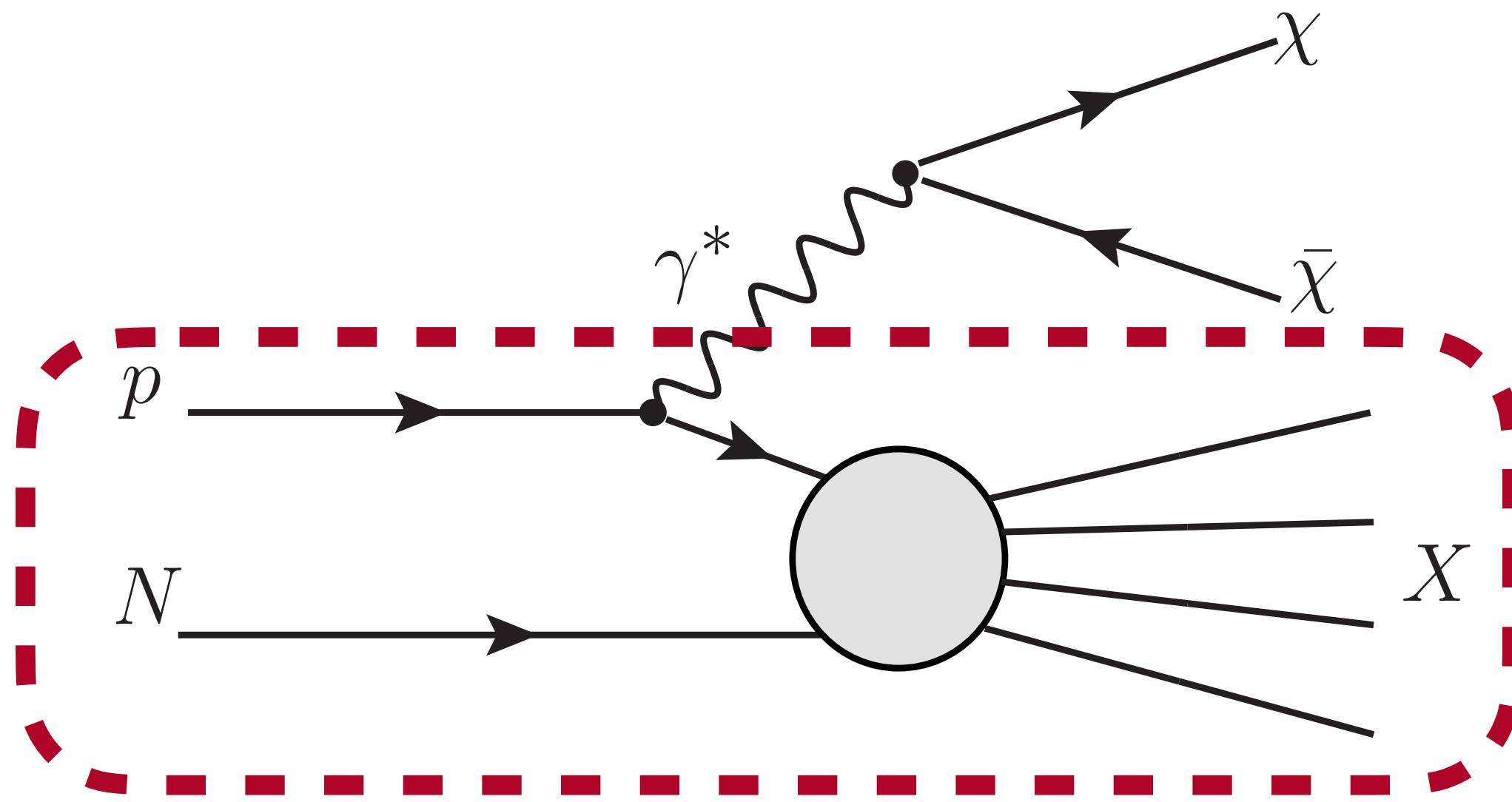
Kachelriess et al., 2104.06811

Arguelles et al., 2104.13924

- MCPs can be produced via the Dalitz decay of pseudo-scalar mesons and two body decay of vector mesons.



# Proton Bremsstrahlung



We include a new process, proton bremsstrahlung, in the MCP production.

Factorization:

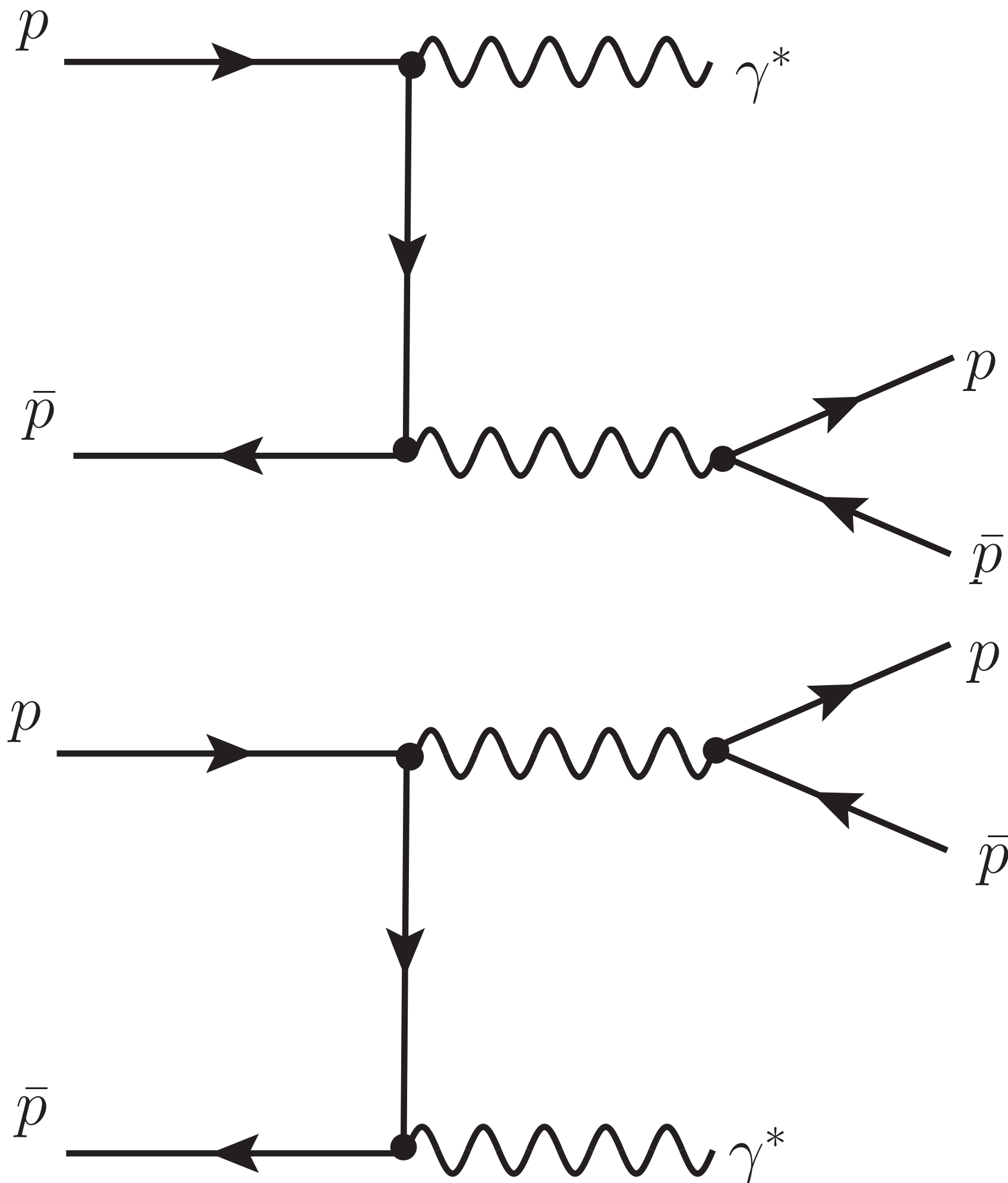
$$d\sigma_{pN \rightarrow \gamma^* X}(s) = d\mathcal{P}_{p \rightarrow \gamma^* p} \times \sigma_{pN \rightarrow X}(s')$$

The  $d\mathcal{P}_{p \rightarrow \gamma^* p}$  is the splitting kernel.

The splitting kernel is usually given by the FWW approximation when all of the particles are highly relativistic.

Blumlein et al., 1311.3870

# Splitting Kernel

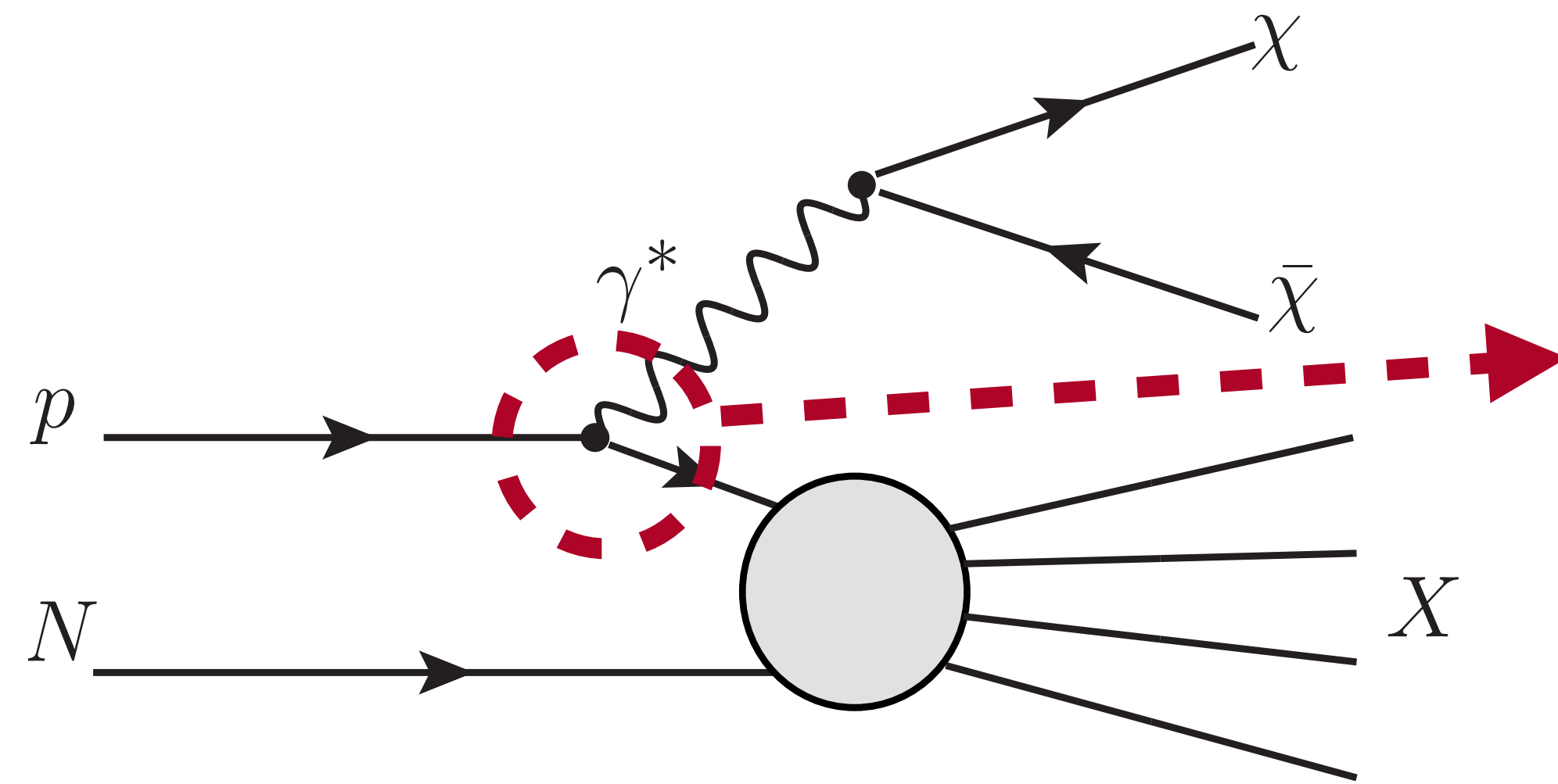


$$\frac{d\Phi_p}{dE_p d\Omega}(h_{\max}) = \frac{0.74 \times 1.8 \times 10^4}{\text{m}^2 \text{ s sr GeV}} \left( \frac{E_p}{\text{GeV}} \right)^{-2.7}$$

The low energy protons are important

$$d\mathcal{P}_{p \rightarrow p\gamma^*} = \frac{d\sigma_{p\bar{p} \rightarrow \gamma^* p\bar{p}}(s)}{\sigma_{p\bar{p} \rightarrow p\bar{p}}(s')}$$

# Form Factor



The radiation process is enhanced by the time-like form factor of proton.

$$F_1(q^2) = \sum_{V=\rho \ \rho' \ \rho'' \ \omega \ \omega' \ \omega''} \frac{f_V m_V^2}{m_V^2 - q^2 - i m_V \Gamma_V},$$

Faessler et al., 0910.5589

$$m_\rho \approx m_\omega \approx 0.77 \text{ GeV}$$

# Cascade Equation

M. Thunman et al., hep-ph/9505417

- The MCP flux at the surface of Earth:

$$\frac{d\Phi_{\chi}^s}{dE_{\chi}^s} = \iint dh dE_p \frac{d\Phi_p}{dE_p}(h) n_T(h) \sigma_{pT}(E_p) \sum_i \frac{dN_{\chi}^i}{dE_{\chi}}$$

- The proton flux at a given height:

$$\frac{d}{dh} \left( \frac{d\Phi_p}{dE_p}(h) \right) = \sigma_{pT}(E_p) n_T(h) \frac{d\Phi_p}{dE_p}(h)$$



# Earth Attenuation

Gaisser et al., Cosmic Rays and Particle Physics

- MCPs lose energy when travel through Earth:

$$-\frac{dE}{dX} \approx \varepsilon^2(a + bE)$$

- MCP flux after earth attenuation

$$\frac{d^2\Phi_{\chi}^D(X)}{dE_{\chi}d\Omega} = e^{\varepsilon^2 bX} \frac{d^2\Phi_{\chi}^s}{dE_{\chi}^s d\Omega^s}$$

$$E_{\chi}^s = (E_{\chi} + a/b) \exp(\varepsilon^2 bX) - a/b$$

# Signal

- The signals of MCP come from the elastic scattering with electron in the detector.

$$\frac{d\sigma}{dE_r} = \varepsilon^2 \alpha^2 \pi \frac{m_e \left( E_r^2 + 2E_\chi^2 \right) - E_r \left( m_e \left( 2E_\chi + m_e \right) + m_\chi^2 \right)}{E_r^2 m_e^2 \left( E_\chi^2 - m_\chi^2 \right)}$$

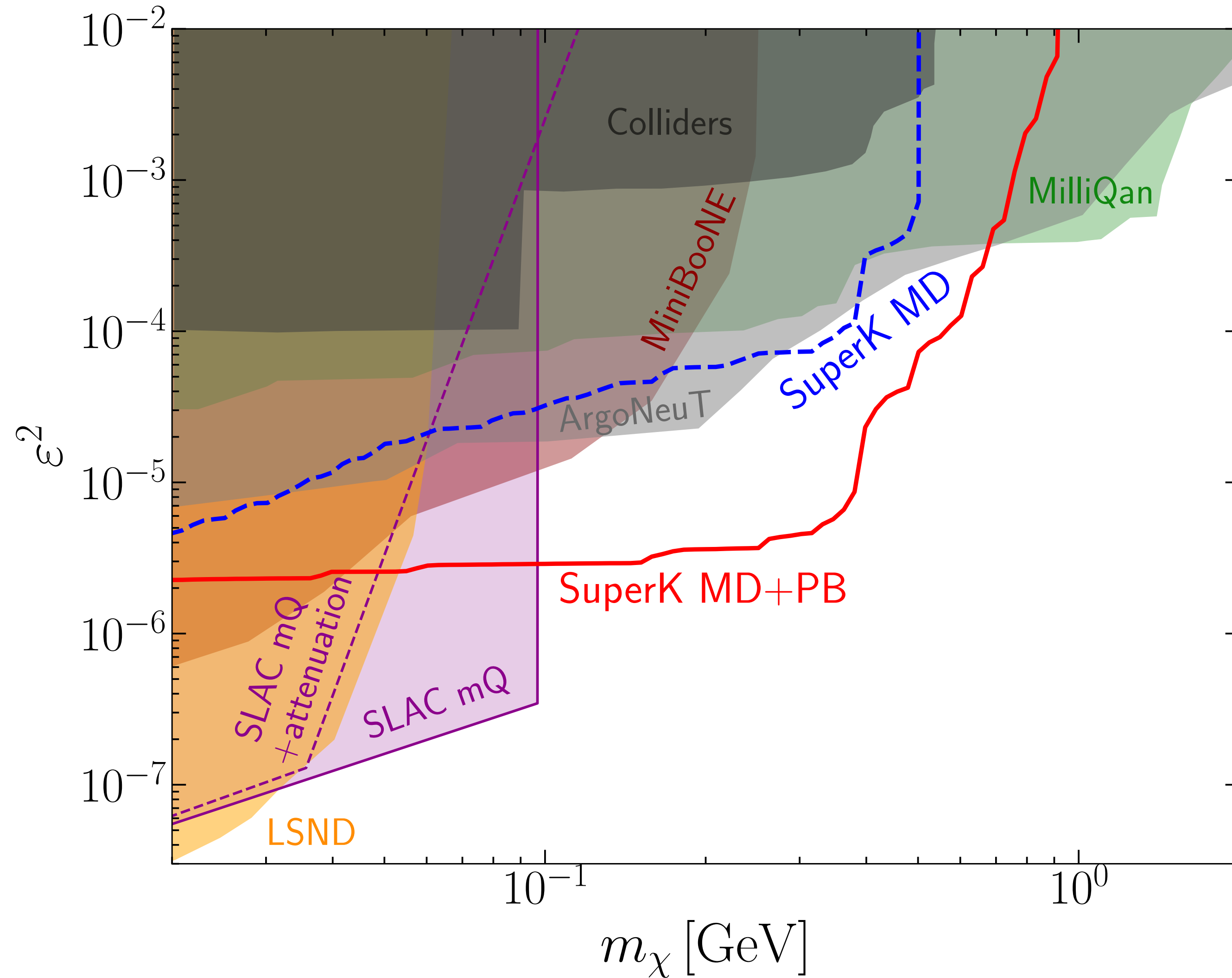
- signals per bin:

$$S_i = 2\pi n_e \mathcal{E} \int dE_r f(E_r) \int dE_\chi \int d\cos\theta \frac{d^2\Phi_\chi^D}{dE_\chi d\cos\theta} \frac{d\sigma}{dE_r}$$

- We use data and signal efficiency from SuperK phase I to phase III to set the constraint to MCPs.

Arguelles et al., 2104.13924

# SuperK constraints



Blue: meson decay  
Red: meson decay plus proton  
bremsstrahlung

# Conclusion

- The MCPs can be copiously produced in the collision between cosmic ray protons and the atmosphere.
- We include a new production channel, proton bremsstrahlung, of MCPs which is enhanced by the resonance of the time-like form factor of proton in sub-GeV region.
- After including the PB process, the SuperK constraint for MCPs become much stronger than the meson decay processes.
- These enhancement will also appear in other pN collision experiments.

Thank you !

# Detail Calculation of the Splitting Kernel

- The splitting kernel is calculated using the initial state radiation process  $p\bar{p} \rightarrow p\bar{p}\gamma^*$ , and in CM frame:

$$\frac{d^2 \mathcal{P}_{p \rightarrow \gamma^* p}}{dE_{\gamma^*}^0 d \cos \theta_{p, \gamma^*}^0} = \frac{1}{512 \pi^4 E_p^0 E_{\bar{p}}^0 \left| v_p^0 - v_{\bar{p}}^0 \right|} \frac{\left| F_p(m_{\chi\bar{\chi}}^2) \right|^2}{\sigma_{2 \rightarrow 2}^s(s_1')} \int dE_{p'}^0 \int d\phi_{p', \gamma^*}^0 \left| \mathcal{M}_{2 \rightarrow 3}^s \right|^2$$

- Then we boost the splitting kernel back to the lab frame to calculate differential cross section:

$$\frac{d\sigma_{\text{PB}}}{dE_{\gamma^*}} = \int dE_{\gamma^*}^0 d \cos \theta_{p, \gamma^*}^0 \frac{d^2 \mathcal{P}_{p \rightarrow \gamma^* p}}{dE_{\gamma^*}^0 d \cos \theta_{p, \gamma^*}^0} \sigma_{p, \text{air}}(s_2') \delta(E_{\gamma^*}' - E_{\gamma^*})$$

# Proton Bremsstrahlung

$$d\sigma(P_1 + P_2 \rightarrow \gamma^* X \rightarrow \chi \bar{\chi} X) = d\sigma(P_1 + P_2 \rightarrow \gamma^* X) \times \frac{Q_\chi^2}{12\pi^2} \frac{dk_{\gamma^*}^2}{k_{\gamma^*}^2} \sqrt{1 - \frac{4m_\chi^2}{k_{\gamma^*}^2}} \left(1 + \frac{2m_\chi^2}{k_{\gamma^*}^2}\right).$$

S. N. Gninenko, et al. 1810.06856