

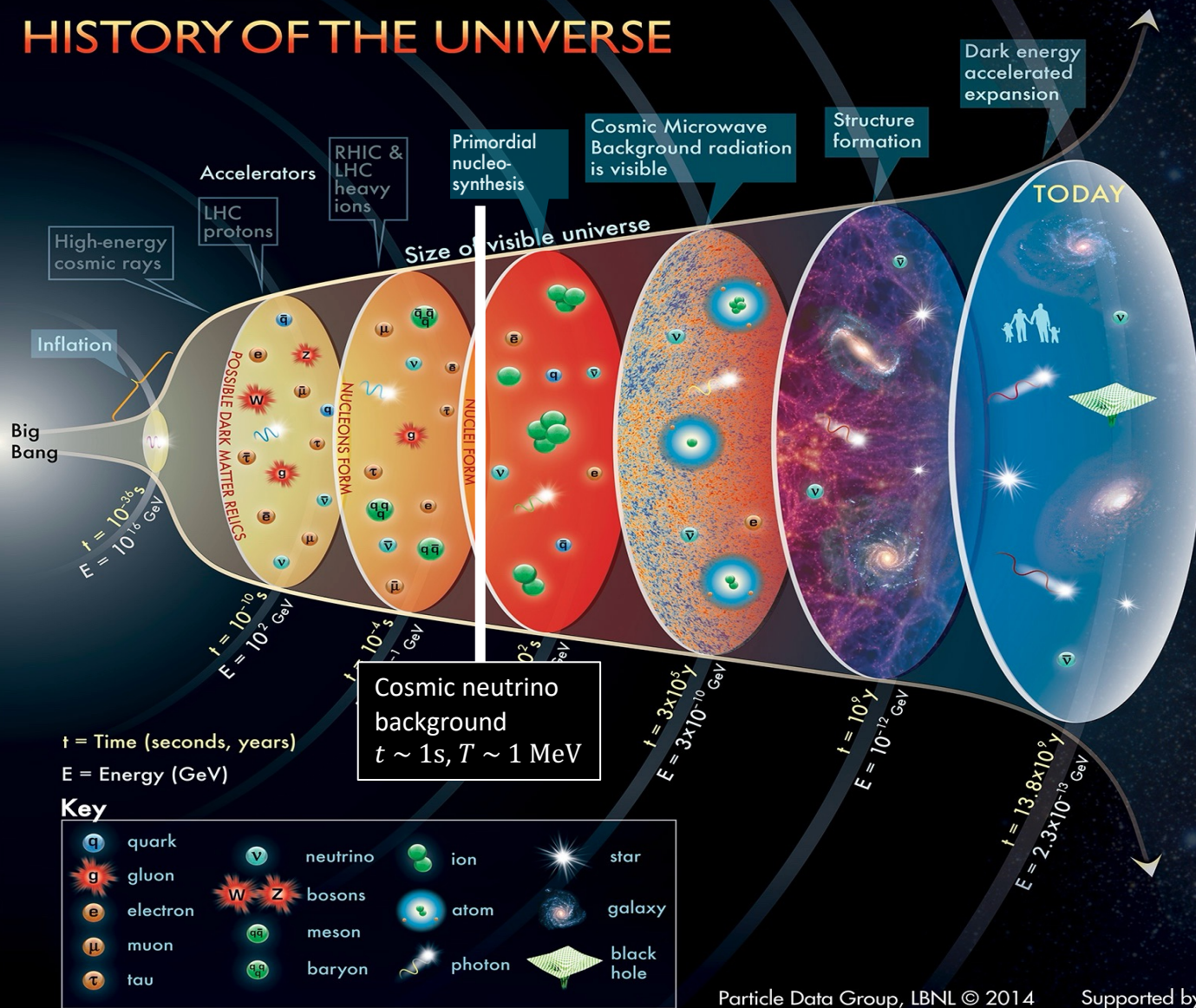
Neutrino (and other particle) physics in large-scale structure

Yvonne Y. Y. Wong

UNSW Sydney

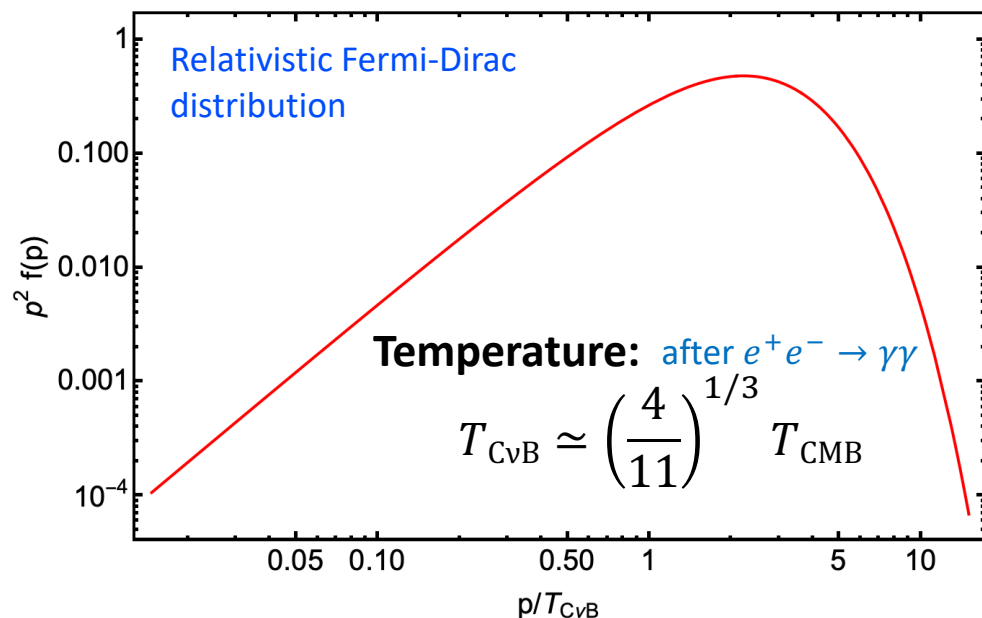
The 32nd Texas Symposium on Relativistic Astrophysics, Shanghai,
December 11-15, 2023

HISTORY OF THE UNIVERSE



The cosmic neutrino background...

Standard model predictions



Number density: Per family of neutrinos +antineutrinos

$$n_{\text{CvB}} \approx 110 \text{ cm}^{-3}$$

Energy density: Per family

- Relativistic (if $T_{\text{CvB}} \gg m_\nu$):

$$\rho_{\text{CvB}} \approx \frac{7}{8} \left(\frac{4}{11}\right)^{\frac{4}{3}} \rho_{\text{CMB}} \approx 0.227 \rho_{\text{CMB}}$$

- Non-rel (if $T_{\text{CvB}} \ll m_\nu$):

Neutrino (hot) dark matter

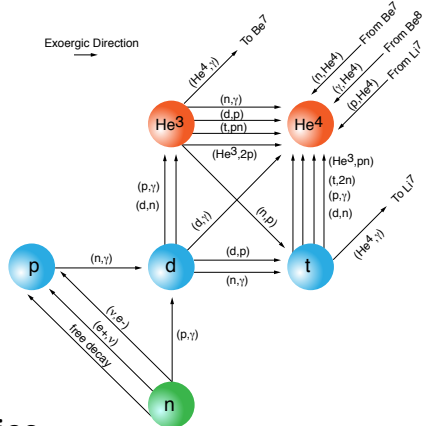
$$\Omega_{\text{CvB}} \approx \frac{m_\nu}{93 h^2 \text{ eV}}$$

Reduced Hubble parameter

Cosmological bounds on neutrino physics...

How the CνB affects the **events that take place after its formation** can be **exploited to constrain its properties**.

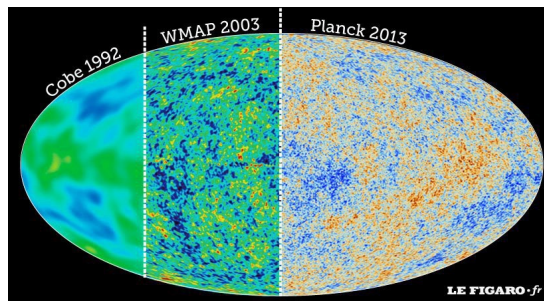
Light element abundances



Properties
of the CνB
probed:

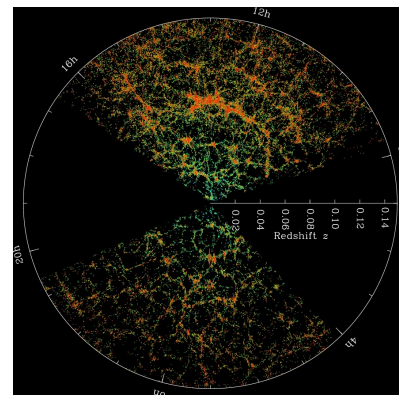
N_{eff} (expansion rate)

CMB anisotropies



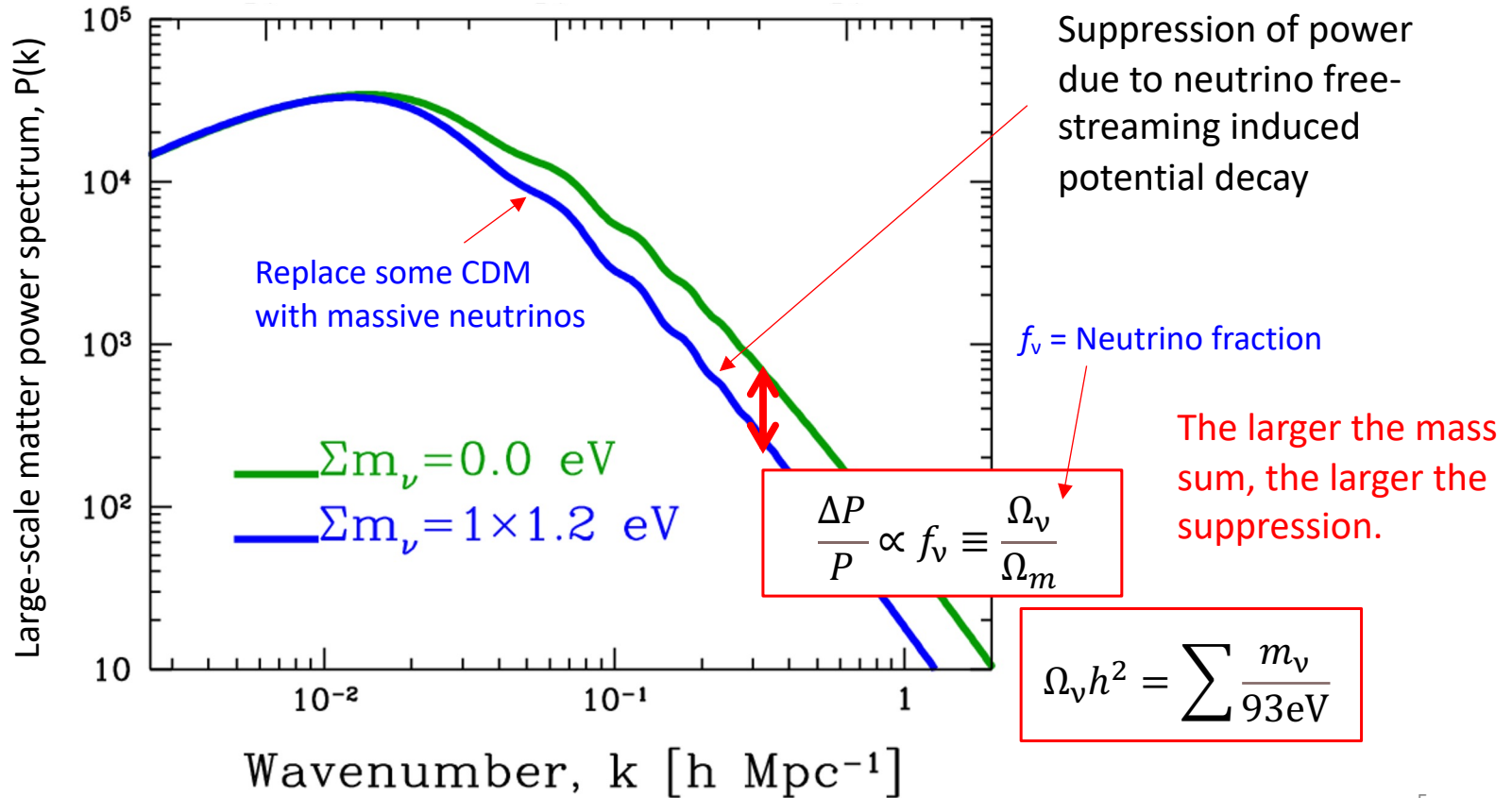
N_{eff} (expansion rate)
 $\sum m_\nu$ (perturbation growth)
 Interactions (free-streaming)
 Lifetime (free-streaming)

Large-scale matter distribution



$\sum m_\nu$ (perturbation growth)
 Interactions (free-streaming)
 Lifetime (free-streaming)

E.g., neutrino masses & perturbation growth...



Constraints on the neutrino mass sum...

Λ CDM+neutrino mass 7-parameter fit; 95% C.L. on $\sum m_\nu$ in [eV].

Two different high- ℓ
likelihood functions

		+CMB lensing	+BAO (non-CMB)	+CMB lensing+BAO
Planck2018 TT+lowE	0.54	0.44	0.16	0.13
2015 number	0.72	0.68	0.21	n/a
Planck2018 TT +lowE+TE+EE	0.26	0.24	0.13	0.12
Planck2018 TT +lowE+TE+EE [CamSpec]	0.38	0.27	n/a	0.13
2015 number	0.49	0.59	0.17	n/a

Planck2015 TT+lowP+Ly α

$$\sum m_\nu < 0.13 \text{ eV}$$

Aghanim et al. [Planck] 2018

Ade et al. [Planck] 2015

Palanque-Delabrouille et al. 2015

What to expect in the future?

Galaxies,
cosmic shear,
clusters, etc.



ESA Euclid

2024

1σ sensitivity to $\sum m_\nu$

0.011 – 0.02 eV

1σ sensitivity to N_{eff}

0.05



LSST

2024

0.015 eV

0.05

These numbers mean, if the true neutrino mass sum is $\sum m_\nu = 0.06$ eV (minimum number required by neutrino oscillation experiments), then it will be **possible to measure it with $(3 - 5)\sigma$ significance**.

Variants on the same theme...

Some other **BSM particle physics** scenarios can also be constrained in the same way.

- E.g., for sufficiently **small axion decay constants** f_a , a **thermal background of QCD axions** can be produced via $\pi + \pi \rightarrow \pi + a$ in the early universe ($T \sim \Lambda_{\text{QCD}} \sim 200$ MeV).
- **Analogous to the CνB** → the **axion mass** m_a can be constrained in the same way as $\sum m_\nu$.

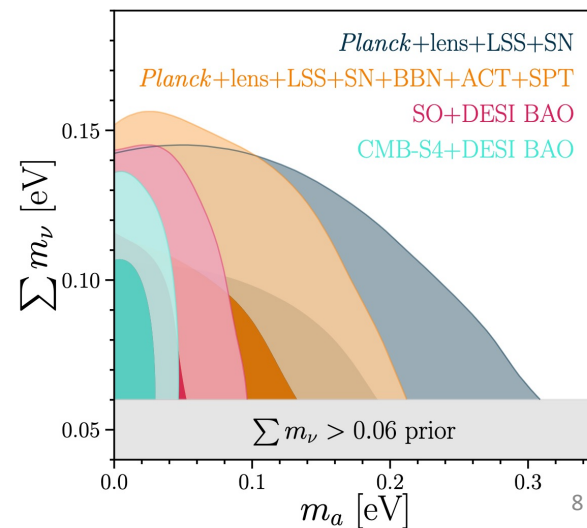
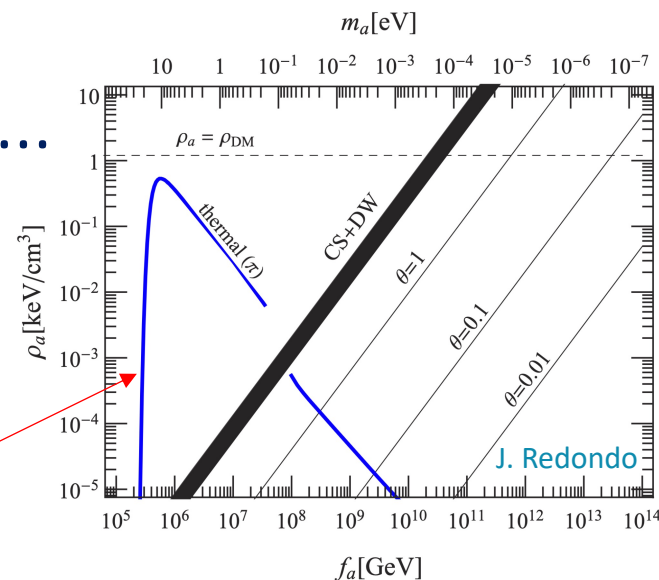
Bianchini, Cortona & Valli 2023

Also:

Notari, Rompineve & Villadoro 2023

D'Eramo et al. 2022

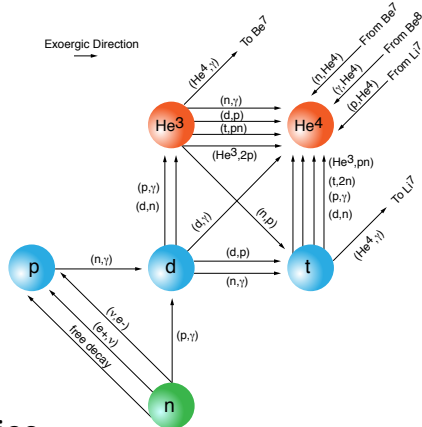
Hannestad, Mirizzi, Raffelt & Y³W 2007, 2008, 2010, 2013, etc.



Cosmological bounds on neutrino physics...

How the CνB affects the **events that take place after its formation** can be **exploited to constrain its properties**.

Light element abundances



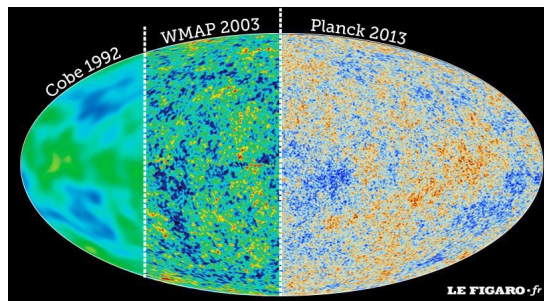
Properties
of the CνB
probed:

N_{eff} (expansion rate)

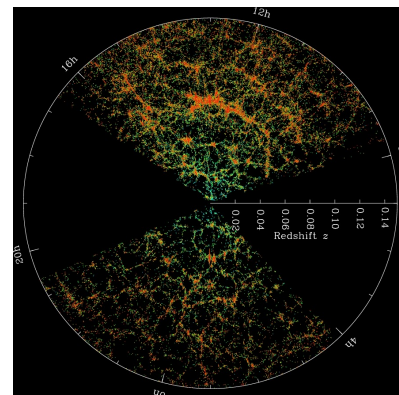


N_{eff} (expansion rate)
 $\sum m_\nu$ (perturbation growth)
 Interactions (free-streaming)
 Lifetime (free-streaming)

CMB anisotropies



Large-scale matter distribution



$\sum m_\nu$ (perturbation growth)
 Interactions (free-streaming)
 Lifetime (free-streaming)

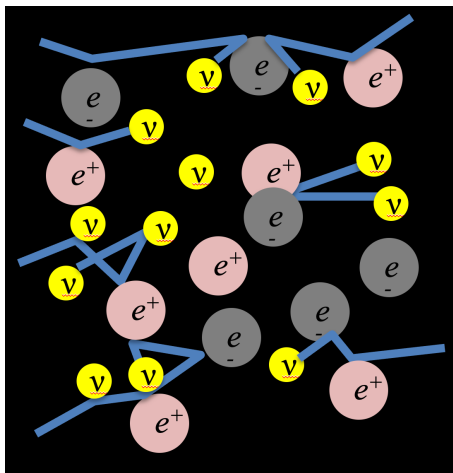
Constraining non-standard
neutrino interactions & lifetime...

Cosmic neutrino background ...

Interaction rate: $\Gamma_{\text{weak}} \sim G_F^2 T^5$

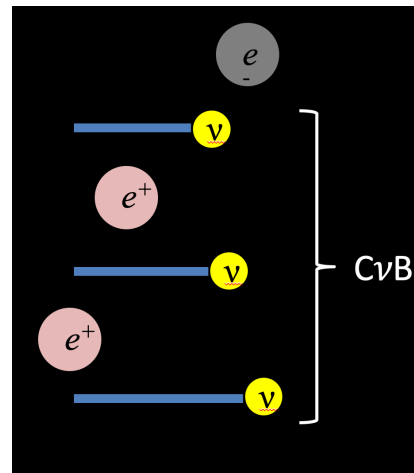
Expansion rate: $H \sim M_{\text{pl}}^{-2} T^2$

The CνB is formed when neutrinos **decouple** from the cosmic plasma.



($T_{\odot \text{core}} \sim 1 \text{ keV}$)

Above $T \sim 1 \text{ MeV}$, even weakly-interacting neutrinos can be produced, scatter off e^+e^- and other neutrinos, and attain **thermodynamic equilibrium**



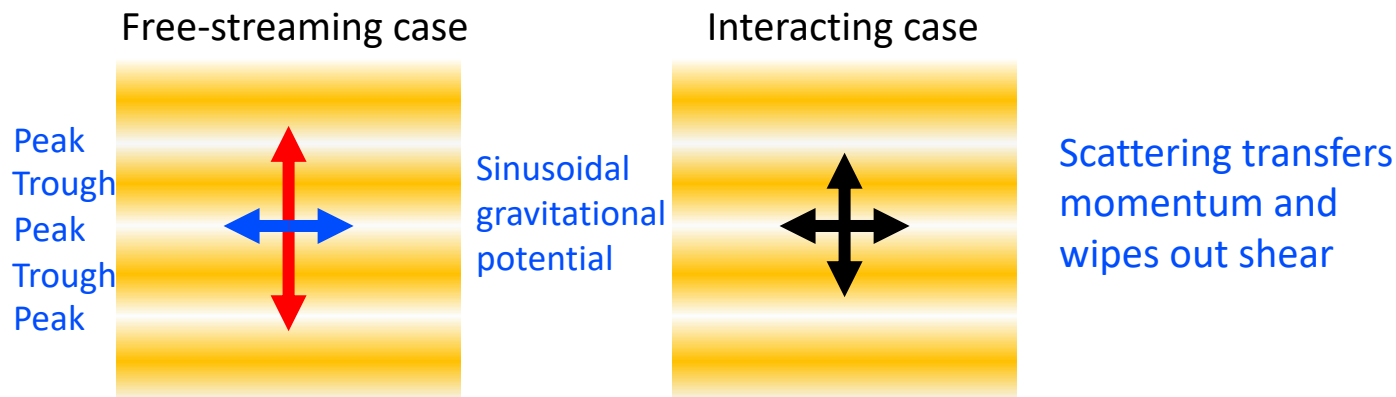
Neutrinos
“free-stream”
to infinity.

Below $T \sim 1 \text{ MeV}$, expansion dilutes plasma, and reduces interaction rate: the universe becomes **transparent to neutrinos**.

Neutrino free-streaming vs interactions...


Standard-model neutrinos free-stream.

- Free-streaming in an inhomogeneous background induces **shear stress (aka momentum anisotropy)**.
- Conversely, **interactions** transfer momentum and, if sufficiently efficient, can **wipe to out shear**.





Neutrino shear stress & the metric...

Neutrino shear stress (or lack thereof) leaves distinct imprints on the spacetime **metric perturbations**.

Scale factor  Conformal Newtonian gauge

$$ds^2 = a^2(\tau)[-(1 + 2\psi)d\tau^2 + (1 - 2\phi)dx^i dx_i]$$

where $k^2(\phi - \psi) = 12\pi G a^2(\bar{\rho} + \bar{P})\sigma$

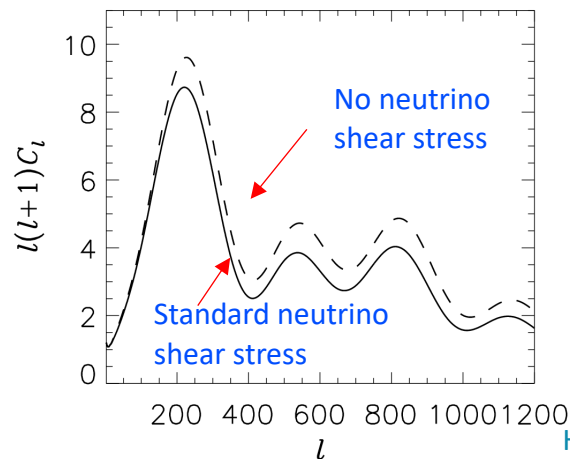
Mean energy density & pressure  Shear stress 

In Λ CDM, mainly from ultra-relativistic neutrinos and photons.

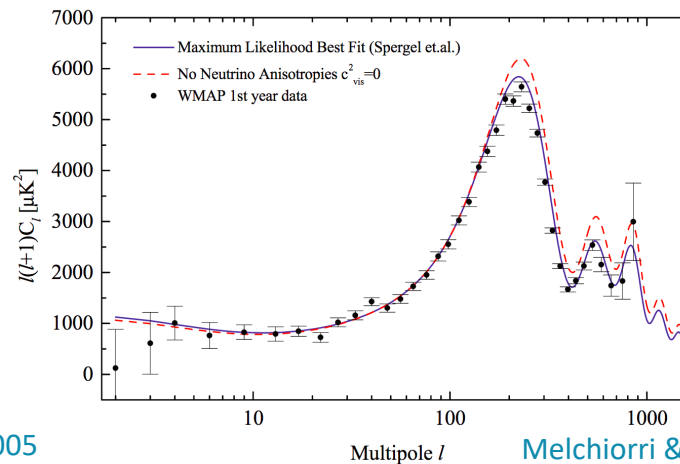
- Changes to $(\phi - \psi)$ at CMB formation times affect the **evolution of CMB perturbations** and are observable in the **TT power spectrum**.
- In turn, the **evolution of ϕ and ψ** individually can influence **growth of matter perturbations**.

Neutrino shear stress & the CMB...

That the **CMB prefers neutrino shear stress to no shear stress** has been known for a long time.



Hannestad 2005



Melchiorri & Trotta 2005

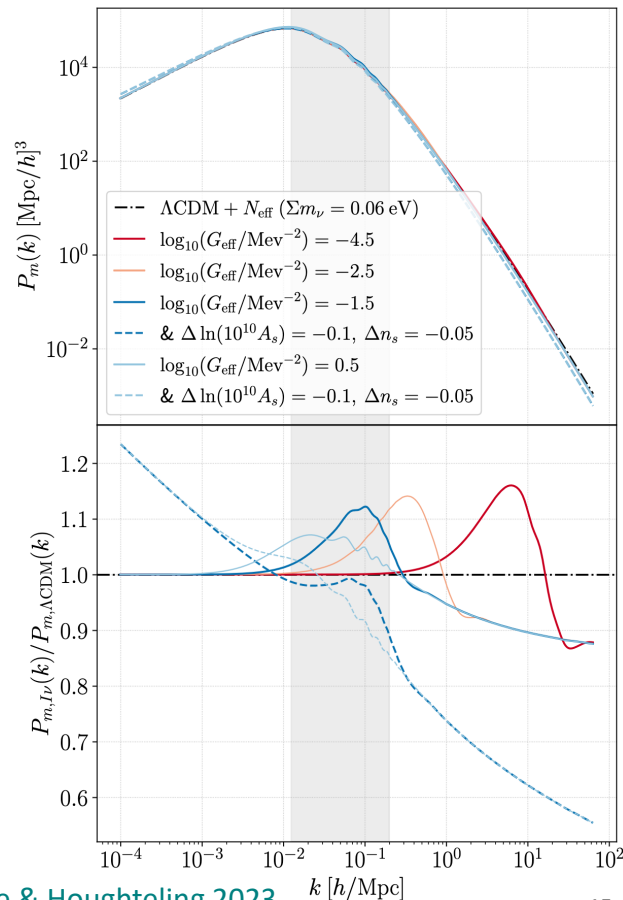
- The tricky part is in translating this preference to constraints on the **fundamental parameters** of a non-standard neutrino interaction

→ What is the **isotropisation timescale** given an interaction?  I'll come back to this in a bit.

Neutrino shear stress & LSS power spectrum...

Neutrino shear stress (or lack thereof) also has a signature in the **mildly-nonlinear part of the matter power spectrum**.

- Large neutrino shear stress expected only **during and shortly after radiation domination**, when neutrinos are **ultra-relativistic**.
 - Observable signatures are thus **confined to small scales** that entered the horizon at the said times.
- There is however room for improvement in the modelling of the LSS signature....



Isotropisation timescale $T_{\text{isotropise}} \dots$

The key to **connecting anisotropic stress loss to a non-standard neutrino interaction** lies in the isotropisation timescale.

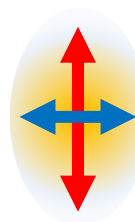
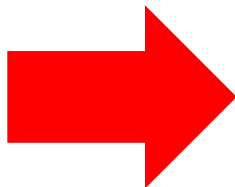
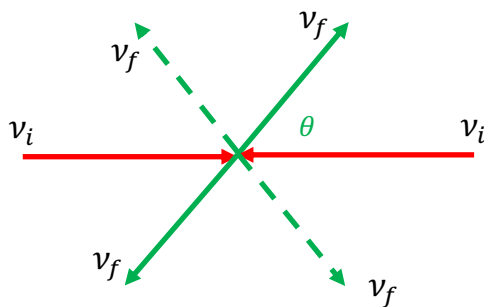
- Given an interaction Lagrangian, $T_{\text{isotropise}}$ is calculable.
- Write down the **Boltzmann equation**:

$$\begin{aligned} P^\alpha \frac{\partial f}{\partial x^\alpha} - \Gamma_{\alpha\beta}^\gamma P^\alpha P^\beta \frac{\partial f}{\partial P^\gamma} = & \frac{1}{2} \left(\prod_j^N \int g_j \frac{d^3 \mathbf{n}_j}{(2\pi)^3 2E_j(\mathbf{n}_j)} \right) \left(\prod_k^M \int g_k \frac{d^3 \mathbf{n}_k}{(2\pi)^3 2E_k(\mathbf{n}_k)} \right) \\ & \times (2\pi)^4 \delta_D^{(4)} \left(p + \sum_j^N n_j - \sum_k^M n'_k \right) |\mathcal{M}_{i+j_1+\dots+j_N \leftrightarrow k_1+\dots+k_M}|^2 \\ & \times [f_{k_1} \dots f_{k_N} (1 \pm f_i)(1 \pm f_{j_1}) \dots (1 \pm f_{j_N}) - f_i f_{j_1} \dots f_{j_N} (1 \pm f_{k_1}) \dots (1 \pm f_{k_M})] \end{aligned}$$

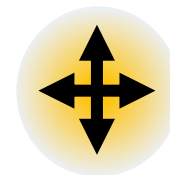
- Decompose in a Legendre series.
- The **damping rate of the quadrupole** ($\ell = 2$) moment is the **isotropisation rate**.

Example 1: ν self-interaction...

Isotropisation from 2-to-2 scattering $\nu_i + \nu_i \rightarrow \nu_f + \nu_f$.



Isotropisation
timescale



- The probability of ν_f emitted at any angle θ is the same for all $\theta \in [0, \pi]$.

Cyr-Racine & Sigurdson 2014; Oldengott, Rampf & Y³W 2015; Lancaster, Cyr-Racine, Knox & Pan 2017; Oldengott, Tram, Rampf & Y³W 2017; Kreisch, Cyr-Racine & Dore 2019; Forastieri et al. 2019; etc.

$$T_{\text{isotropise}} \sim 1/\Gamma_{\text{scattering}}$$

Scattering rate

$$\gtrsim 400 \text{ kyr}$$

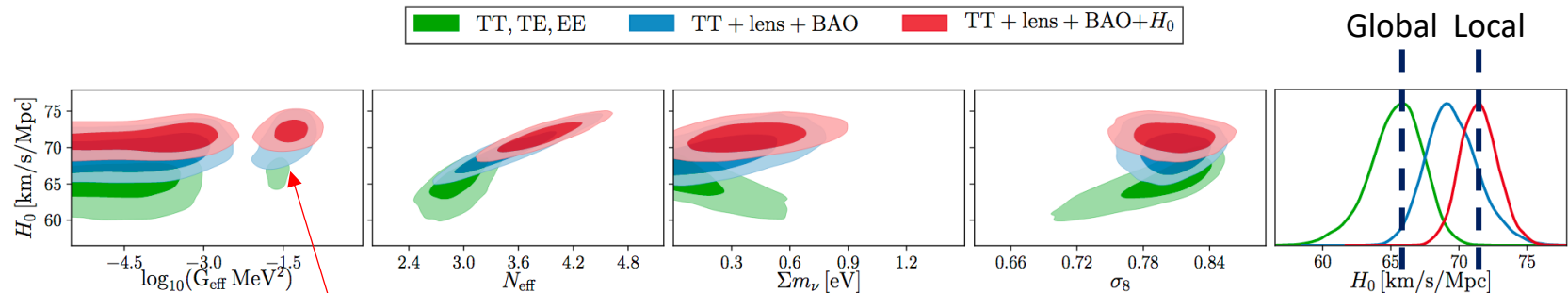
→ Upper limit on $\Gamma_{\text{scattering}}$
(hence coupling).

ν self-interaction and the H_0 tension...

Kreisch, Cyr-Racine & Dore 2019

Recent claim that self-interaction **alleviates the Hubble tension**.

- **Local/late time:** Cepheid-calibrated SNIa (SH0ES) and strong-lensing time delays (H0LiCOW); $H_0 = (73.5 \pm 1.4) \text{ km/s/Mpc}$
- **Global/early time:** Statistical inference from CMB anisotropies (Planck), weak lensing, BAO; $H_0 = (67.4 \pm 0.5) \text{ km/s/Mpc}$

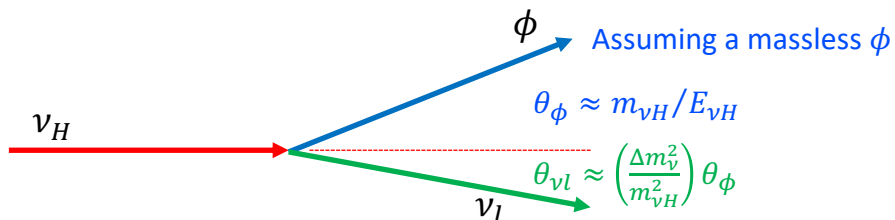


This island:
 $G_{\text{eff}} \sim 10^{10} G_F$

For now this is mainly a CMB result. But the scenario can be further tested in the mildly-nonlinear part of the matter power spectrum.

Example 2: Relativistic ν decay...

Isotropisation can also happen via $\nu_H \rightarrow \nu_l + \phi$ and its inverse process $\nu_l + \phi \rightarrow \nu_H$, but the rate is a bit more complicated.



In relativistic decay, the decay products are **beamed**.

Inverse decay can also only happen when the daughter particles satisfy **strict momentum/angular requirements**.

→ Isotropisation takes a **loooooong time**:

$$T_{\text{isotropise}} \sim (\theta_\phi \theta_{\nu l})^{-2} \gamma_{\nu H} \tau_{\text{rest}} \gtrsim 400 \text{ kyr}$$

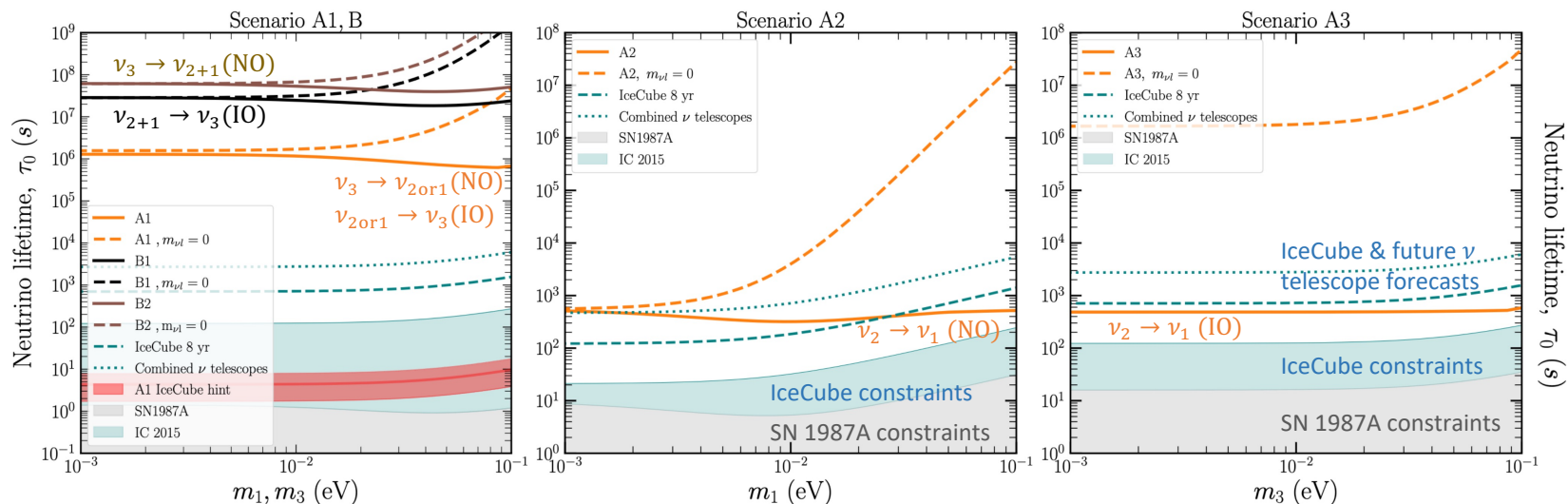
Boost
Rest-frame lifetime

Barenboim, Chen, Hannestad, Oldengott, Tram & Y³W 2021; Chen, Oldengott, Pierobon & Y³W 2022

→ Lower bound on τ_{rest} as a function of $m_{\nu H}$ and $m_{\nu l}$.

Lower bounds on the neutrino lifetime...

CMB currently gives the best limits on invisible neutrino decay $\nu_H \rightarrow \nu_l + \phi$.



NO = Normal mass ordering

IO = Inverted mass ordering

Chen, Oldengott, Pierobon & Y³W 2022

* IceCube constraints & forecasts from Song et al. 2021

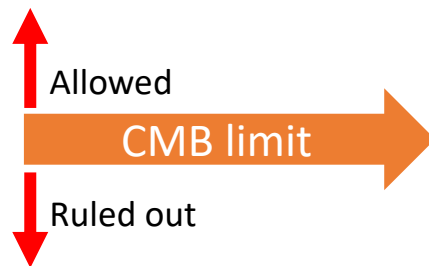
Lower bounds on the neutrino lifetime...

CMB currently gives the best limits on invisible neutrino decay $\nu_H \rightarrow \nu_l + \phi$.

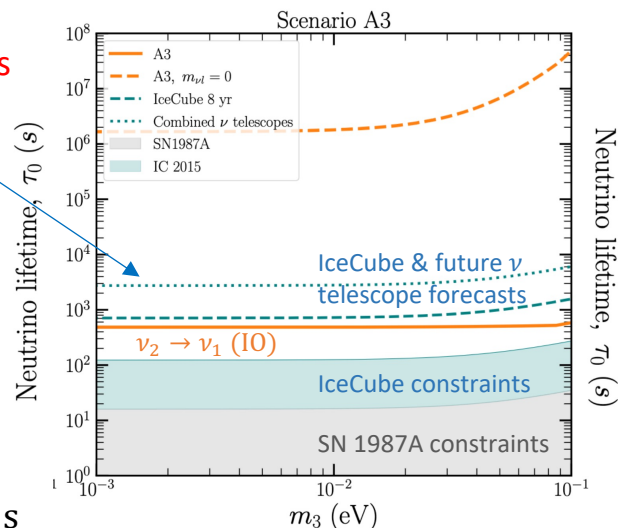


However, depending on the exact decay scenario, **neutrino telescopes** may become competitive in the future! Watch this space!

ν_3
 Inverted mass ordering



BBN: $\tau_0 \gtrsim 10^{-2} \rightarrow 10^{-1}$ s
 Solar ν : $\tau_0 \gtrsim 10^{-5} \rightarrow 10^{-4}$ s
 Lab ν : $\tau_0 \gtrsim 10^{-13} \rightarrow 10^{-11}$ s



Chen, Oldengott, Pierobon & Y³W 2022

* IceCube constraints & forecasts from Song et al. 2021

Lower bounds on the neutrino lifetime...

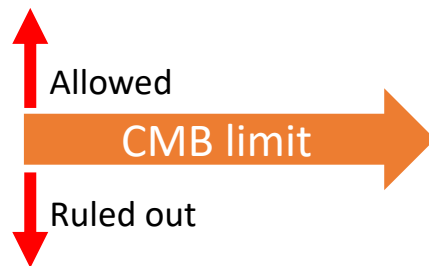
CMB currently gives the best limits on invisible neutrino decay $\nu_H \rightarrow \nu_l + \phi$.

ν_3

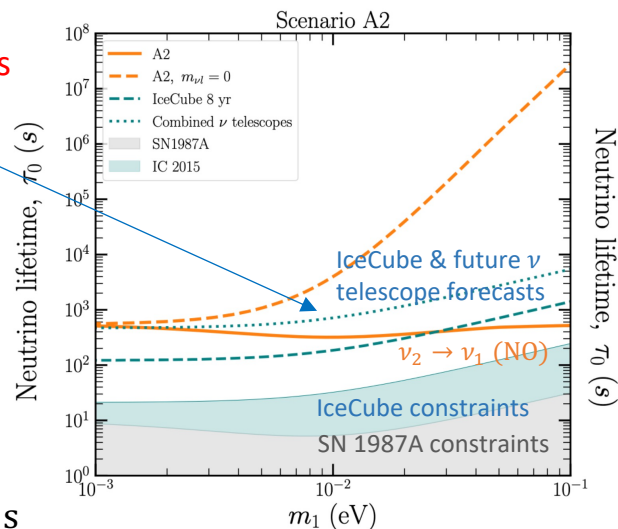
ν_2
 ν_1

Normal mass ordering

However, depending on the exact decay scenario, **neutrino telescopes** may become competitive in the future! Watch this space!



BBN: $\tau_0 \gtrsim 10^{-2} \rightarrow 10^{-1}$ s
Solar ν : $\tau_0 \gtrsim 10^{-5} \rightarrow 10^{-4}$ s
Lab ν : $\tau_0 \gtrsim 10^{-13} \rightarrow 10^{-11}$ s



Chen, Oldengott, Pierobon & Y³W 2022

* IceCube constraints & forecasts from Song et al. 2021

Summary...

It is well known that CMB/large-scale structure observations can set very **competitive upper limits on the neutrino mass sum**.

- But there are also **other well-motivated particle physics** scenarios, e.g., the QCD axion, that can be constrained in the same way.
- Furthermore, besides mass limits, CMB/LSS observations can also be used to probe **non-standard neutrino interactions** and to constrain the **neutrino lifetime**.
 - However, more work on modelling is required to predict the precise LSS signatures of these scenarios.