

# Alfven Wave Dynamics in the Magnetar Magnetosphere

**Xinyu Li** 李昕宇

Department of Astronomy, Tsinghua University

Collaborators: Andrei Beloborodov, Alex Chen, Yajie Yuan, Jens Mahlmann, Jonathan Zrake, Jie-Shuang Wang

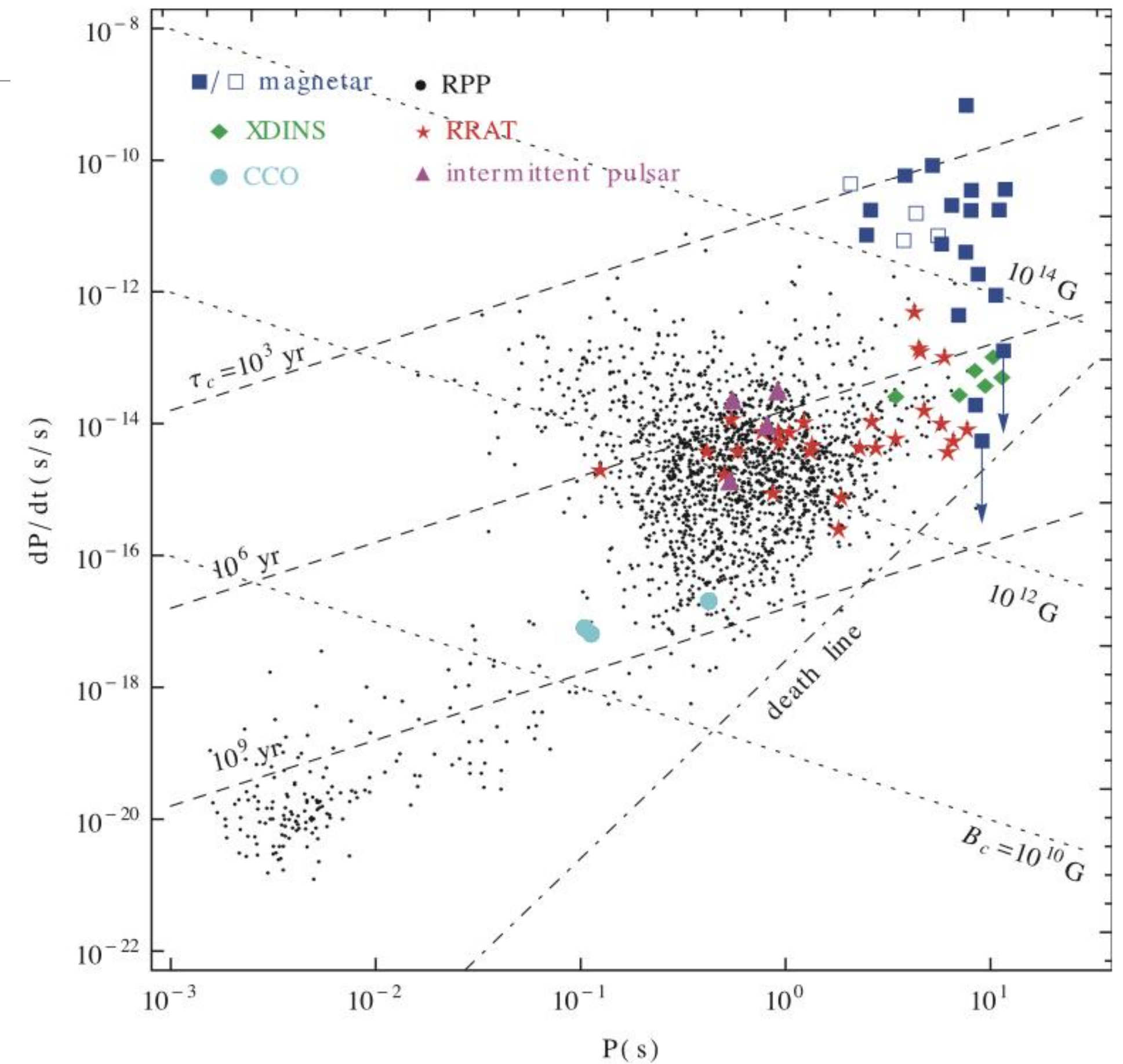


清华大学天文系  
Department of Astronomy, Tsinghua University



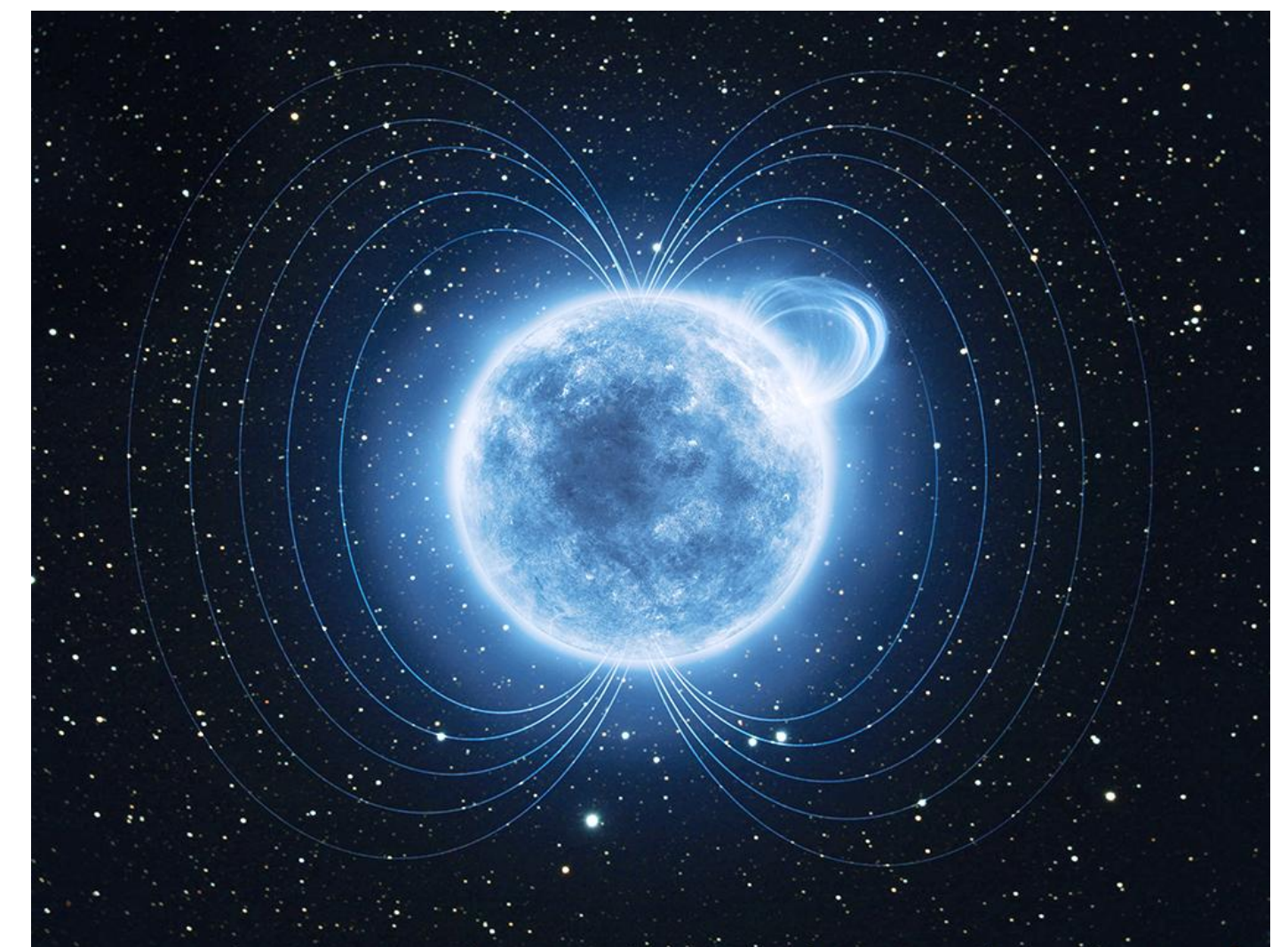
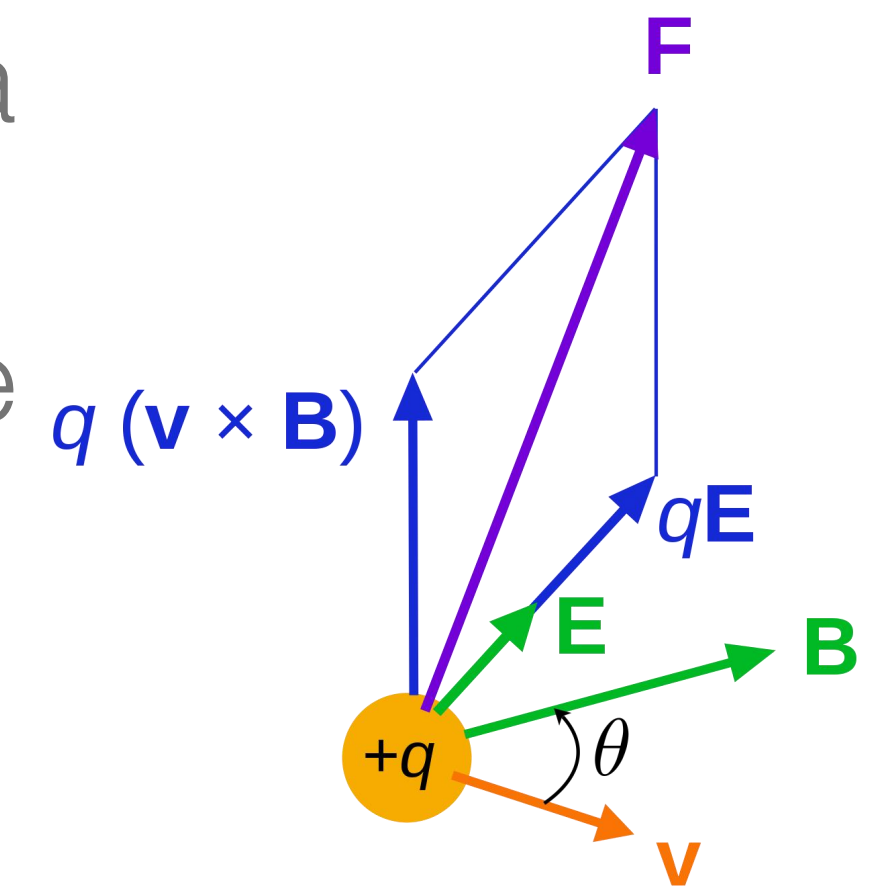
# Magnetars

- Ultra-strong magnetic field up to  $10^{15}$  G
- Slow rotation period 1-10s
- SGR1935: FRB with X-ray bursts



# Magnetosphere: Force-Free Electrodynamics (FFE)

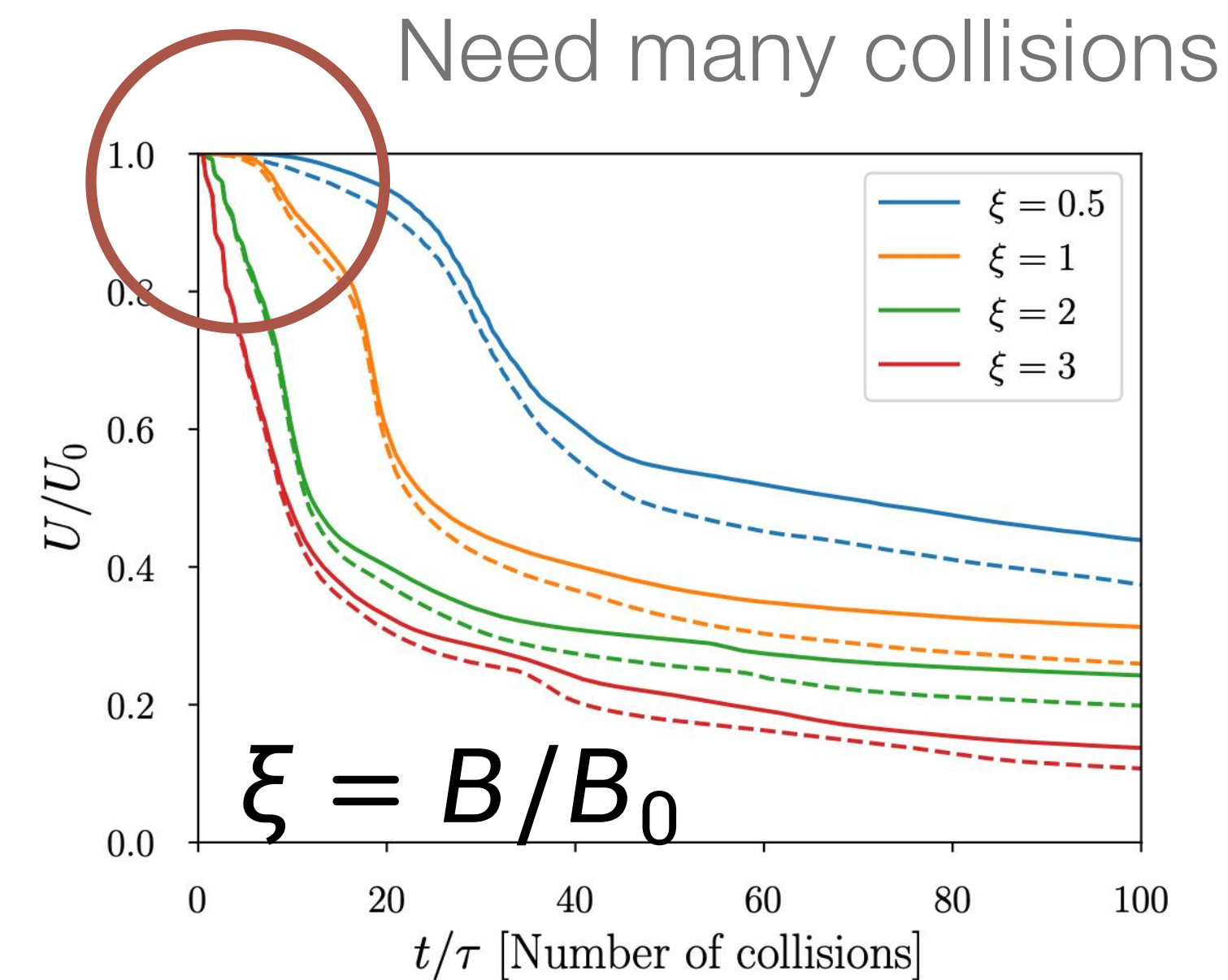
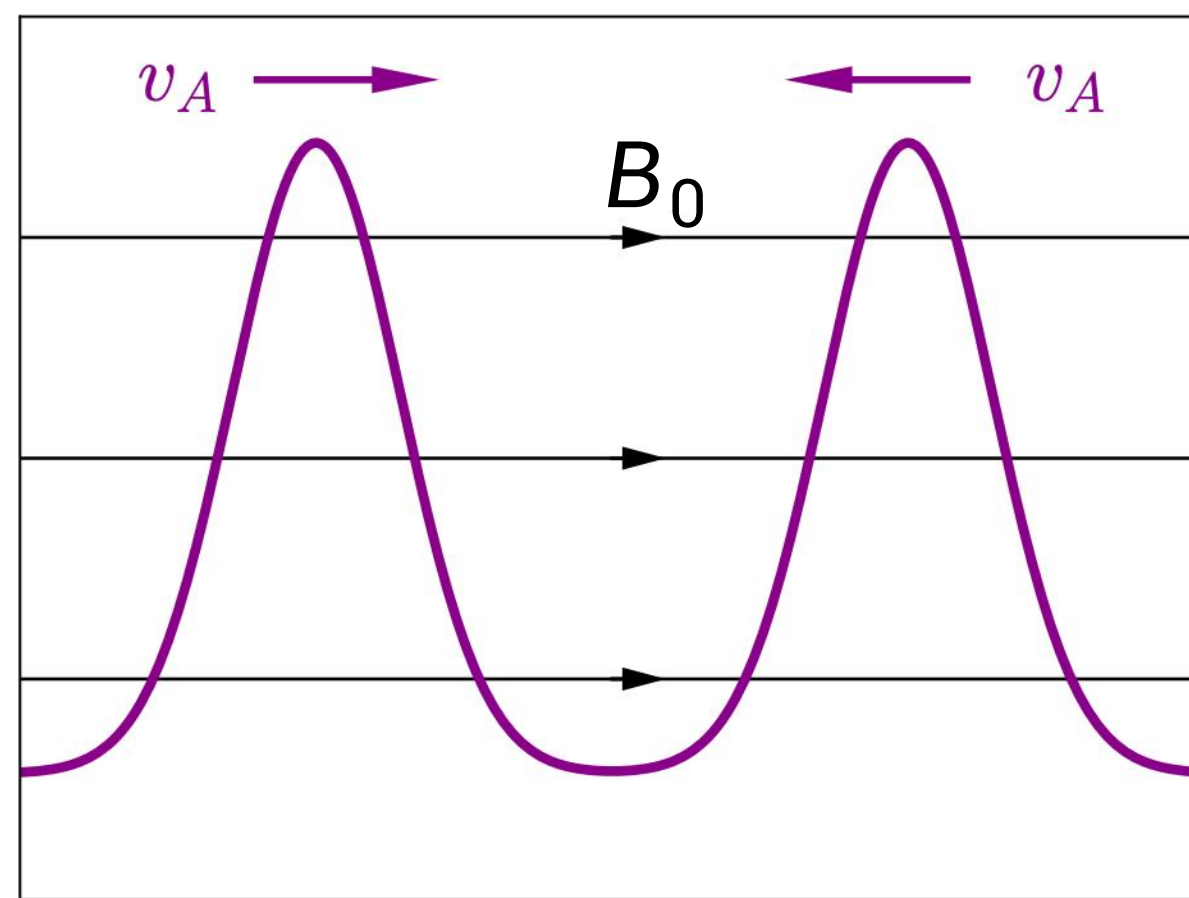
- Magnetic energy dominates over the rest mass energy of the plasma
- The plasma follows the field dynamics with a vanishing Lorentz force
- Need force-free conditions  $E < B$   $E \cdot B = 0$
- **Alfven waves:** guided to move along field lines
- **Fast waves:** propagate like in vacuum
- Three-wave interactions through  $A + A \rightarrow F$





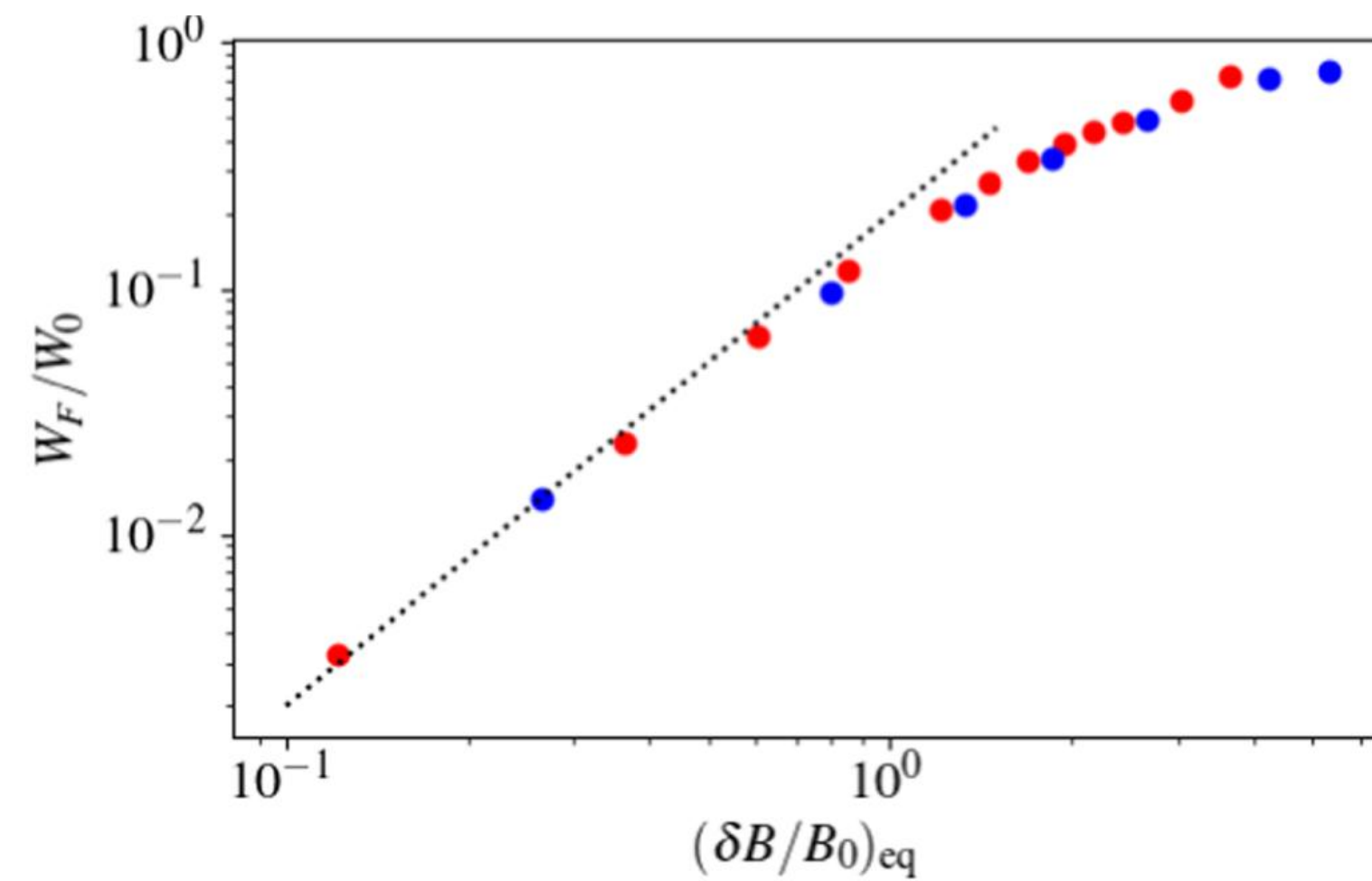
# Nonlinear Wave Interaction in FFE

- FFE simulation (WENO) of a pair of counter-propagating Alfvén waves in a periodic box
- Turbulent anisotropic forward cascade, dissipation is weak
- Fast waves carries away a few percent of wave energy

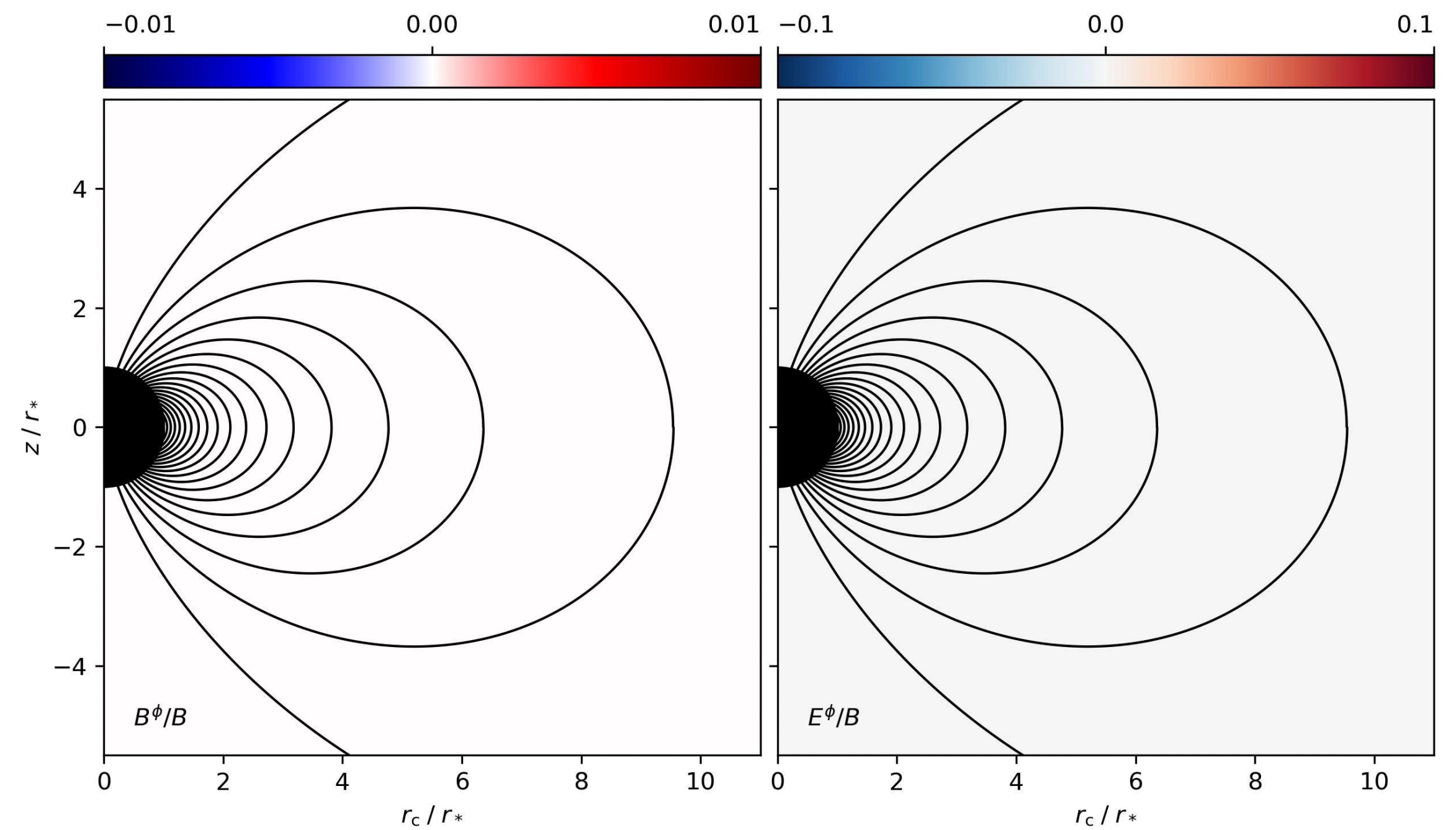


# Alfven Wave in the Dipole Magnetosphere

- Outgoing fast waves are spontaneously launched
- Alfven waves become strongly sheared



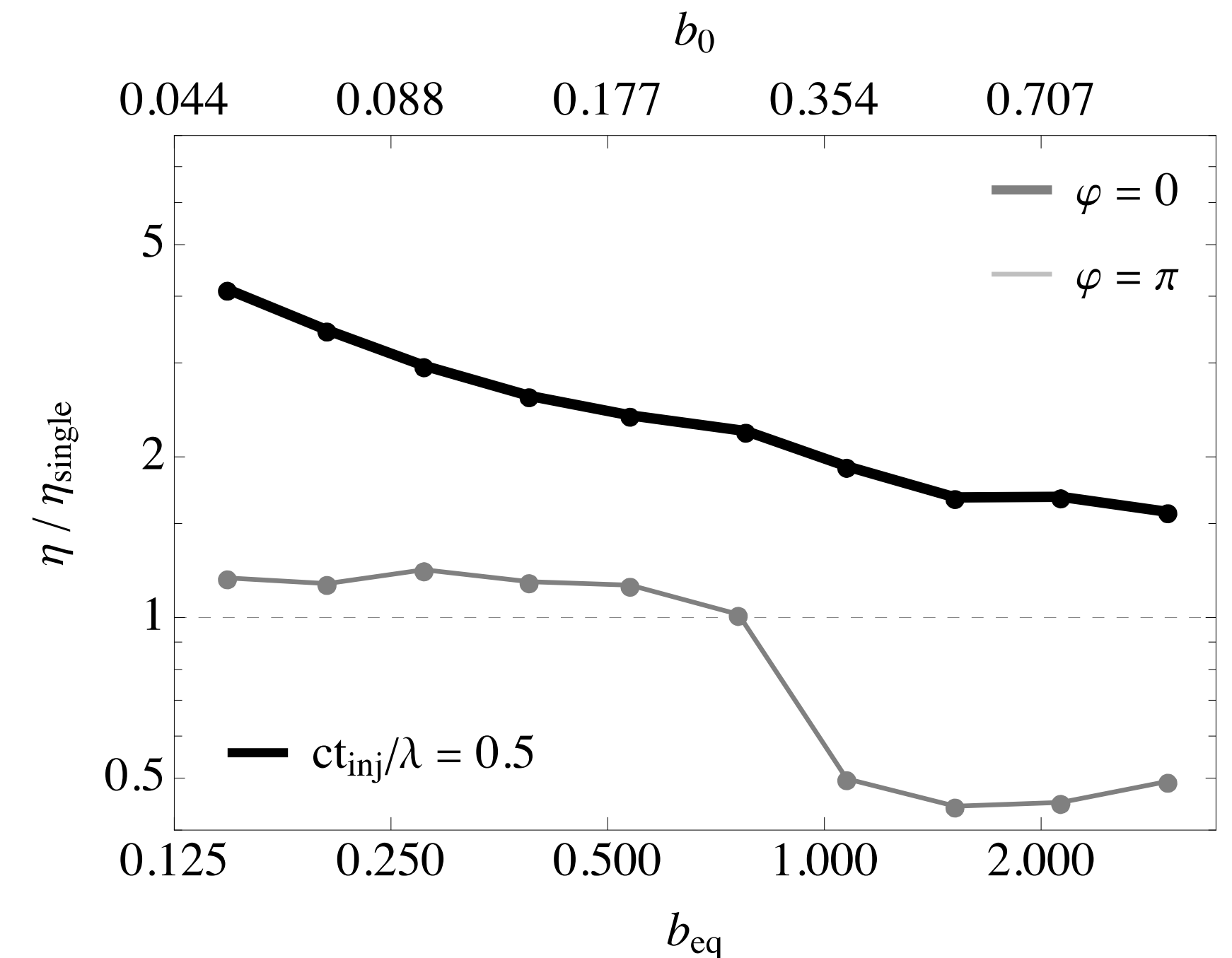
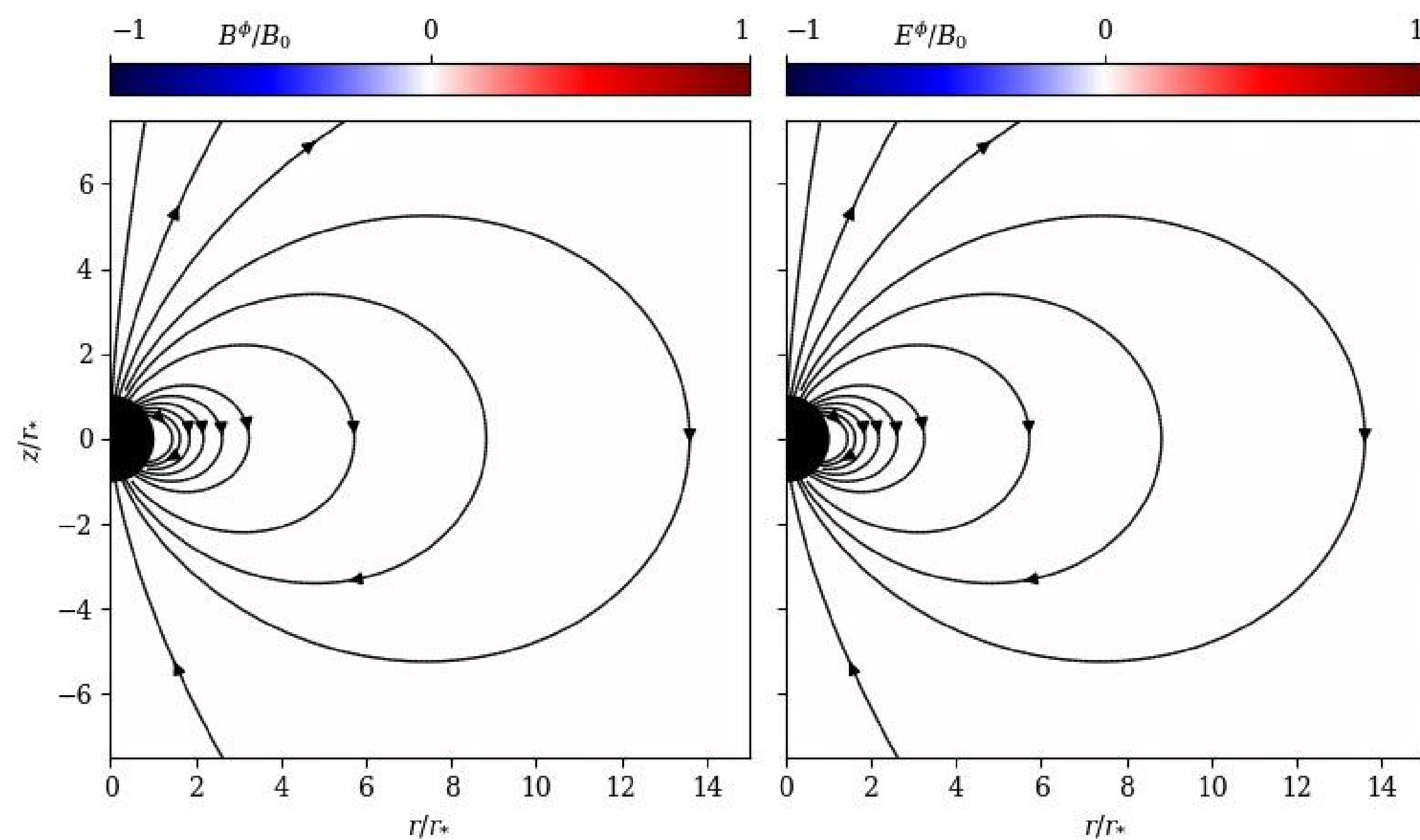
Yuan et al. 2021



Mahlmann & Li, in prep

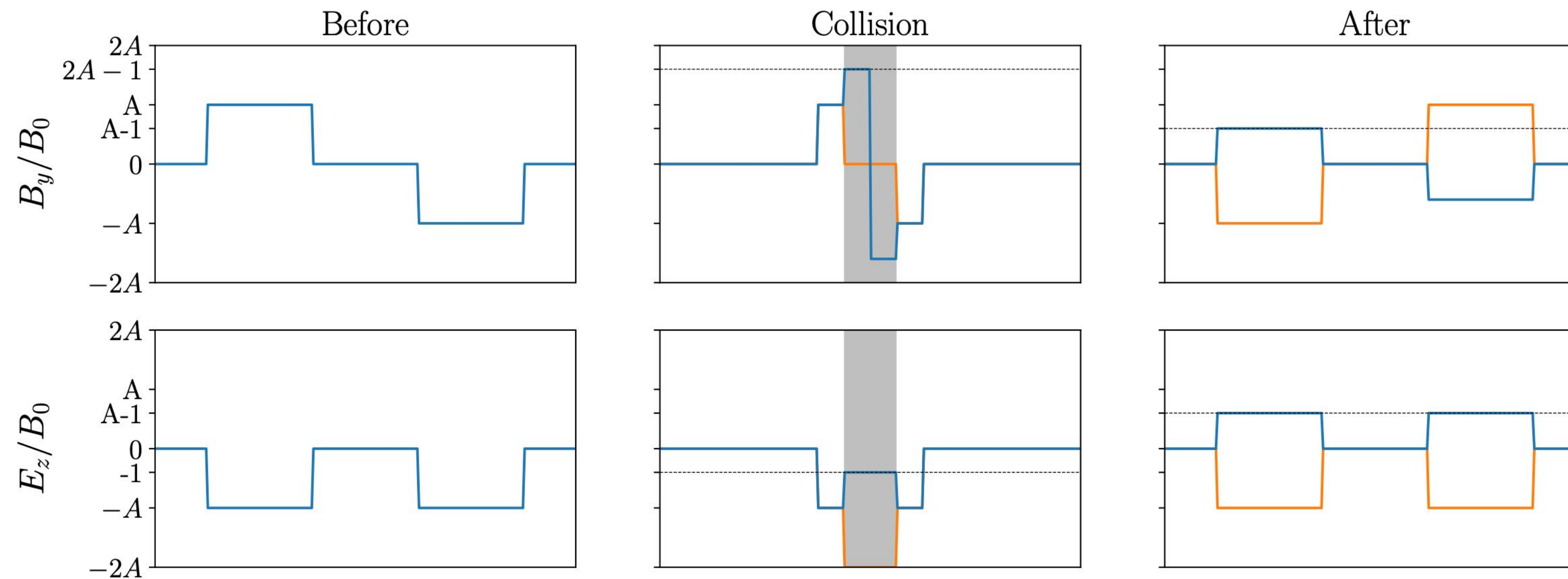
# Wave Interactions in the Dipole Magnetosphere

- Enhanced rate of fast wave generation — —only for the case the two waves have the same polarization
- Fast waves propagating outward can break the FFE condition



# Wave Collision: Break the FFE Condition

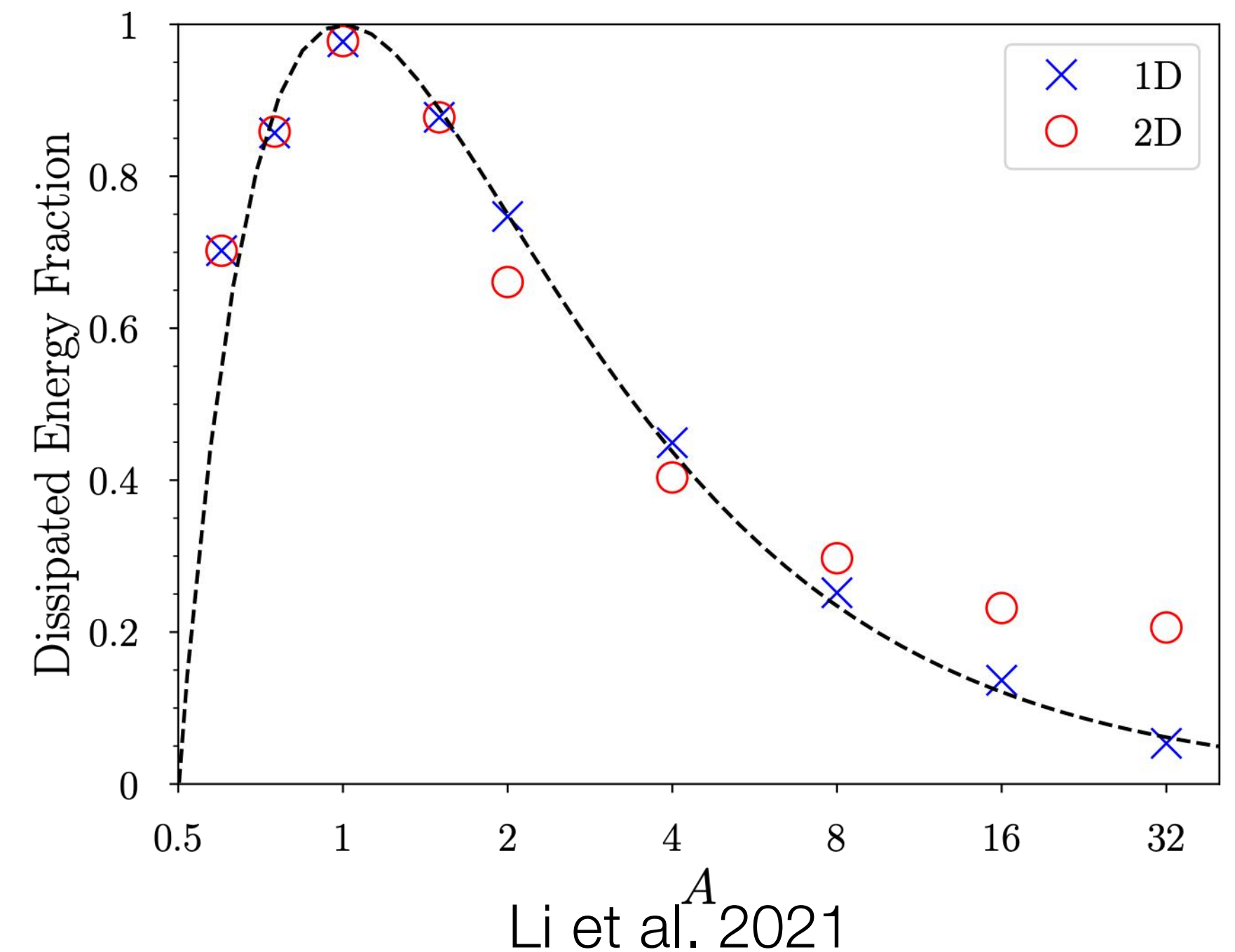
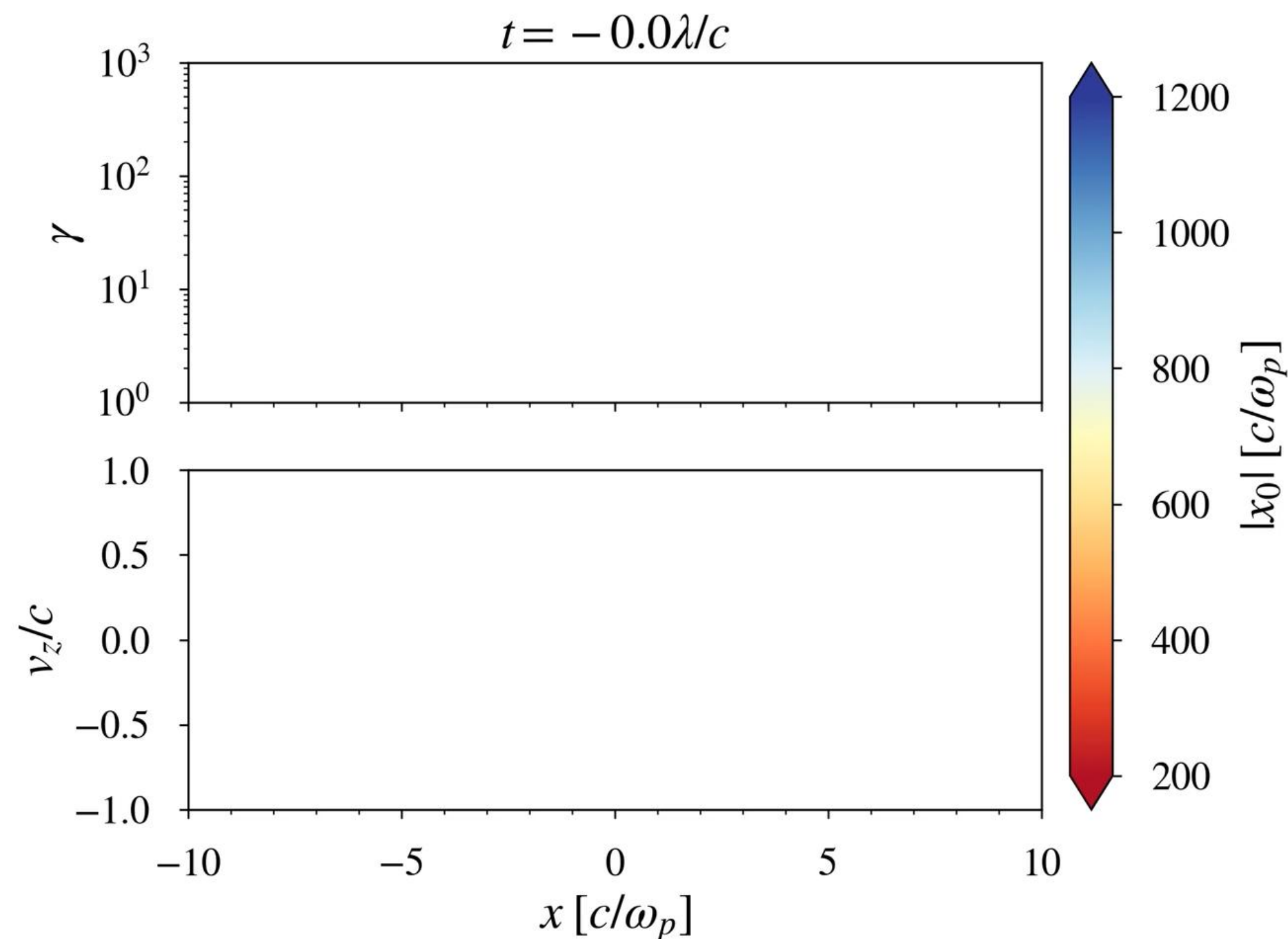
- Particles are accelerated to form a current sheet and reduce the electrical field close to  $B_0$ .
- Incoming waves are reflected with amplitude  $|A-1|$ .
- A large part  $f = (2A - 1)/A^2$  of the incoming wave energy is dissipated to particles.





# Wave Collision: Break the FFE Condition

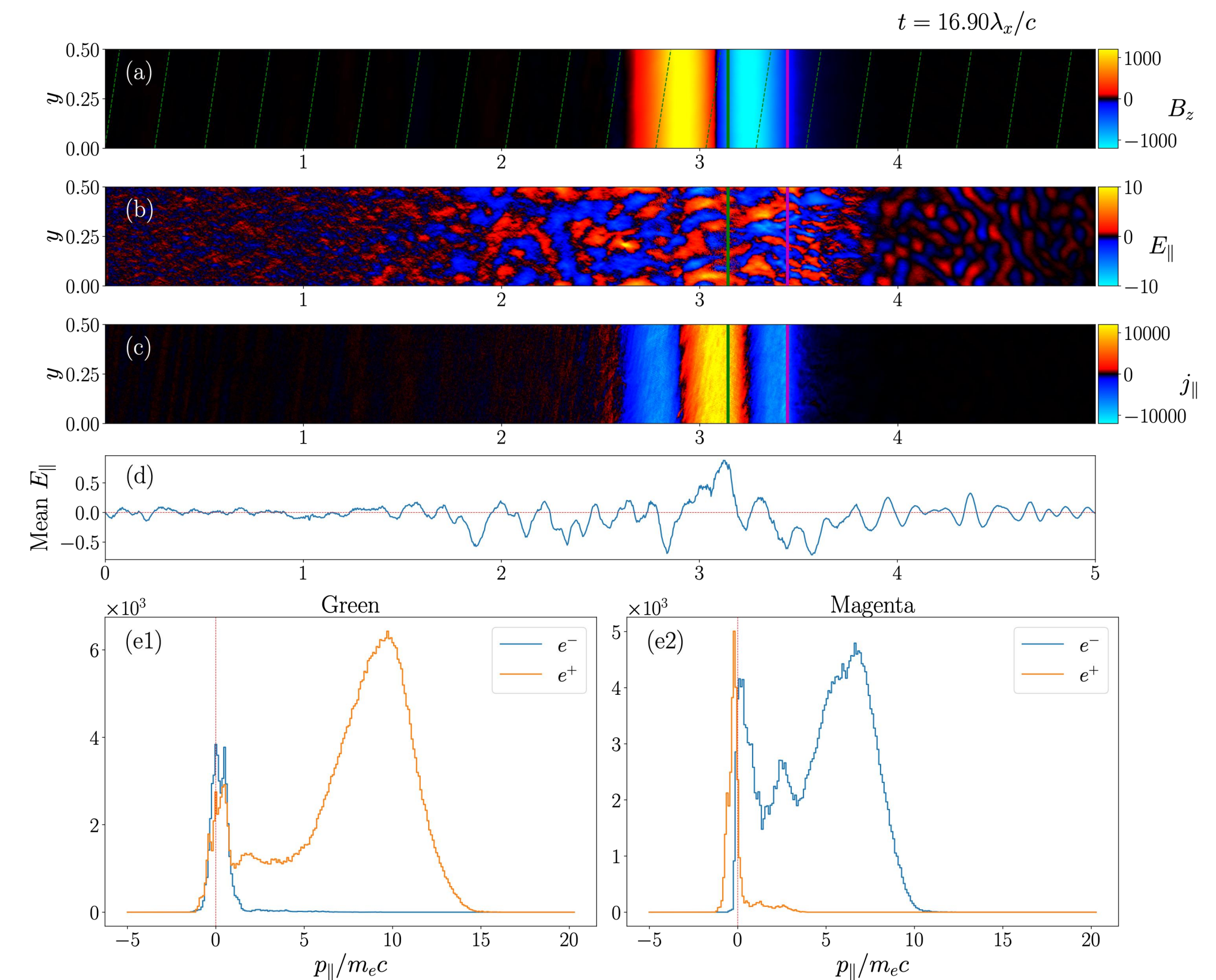
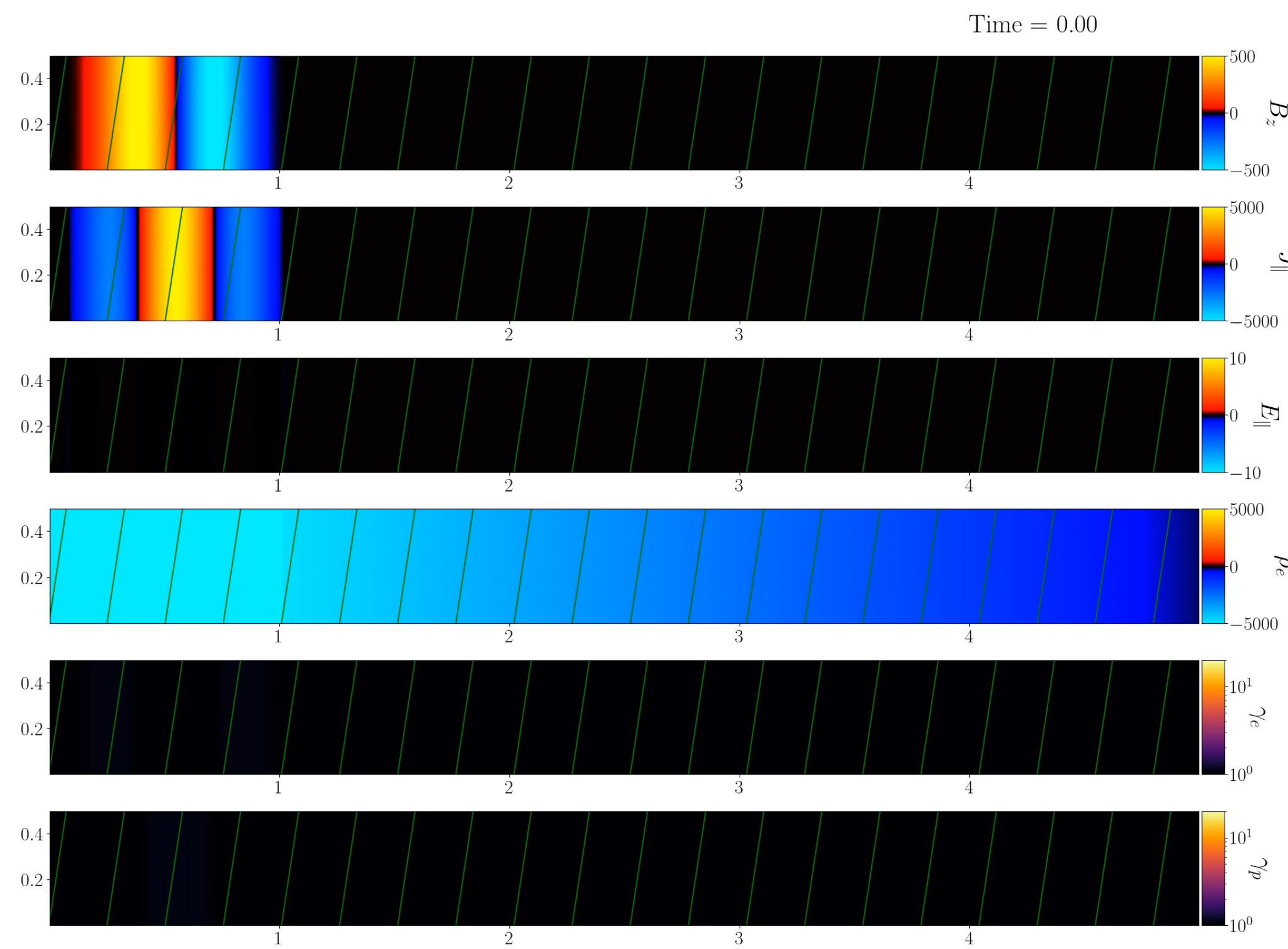
- 1D dissipation agrees with analytical calculations  $f = (2A - 1)/A^2$ , ~100% efficiency for  $A=1$ .
- For 2D cases, dissipation of large amplitude waves is dominated by normal reconnection with dissipated fraction ~20%.





# Strongly Sheared Alfven Waves

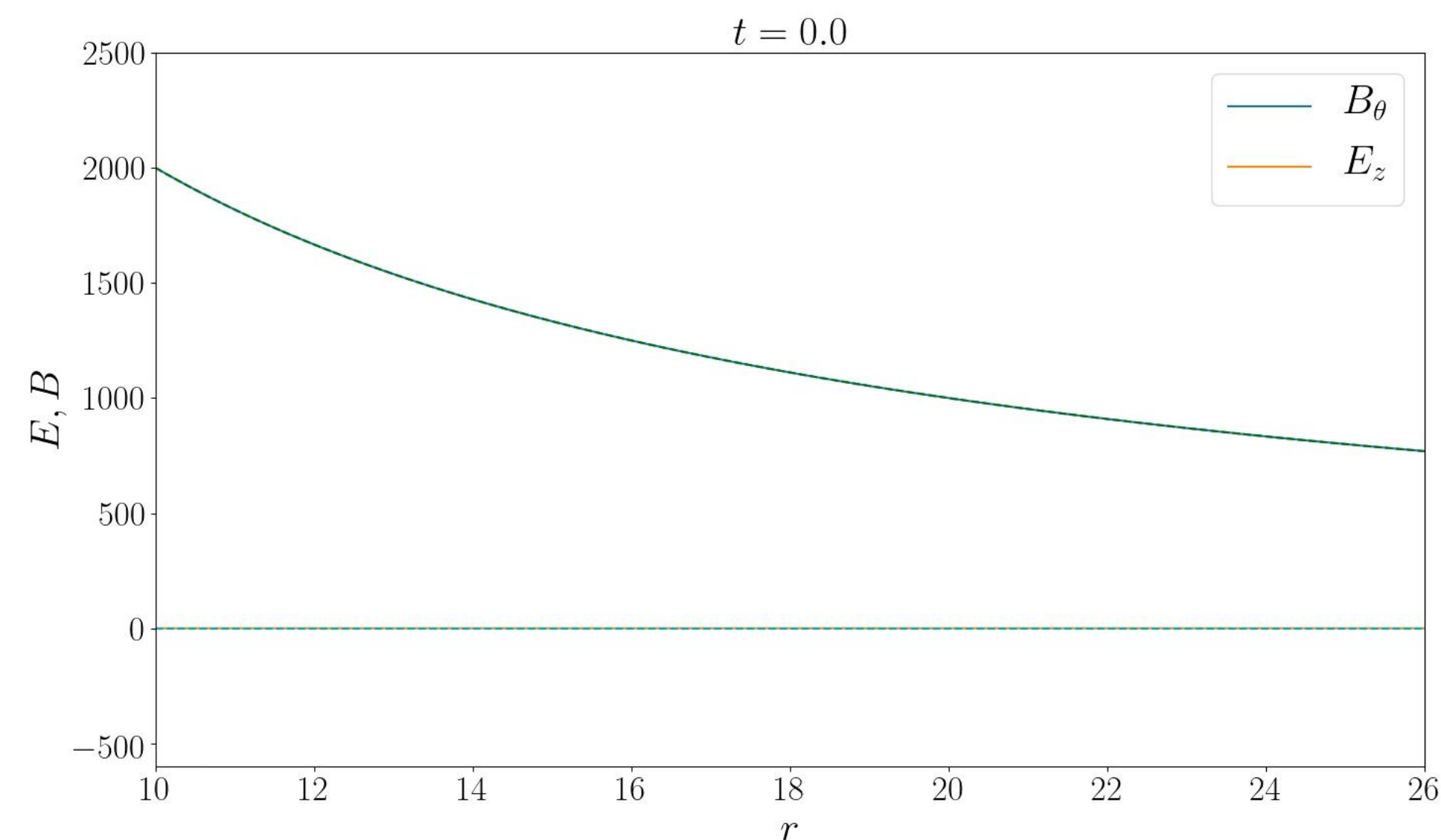
- **No charge starvation!** Particles advected with the waves get accelerated to support the current for wave propagation.



# Strong Wave Propagation

---

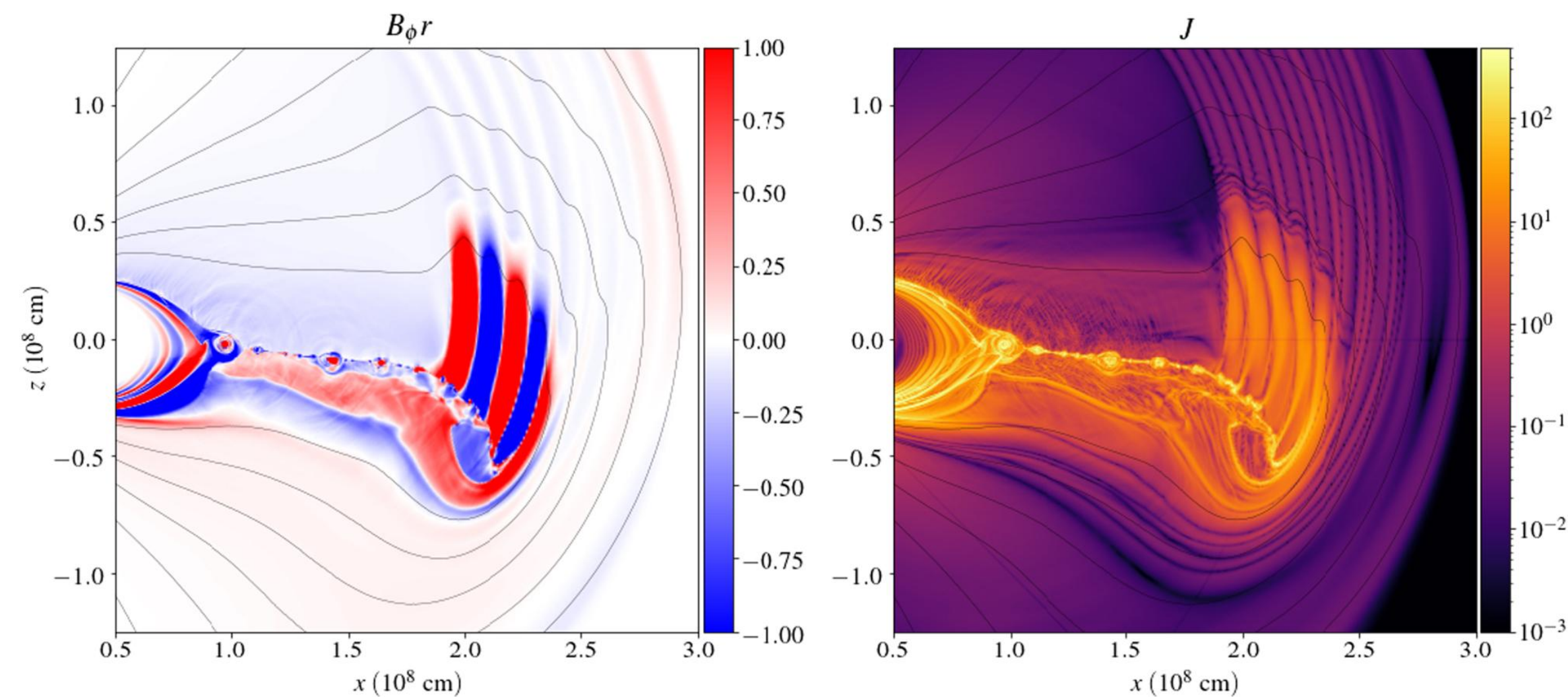
- Wave steepens into a shock. Plasma particles drift into the shock and undergo coherent gyration, and subsequently become thermalized.
- Quickly dissipates the energy of strong waves emitted deep within the magnetosphere, preventing GHz waves (FRB) from escaping (Beloborodov 2021,2022,2023)
- May provide an alternative way to launch shocks in the magnetosphere without requiring a relativistic ejecta



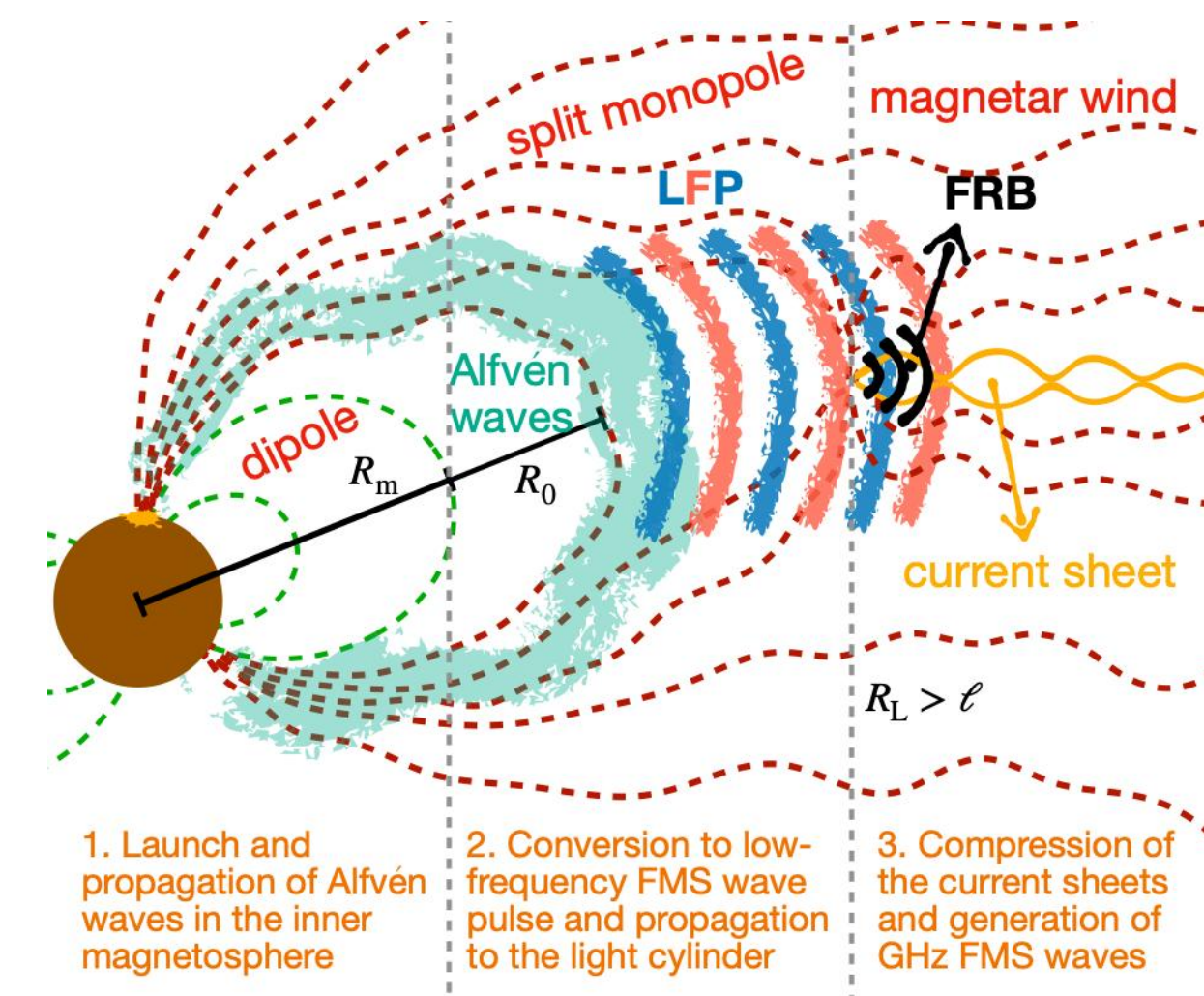


# Application to FRB models

- **Near Field Model:** No charge starvation. Strong GHz waves (FRB) generated near the magnetar can't escape (Beloborodov 2021,2022,2023)
- **Far Field Model:** Relativistic plasmoid ejection drives blast waves to form shocks (Yuan 2020)
- **Intermediate Field Model:** Fast wave driven reconnection (Wang et al. 2022)



Yuan et al. 2021



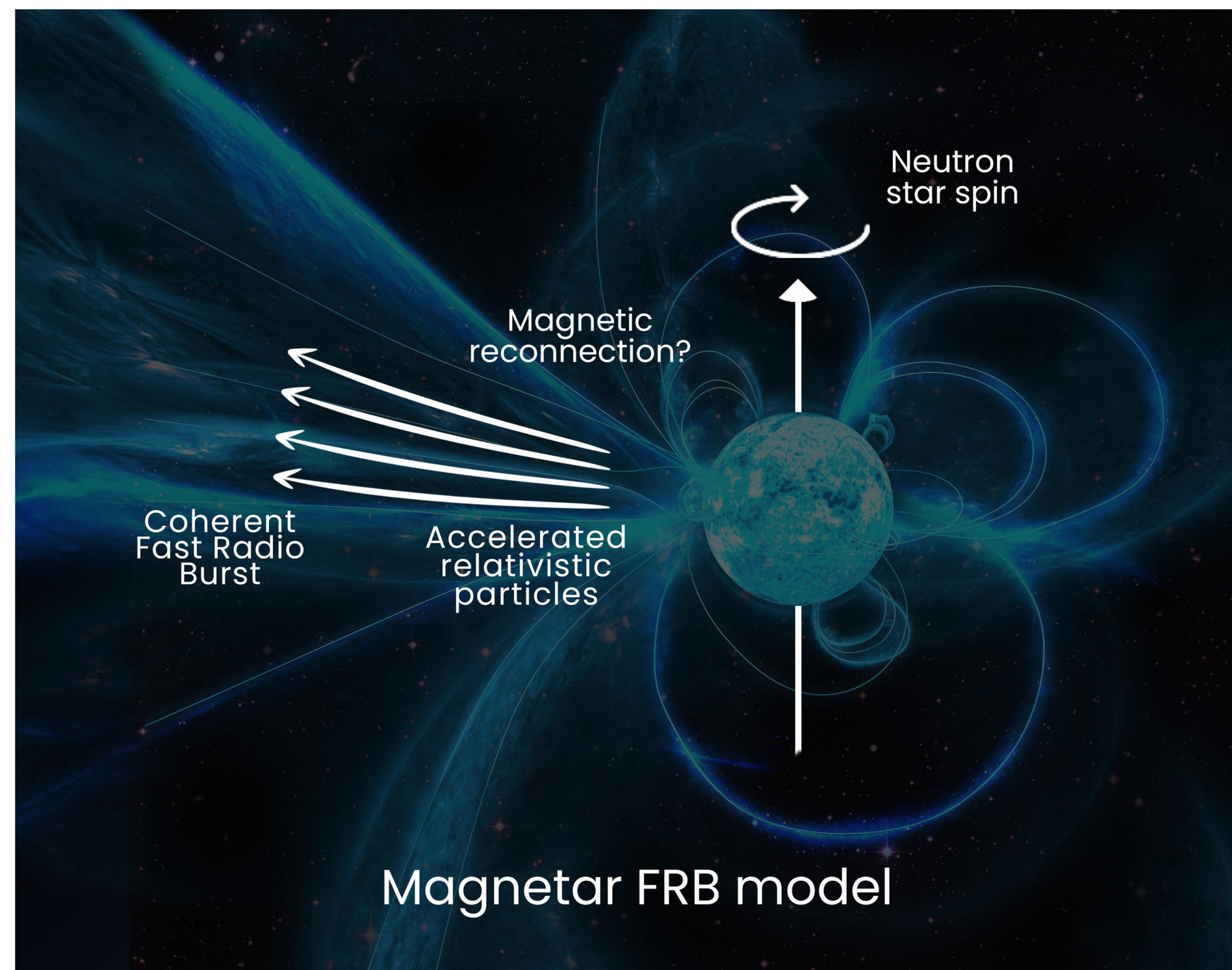
Wang et al. 2023



# Conclusion

---

- Rich physics of Alfven waves and plasmas in the magnetosphere!
- More work needed to understand it before we can fully figure the origin of fast radio bursts





Thank you for your  
attention!

