

Toward a new generation of reflection models for precision measurements of accreting black holes

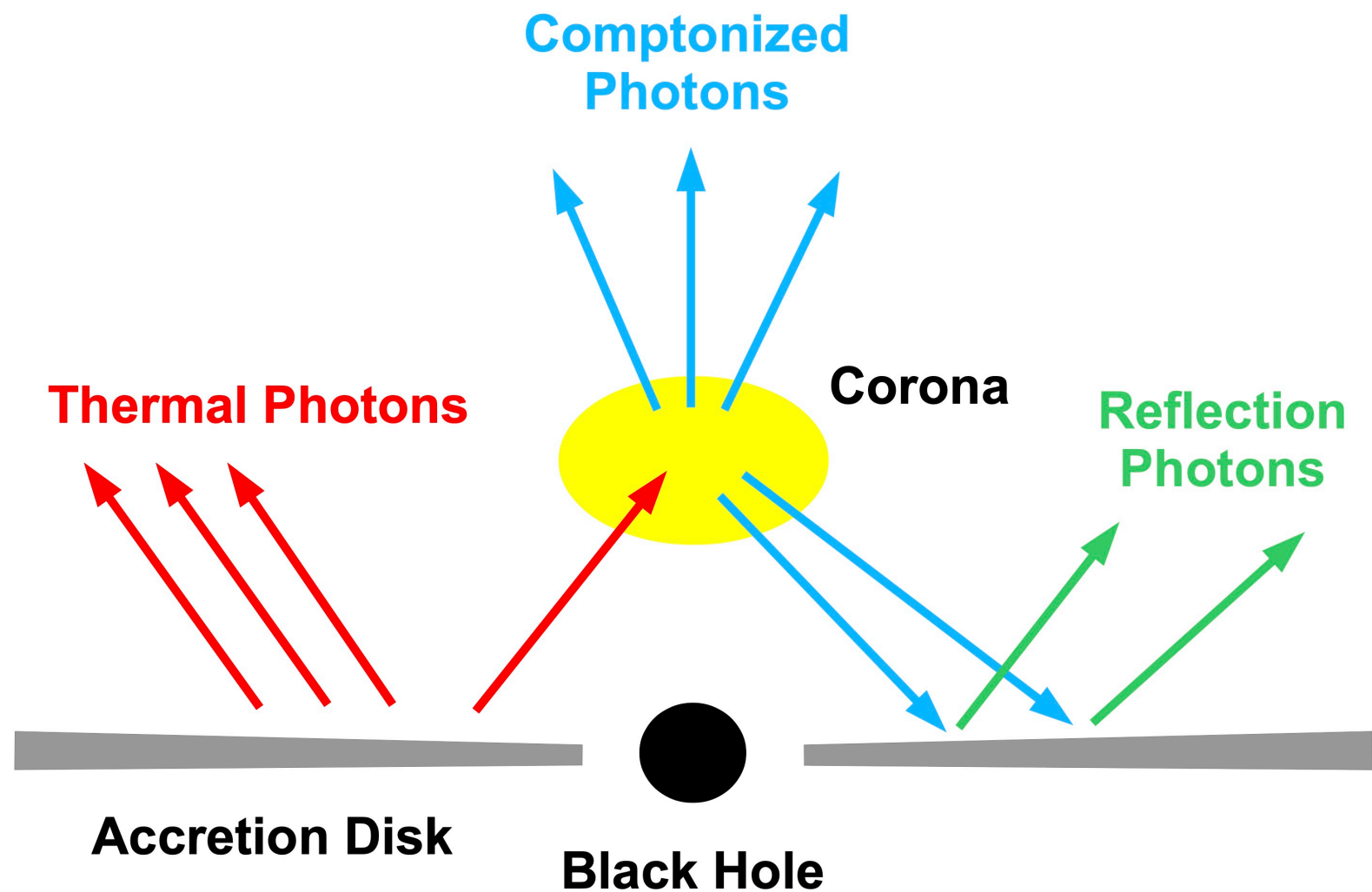
Cosimo Bambi
Fudan University



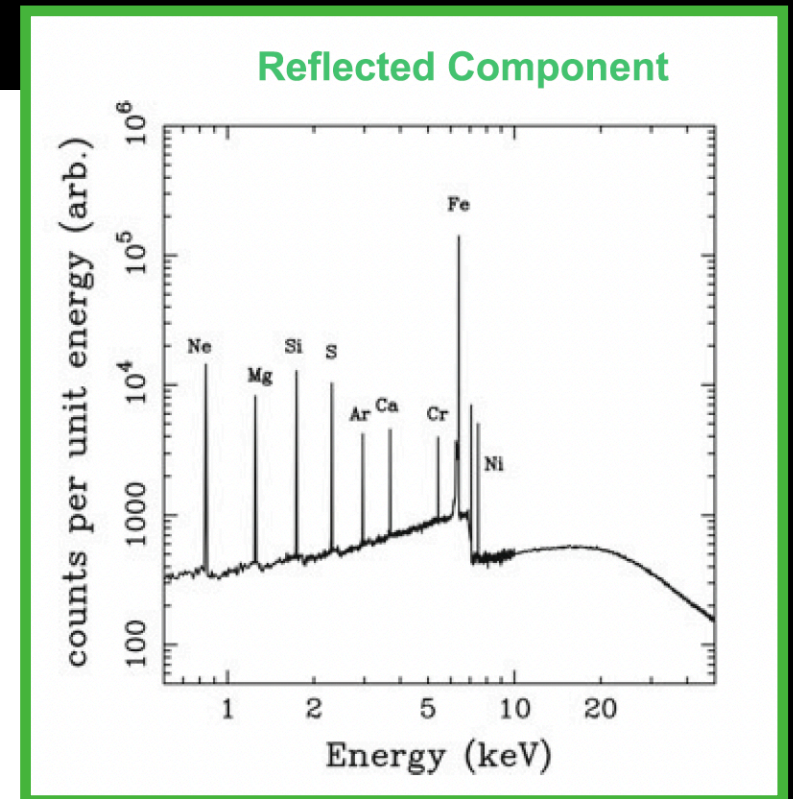
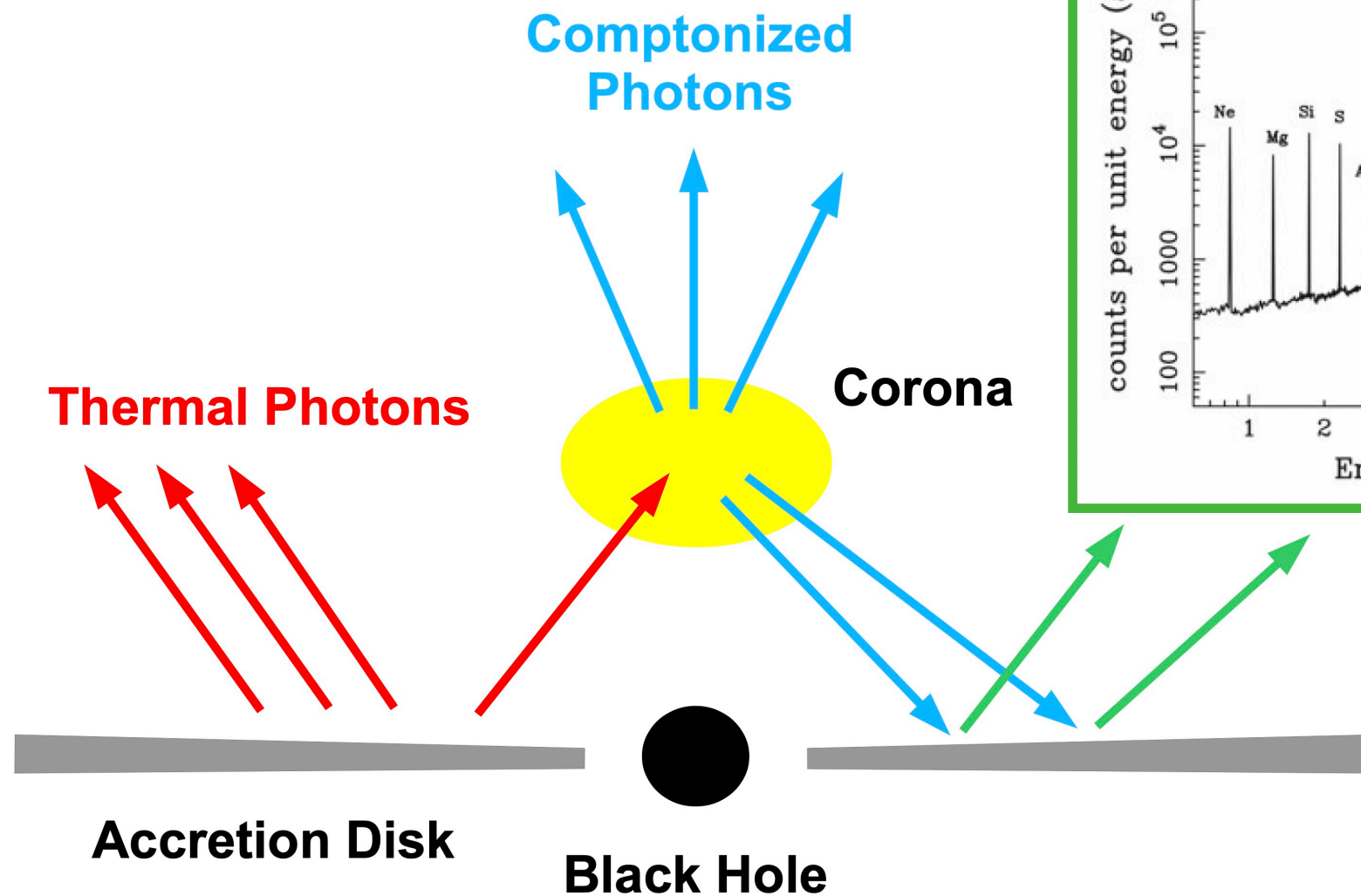
32nd Texas Symposium on Relativistic Astrophysics
Shanghai (11-15 December 2023)



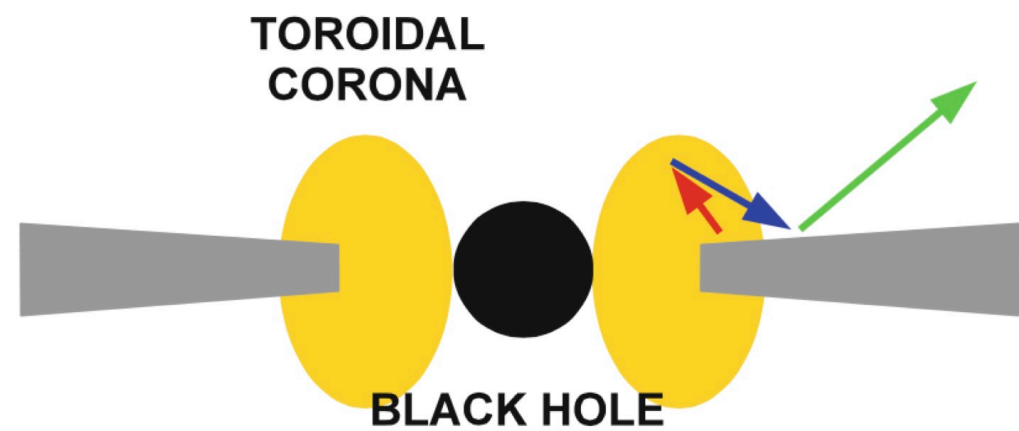
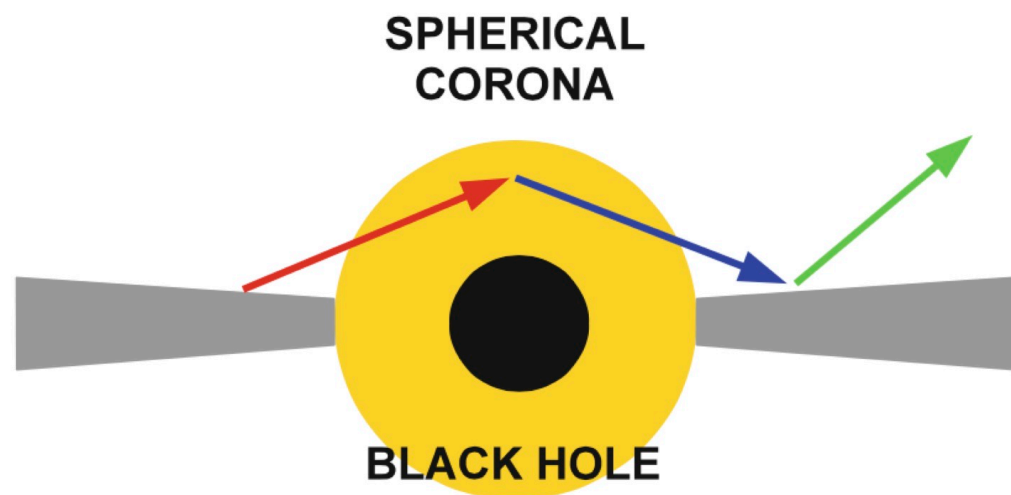
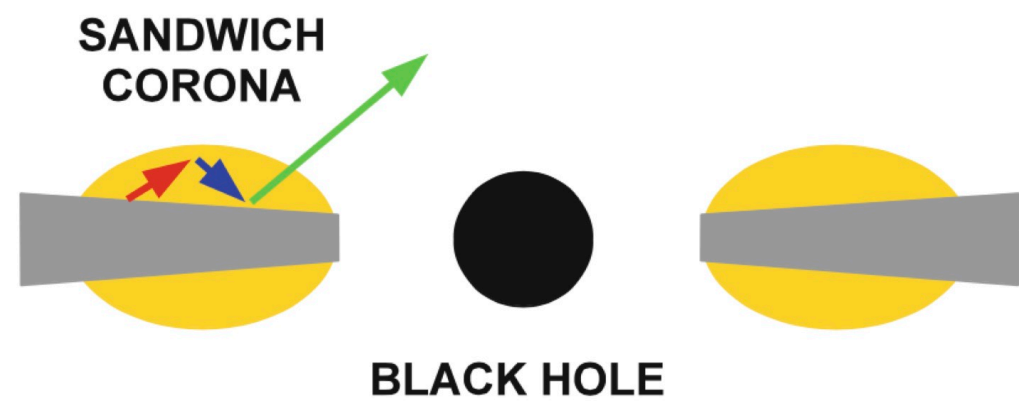
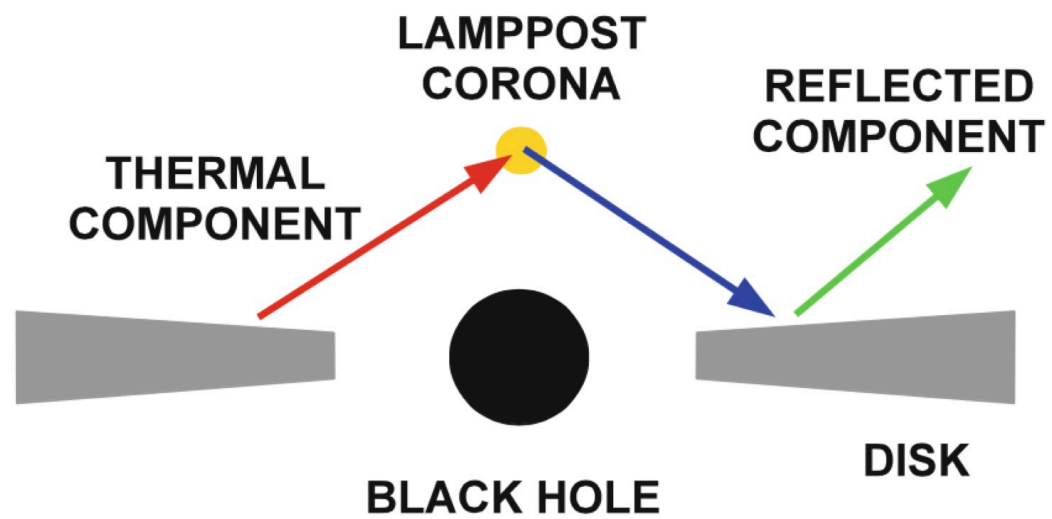
Disk-Corona Model



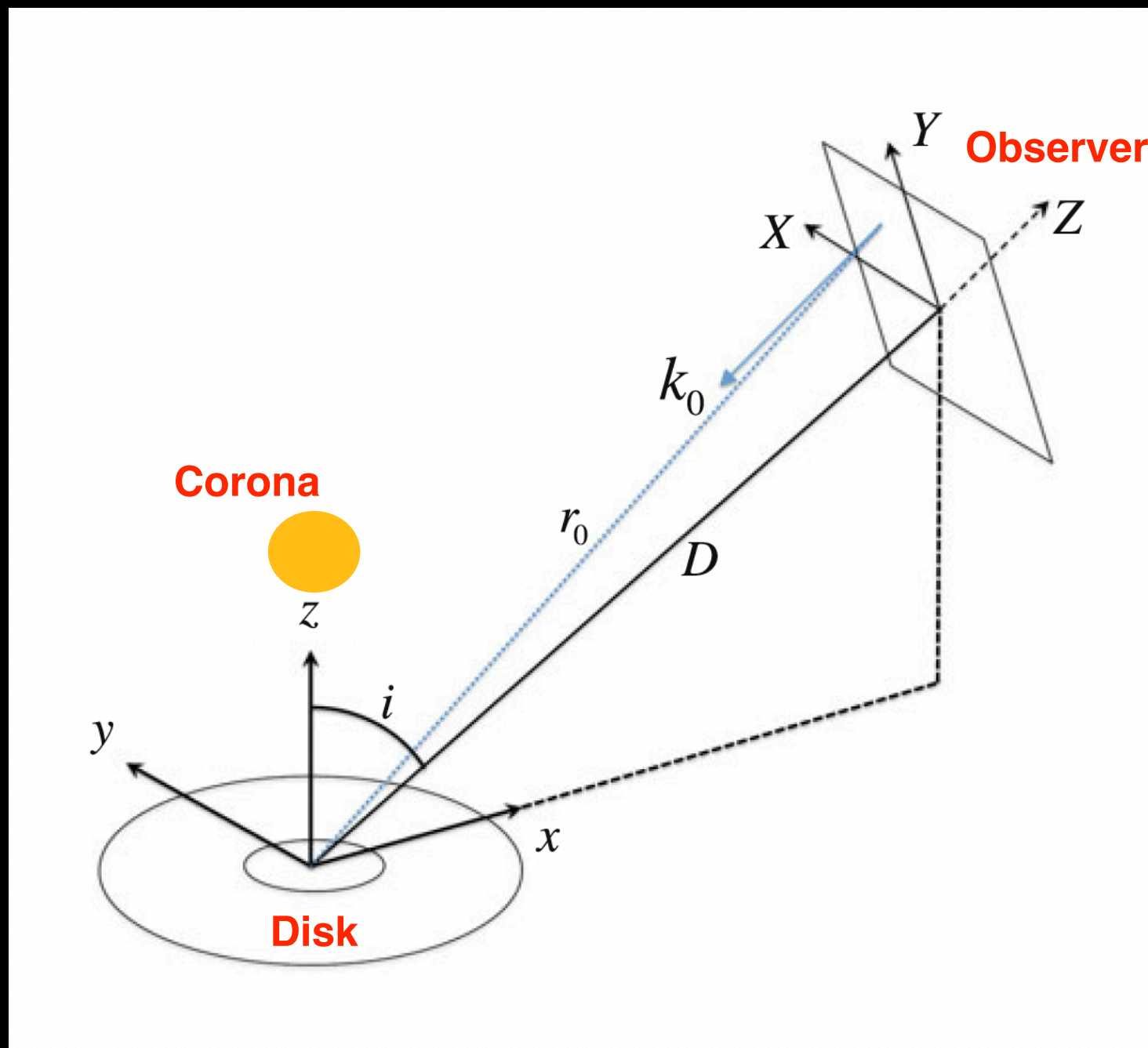
Disk-Corona Model



Coronal Geometries



Disk-Observer System



Redshift Image of the Disk

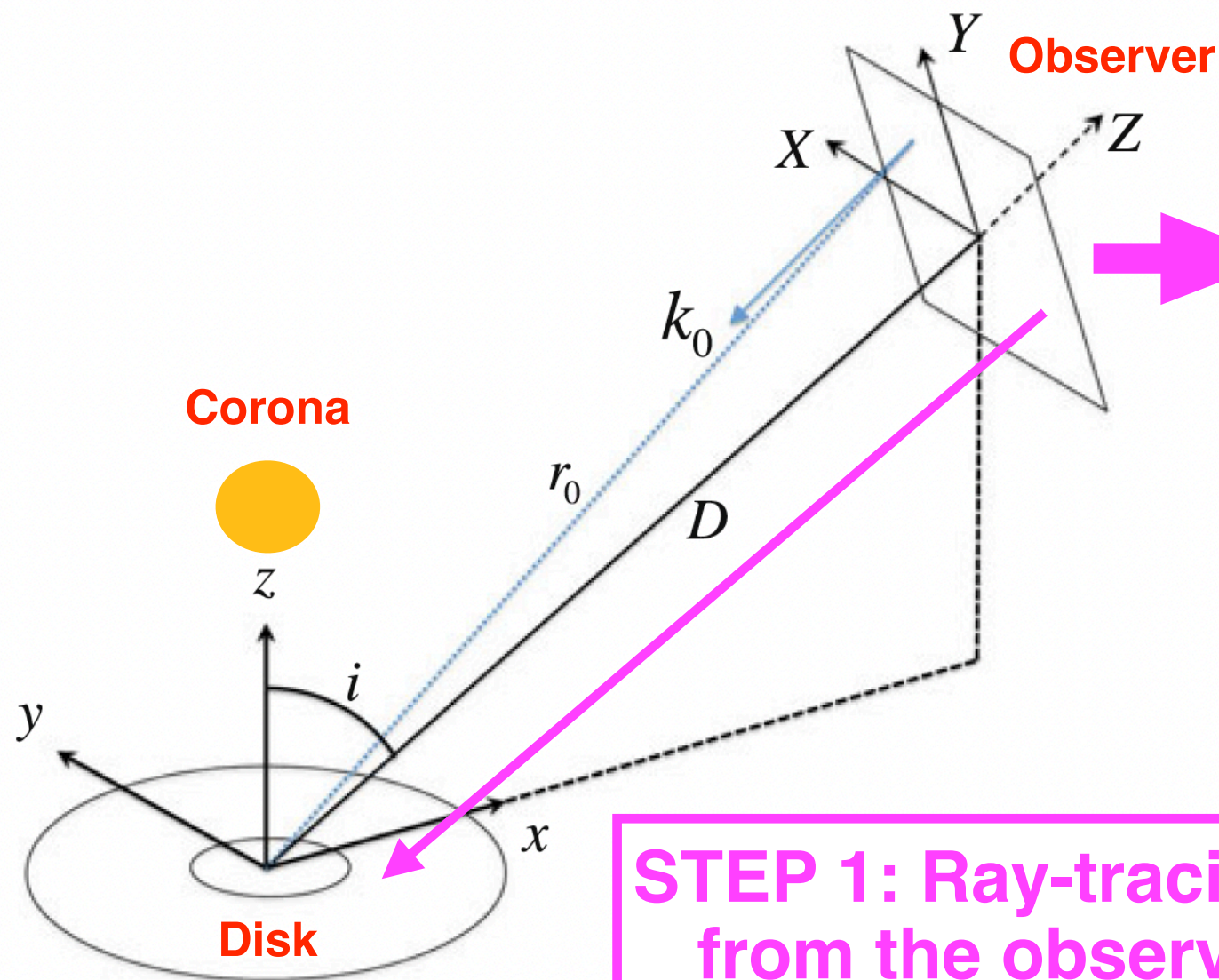
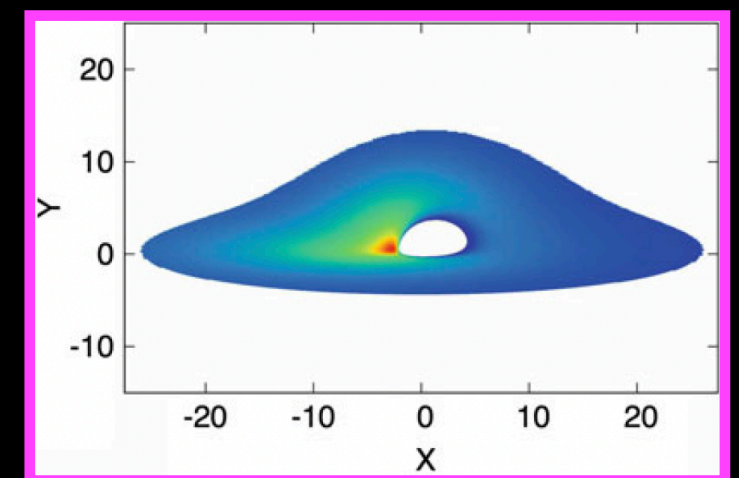


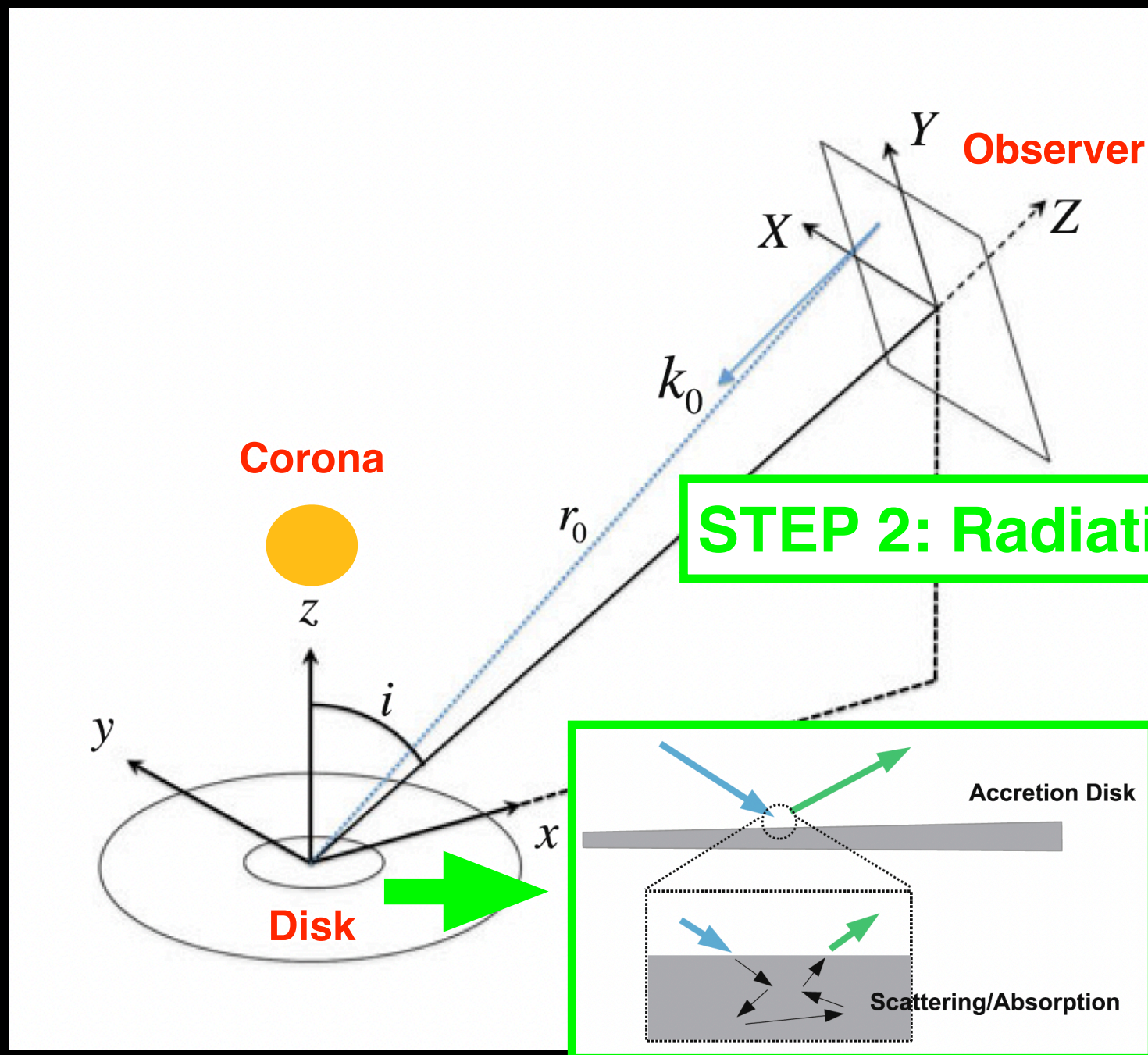
Image of the accretion disk



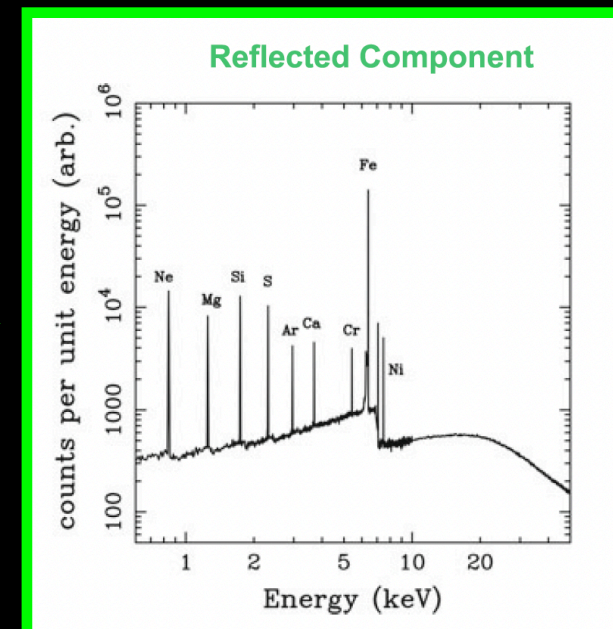
Every point on the image is characterized by its redshift factor g

STEP 1: Ray-tracing calculations from the observer to the disk

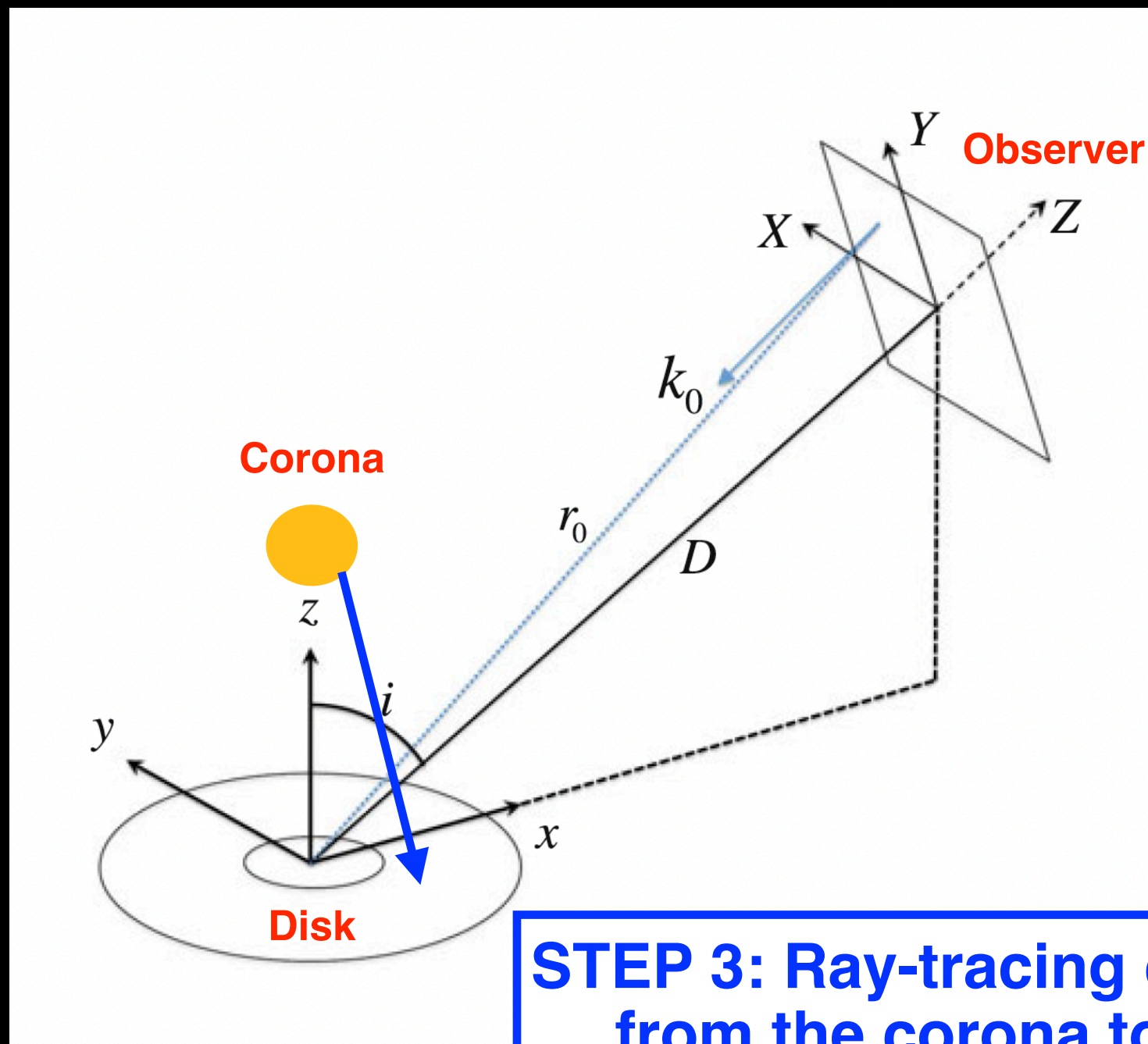
Local Spectrum



STEP 2: Radiative transfer equations



Emissivity Profile of the Disk




**STEP 3: Ray-tracing calculations
from the corona to the disk**

Transfer Function

$$F_{\text{obs}}(\nu_{\text{obs}}) = \int I_{\text{obs}}(\nu_{\text{obs}}, X, Y) d\tilde{\Omega} = \int g^3 I_{\text{e}}(\nu_{\text{e}}, r_{\text{e}}, \vartheta_{\text{e}}) d\tilde{\Omega} ,$$



$$F_{\text{obs}}(\nu_{\text{obs}}) = \frac{1}{D^2} \int_{r_{\text{ISCO}}}^{\infty} \int_0^1 \pi r_{\text{e}} \frac{g^2}{\sqrt{g^*(1-g^*)}} f(g^*, r_{\text{e}}, i) I_{\text{e}}(\nu_{\text{e}}, r_{\text{e}}, \vartheta_{\text{e}}) dg^* dr_{\text{e}} .$$

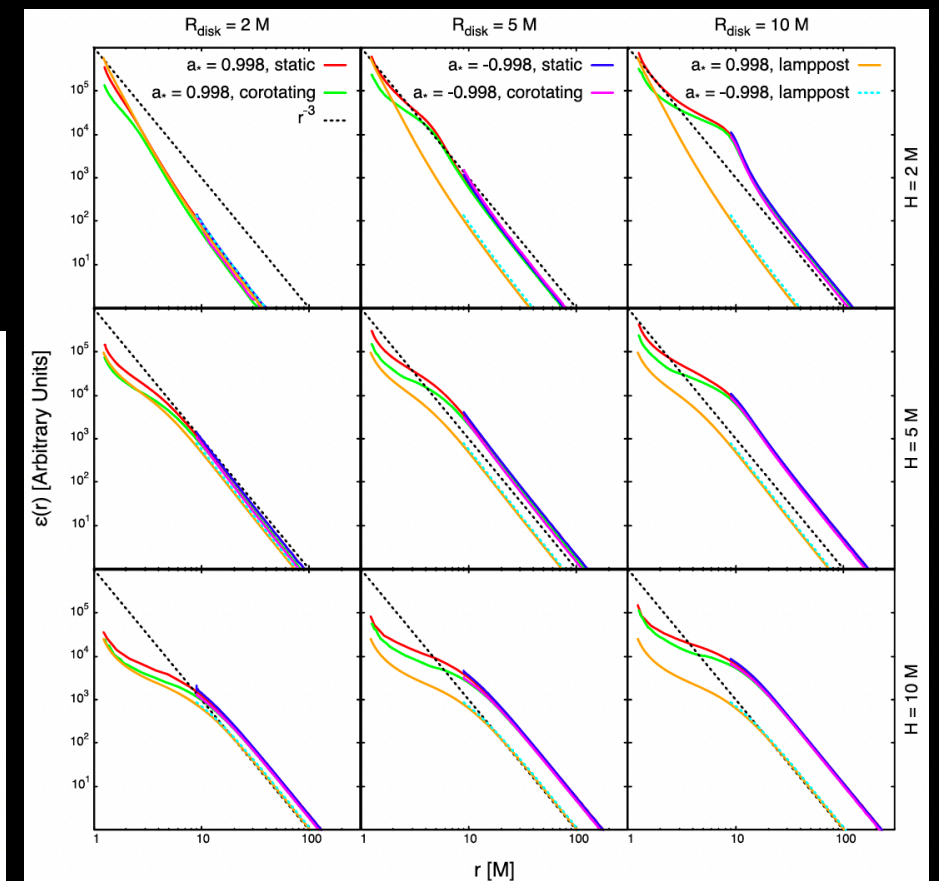
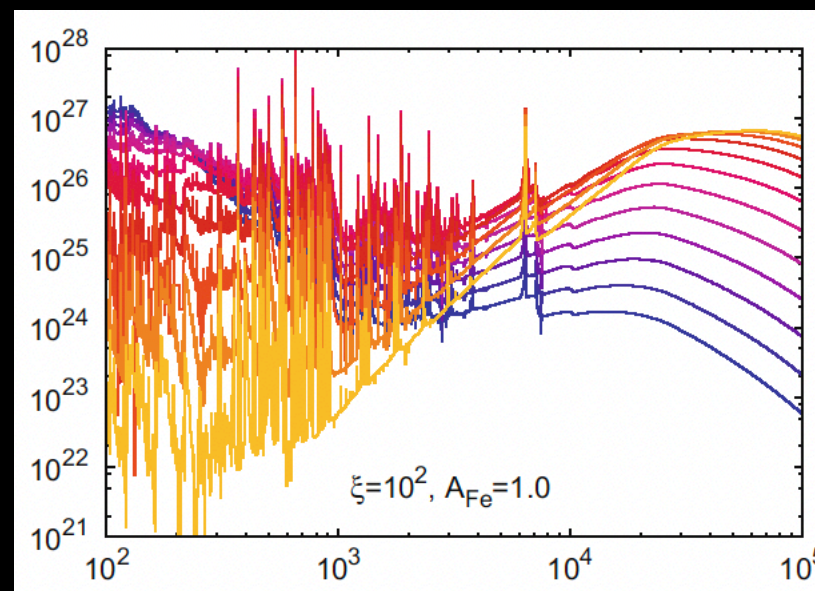
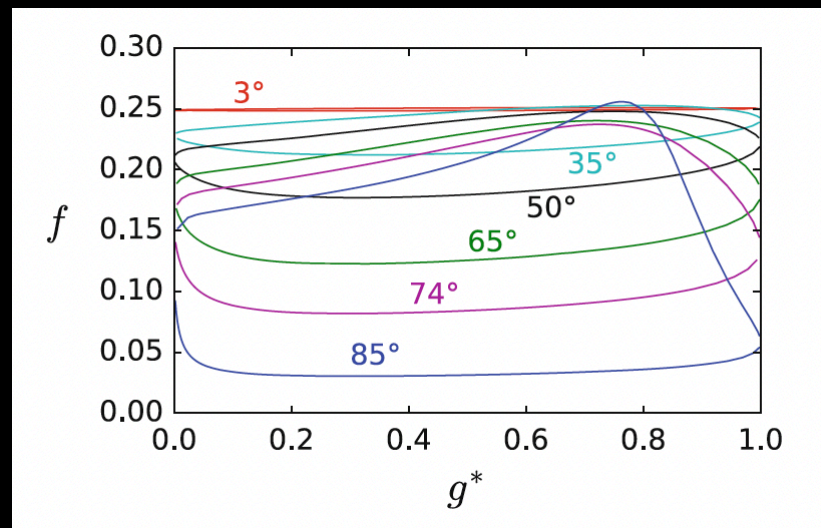

$$g^* = \frac{g - g_{\text{min}}}{g_{\text{max}} - g_{\text{min}}} ,$$



$$f(g^*, r_{\text{e}}, i) = \frac{1}{\pi r_{\text{e}}} g \sqrt{g^*(1-g^*)} \left| \frac{\partial (X, Y)}{\partial (g^*, r_{\text{e}})} \right| ,$$

FITS Files

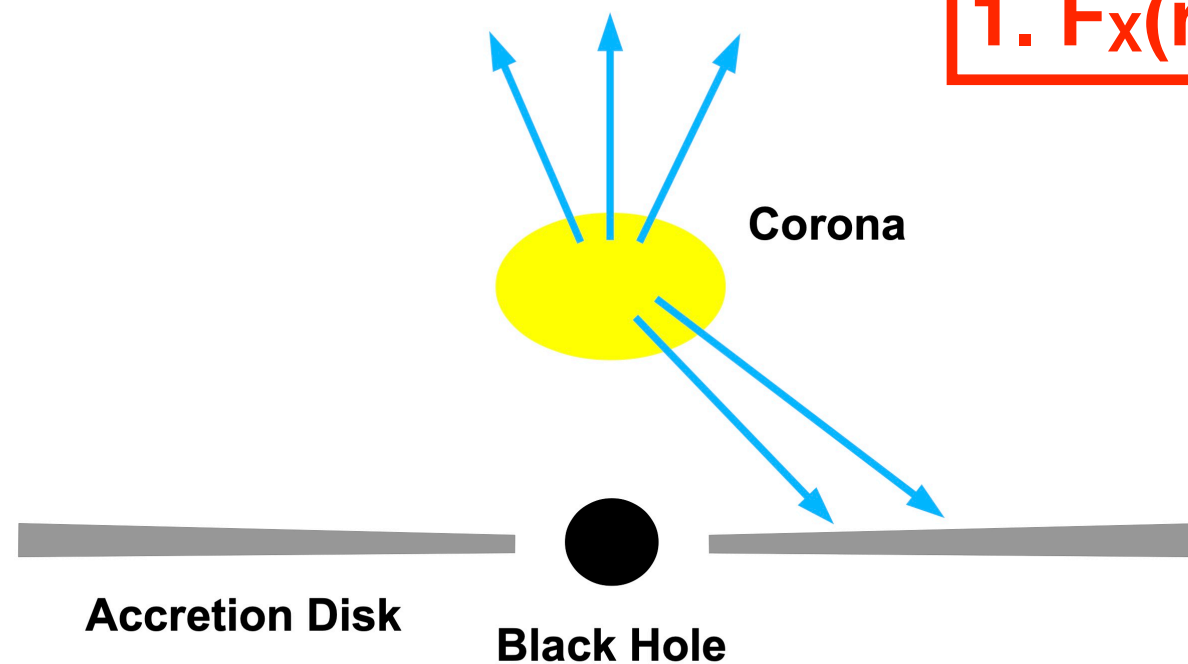
$$F_{\text{obs}}(\nu_{\text{obs}}) = \frac{1}{D^2} \int_{r_{\text{ISCO}}}^{\infty} \int_0^1 \frac{\pi r_e g^2}{\sqrt{g^*(1-g^*)}} f_1(g^*, r_e, i) I_e(\nu_e, r_e, \vartheta_{e,1}) dg^* dr_e \\ + \frac{1}{D^2} \int_{r_{\text{ISCO}}}^{\infty} \int_0^1 \frac{\pi r_e g^2}{\sqrt{g^*(1-g^*)}} f_2(g^*, r_e, i) I_e(\nu_e, r_e, \vartheta_{e,2}) dg^* dr_e ,$$



How Can We Improve Current Reflection Models?

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- 1) Spacetime (Kerr: M, a)
- 2) Disk (n)
- 3) Corona (lamppost: h, Γ, T)

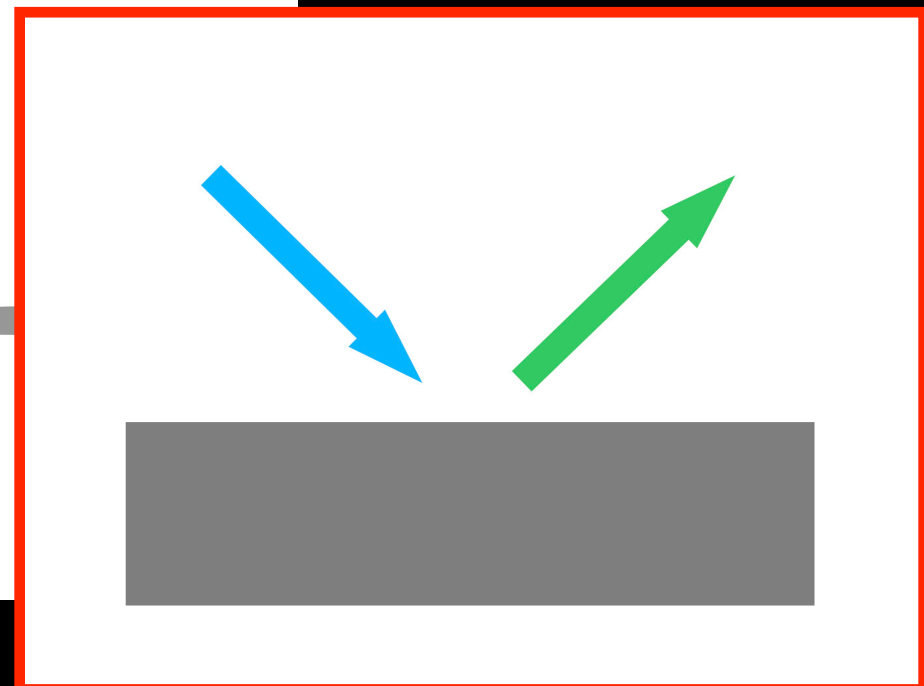
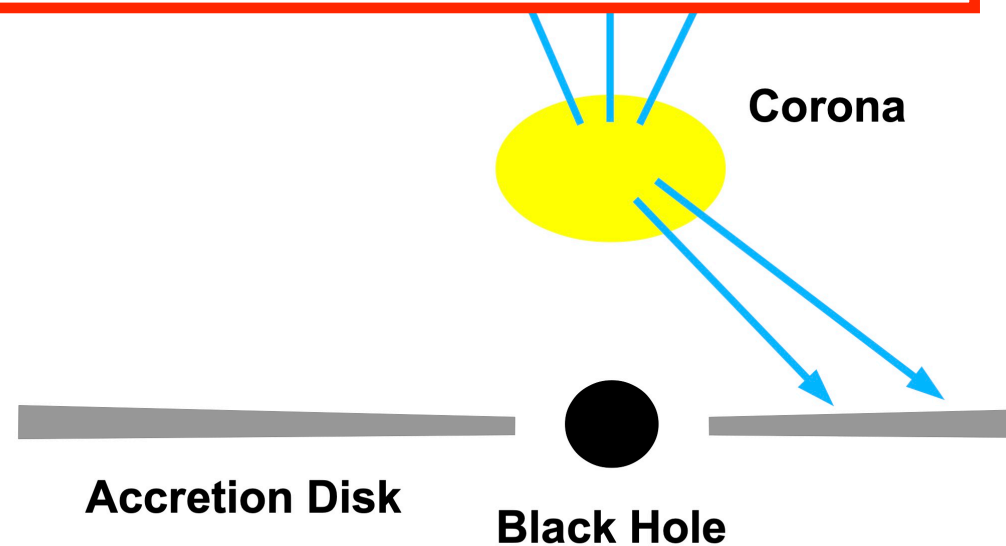


1. $F_x(r)$ from the corona

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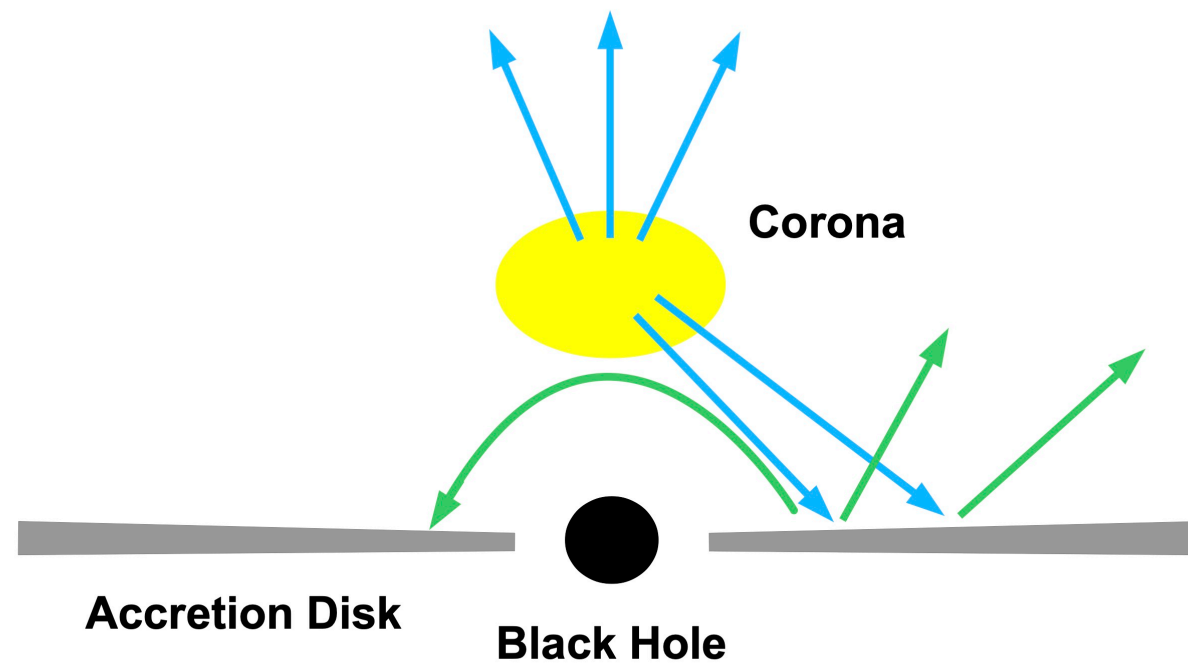
- 1) Spacetime (Kerr: M, a)
- 2) Disk (n)
- 3) Corona (lamppost: h, Γ, T)

2. Reflection spectrum $I_e(r)$
Note: $\xi(r)$, redshifted coronal spectrum



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3. Returning radiation at every radius

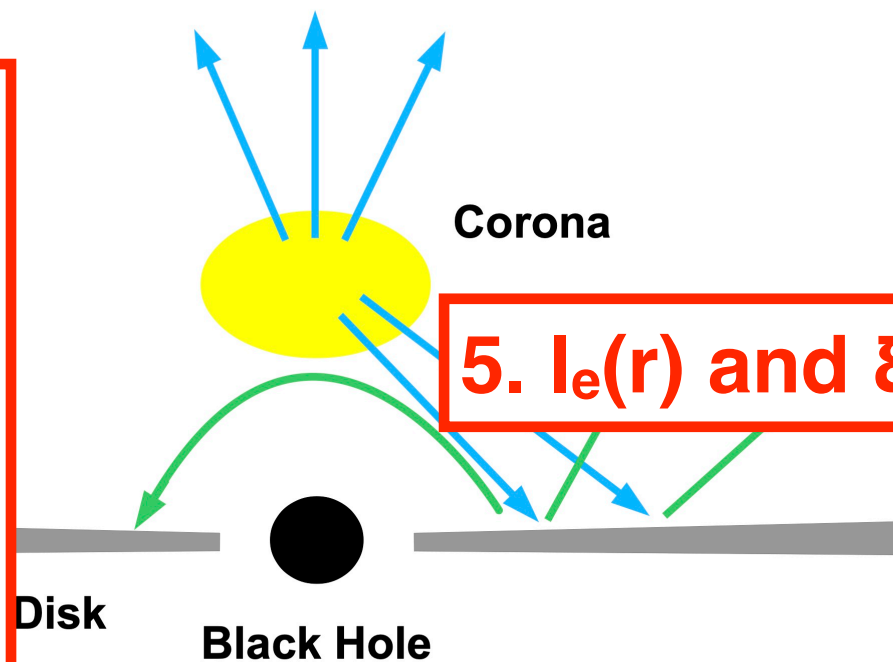
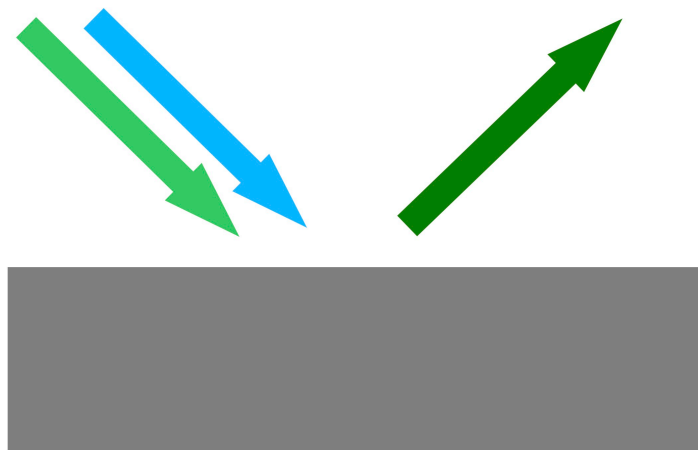


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3. Returning radiation at every radius

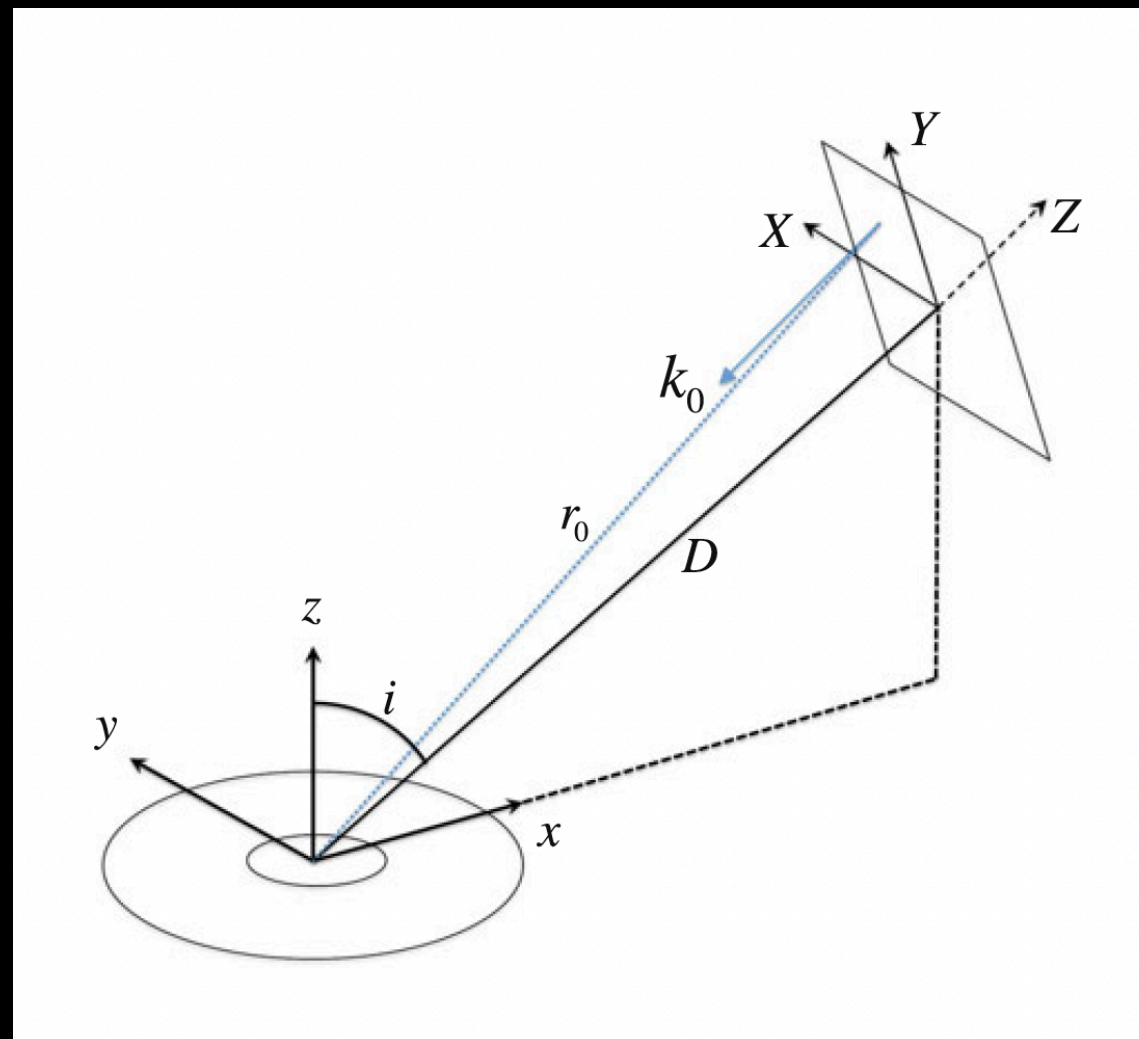
4. New $I_e(r)$ and $\xi(r)$

5. $I_e(r)$ and $\xi(r)$ at the 4th order



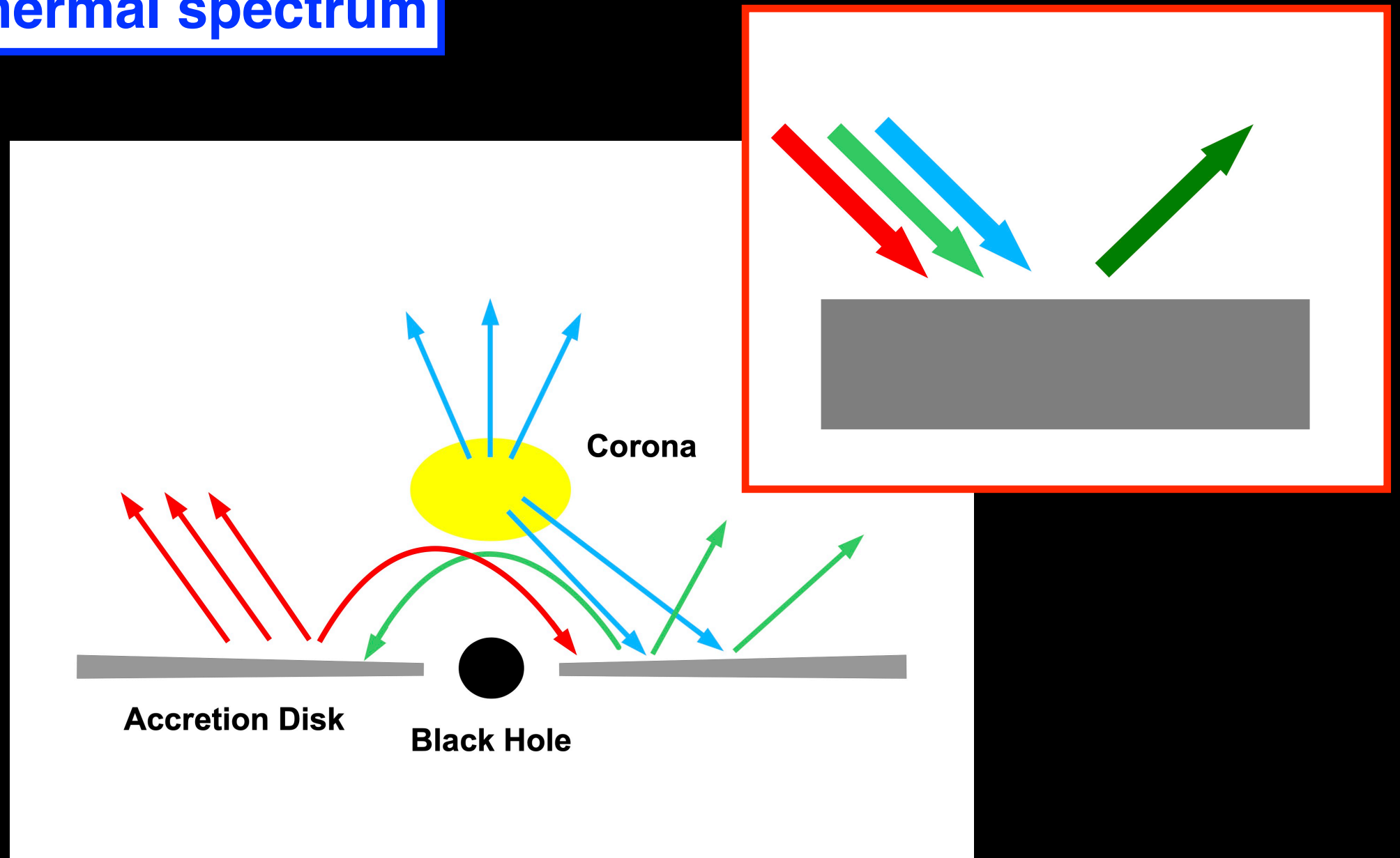
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6. Observed reflection spectrum (viewing angle i)



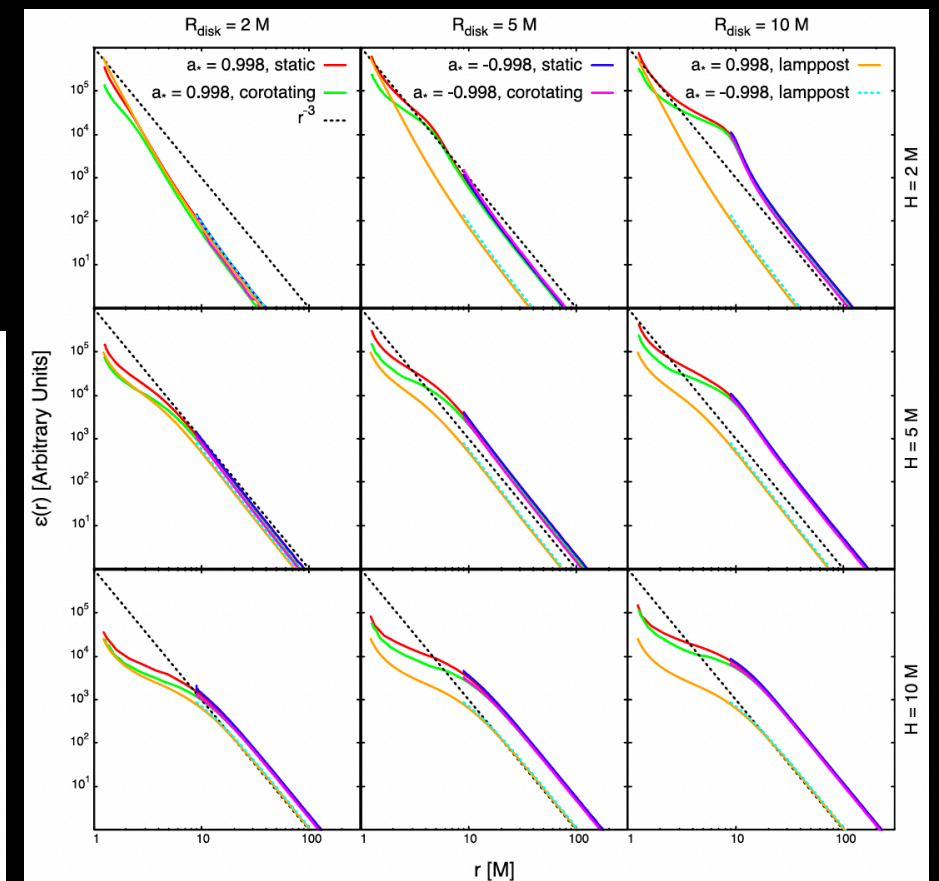
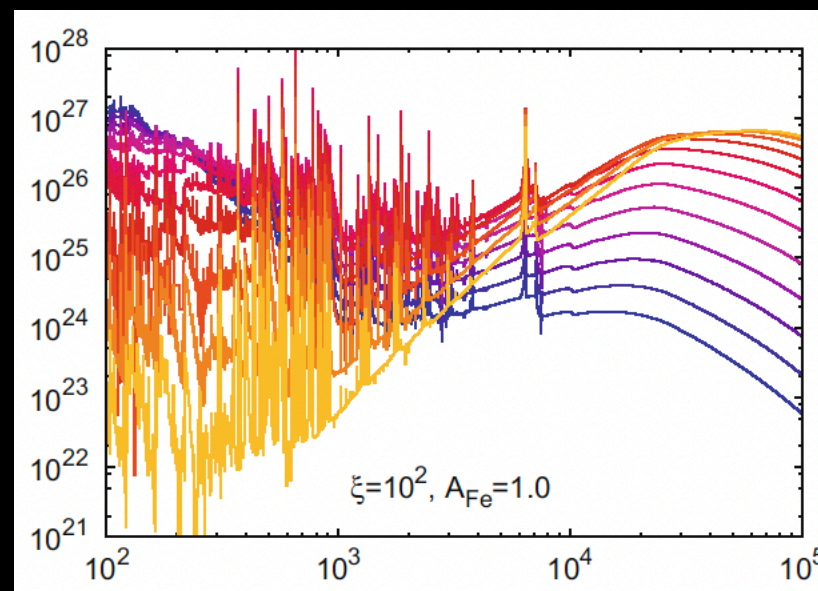
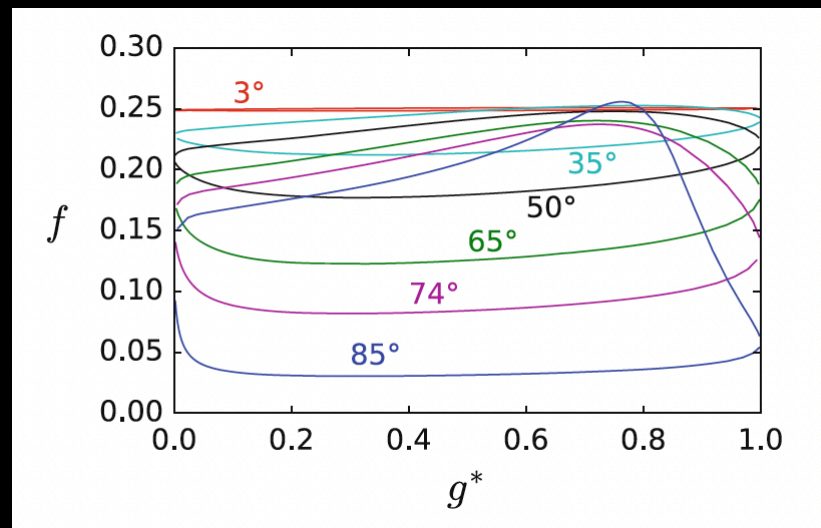
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7. Thermal spectrum



Current Reflection Models for Data Analysis

$$F_{\text{obs}}(\nu_{\text{obs}}) = \frac{1}{D^2} \int_{r_{\text{ISCO}}}^{\infty} \int_0^1 \frac{\pi r_e g^2}{\sqrt{g^*(1-g^*)}} f_1(g^*, r_e, i) I_e(\nu_e, r_e, \vartheta_{e,1}) dg^* dr_e \\ + \frac{1}{D^2} \int_{r_{\text{ISCO}}}^{\infty} \int_0^1 \frac{\pi r_e g^2}{\sqrt{g^*(1-g^*)}} f_2(g^*, r_e, i) I_e(\nu_e, r_e, \vartheta_{e,2}) dg^* dr_e ,$$



Conclusions

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- The analysis of observations from the next generation of X-ray missions (eXTP, Athena, HEX-P, etc.) will necessarily require more sophisticated synthetic spectra than those available today
- New generation of reflection models (neural networks?)

Thank You!