



上海交通大学
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SJTUPA

上海交通大学物理与天文学院

Seeking Lensing Effects from Counting Galaxies

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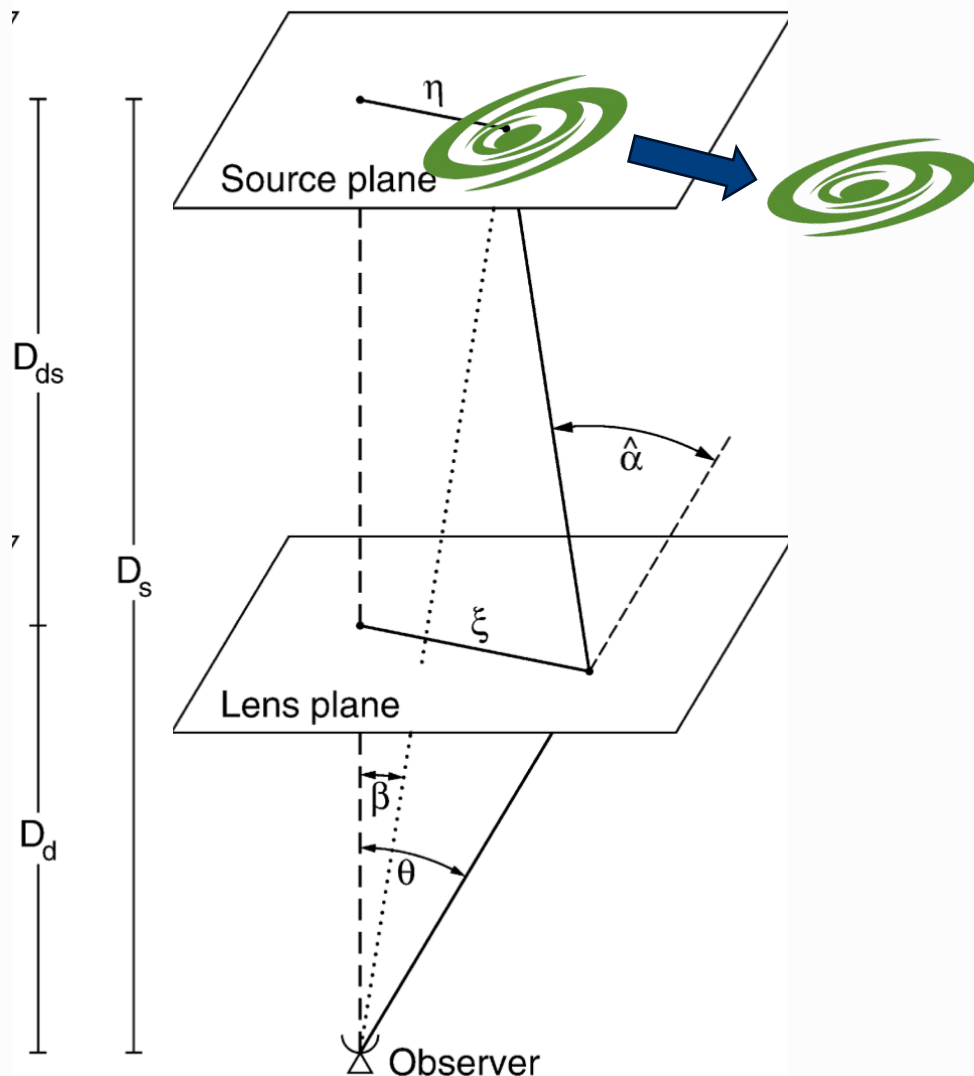
2023-12-15



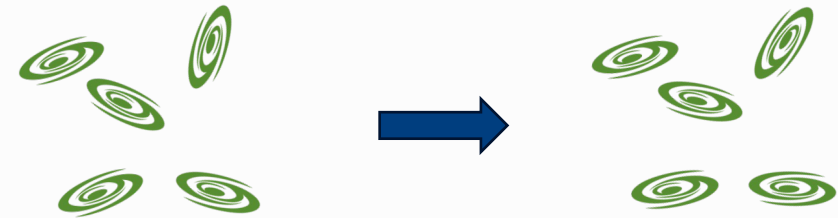
Content

- Cosmic shear & magnification
- Modified internal linear combination method
- Optimal Weighting method
- Application of MILC on observation
- Summary

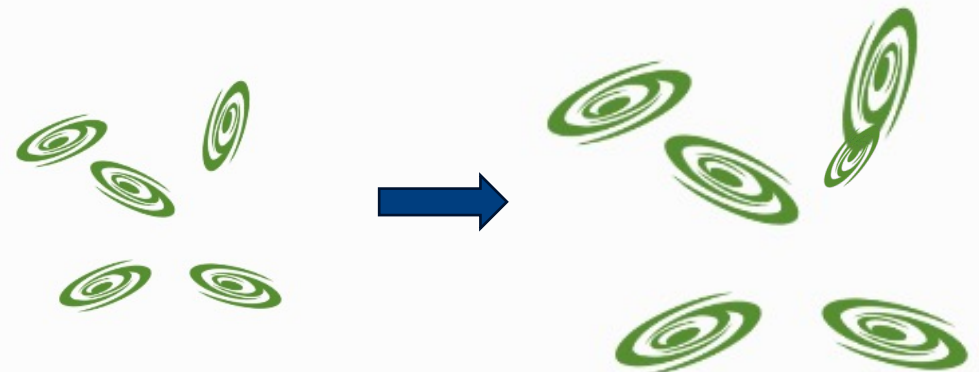
cosmic shear & cosmic magnification



coherent change in galaxy shape: cosmic shear



(de)magnify the galaxy image/sky area: cosmic magnification



Cosmic Shear v.s. Cosmic Magnification

$$e^L = e_{\text{IA}} + \underline{\gamma} + e^S$$

- intrinsic alignment
- cosmic shear
- shape noise

$$\delta^L = \delta_g + \underline{g\kappa} + \delta^S$$

- intrinsic clustering
- cosmic magnification
- shot noise

$$g = 2(a - 1), \quad a = -\frac{d \ln n(F)}{d \ln F} - 1$$

observable

observable

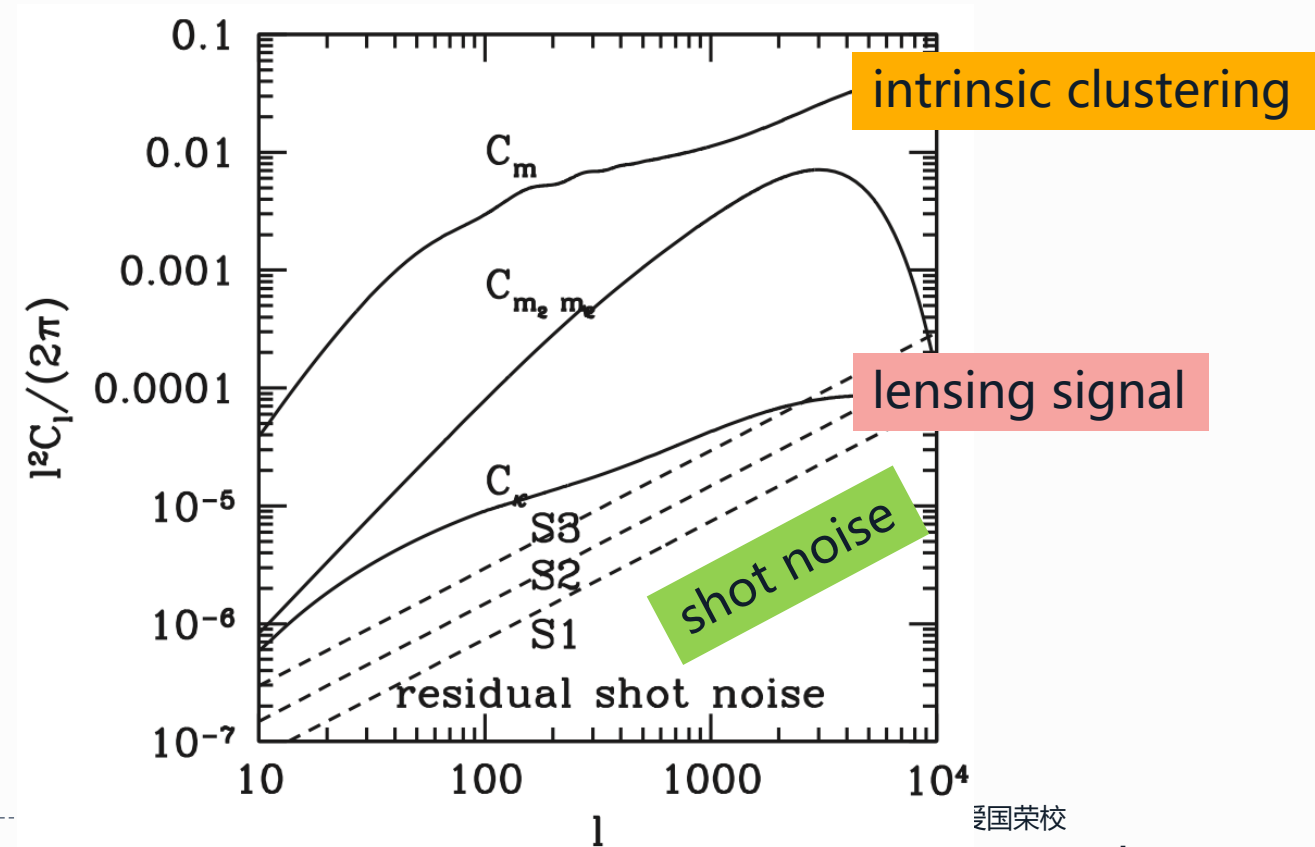
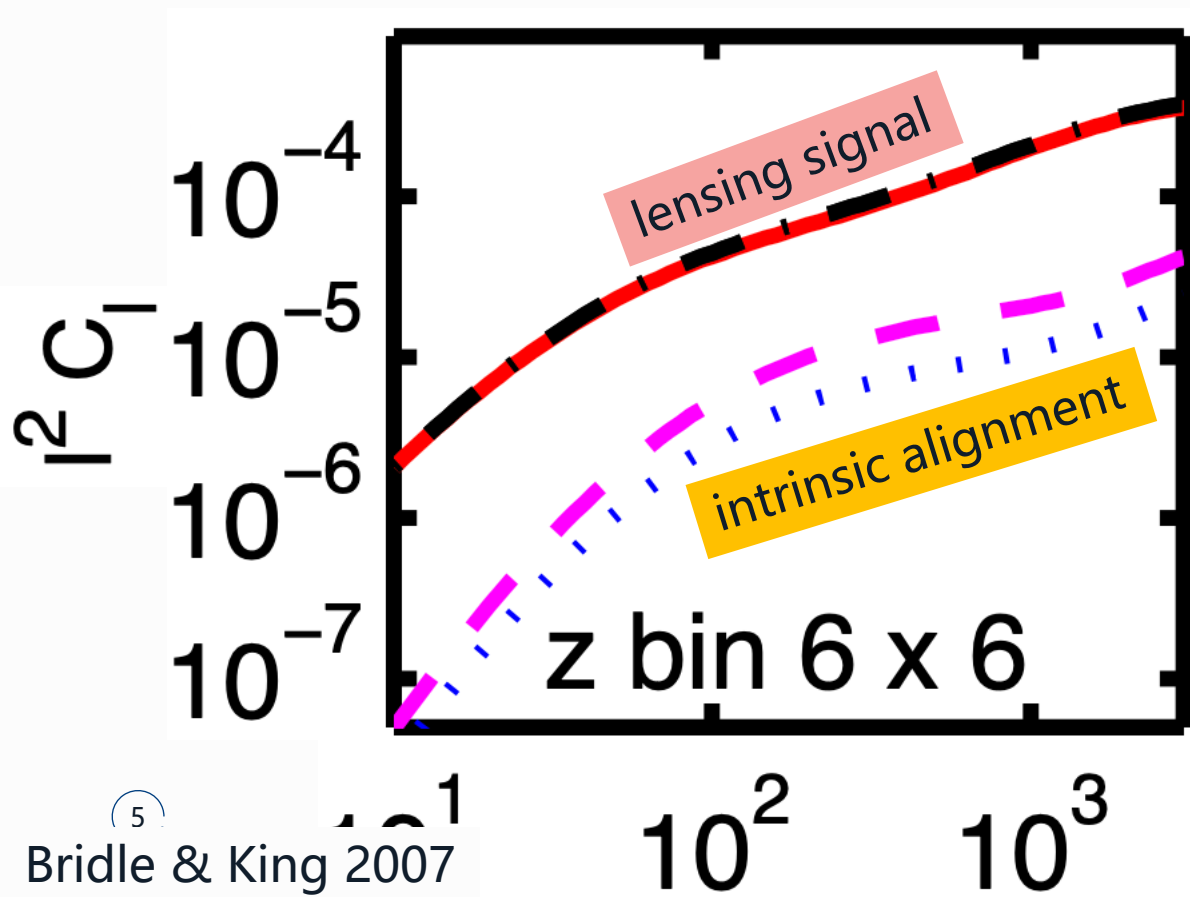
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Cosmic Shear v.s. Cosmic Magnification

Much more challenge !

$$e^L = e_{\text{IA}} + \gamma + e^S$$

$$\delta^L = \delta_g + g\kappa + \delta^S$$



Magnification History

- Cross correlate two Gal/QSO samples far from each other:

SDSS QSO X SDSS LRG, [Scranton et al. 2005](#)

CFHTLS X LBG $2.5 < z < 5$, [Hildebrandt et al. 2009, 2013](#)

SDSS X HerMES submillimetre galaxies, $z \sim 2$, [Wang et al. 2011](#); [González-Nuevo et al. 2014](#); [Bonavera et al. 2021](#); [González-Nuevo et al. 2021](#)

DES SV X DES SV [Garcia-Fernandez et al. 2018](#)

$\langle \delta_f \delta_b \rangle \rightarrow \langle \delta_f \kappa_b \rangle$, suffer from galaxy bias

- HSC cosmic shear $\rightarrow$ convergence X HSC galaxy [Liu et al. 2021](#)

$\langle \kappa_f \delta_b \rangle \rightarrow \langle \kappa_f \kappa_b \rangle$, free from galaxy bias

Indirect measurement
No magnification map

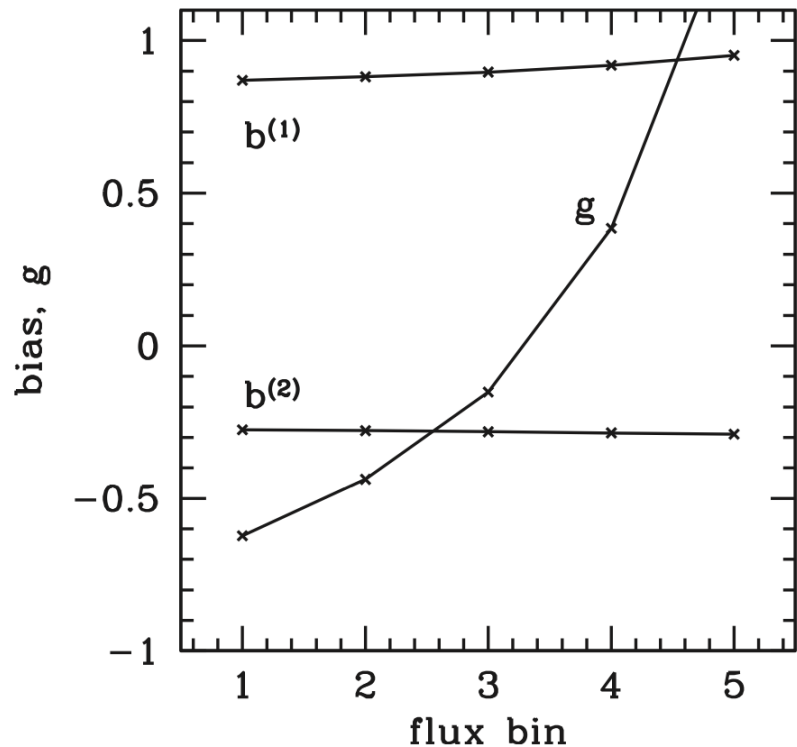
Magnification History

- Separate the lensing signal using the known dependence on the prefactor g

$$\delta^L = b\delta_m + g\kappa + \delta^S$$

$$g = 2(a - 1), \quad a = -\frac{d \ln n(F)}{d \ln F} - 1$$

observable



Proposed in [Zhang & Pen 2005](#)

Analytically validated in [Yang & Zhang \(2011\)](#); [Yang et al. \(2015\)](#)

Analytic Blind Separation [Yang et al. 2017](#); [Zhang et al. 2018](#)

...

We want a
magnification map!

Content

arXiv: 2106.09970
Shutong HOU +



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Cosmic Magnification v.s. CMB observation

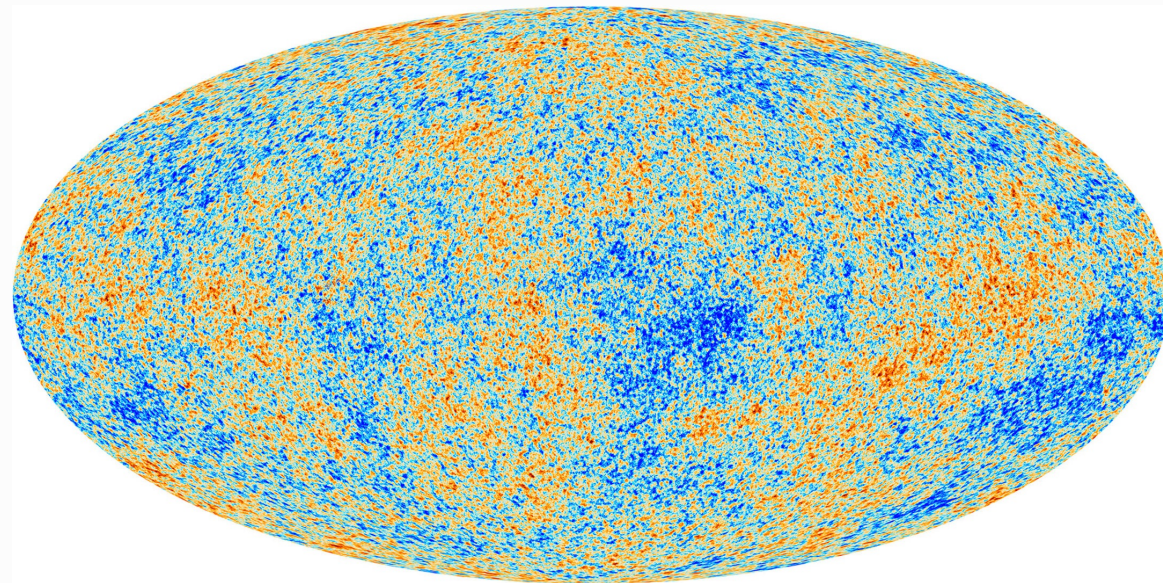
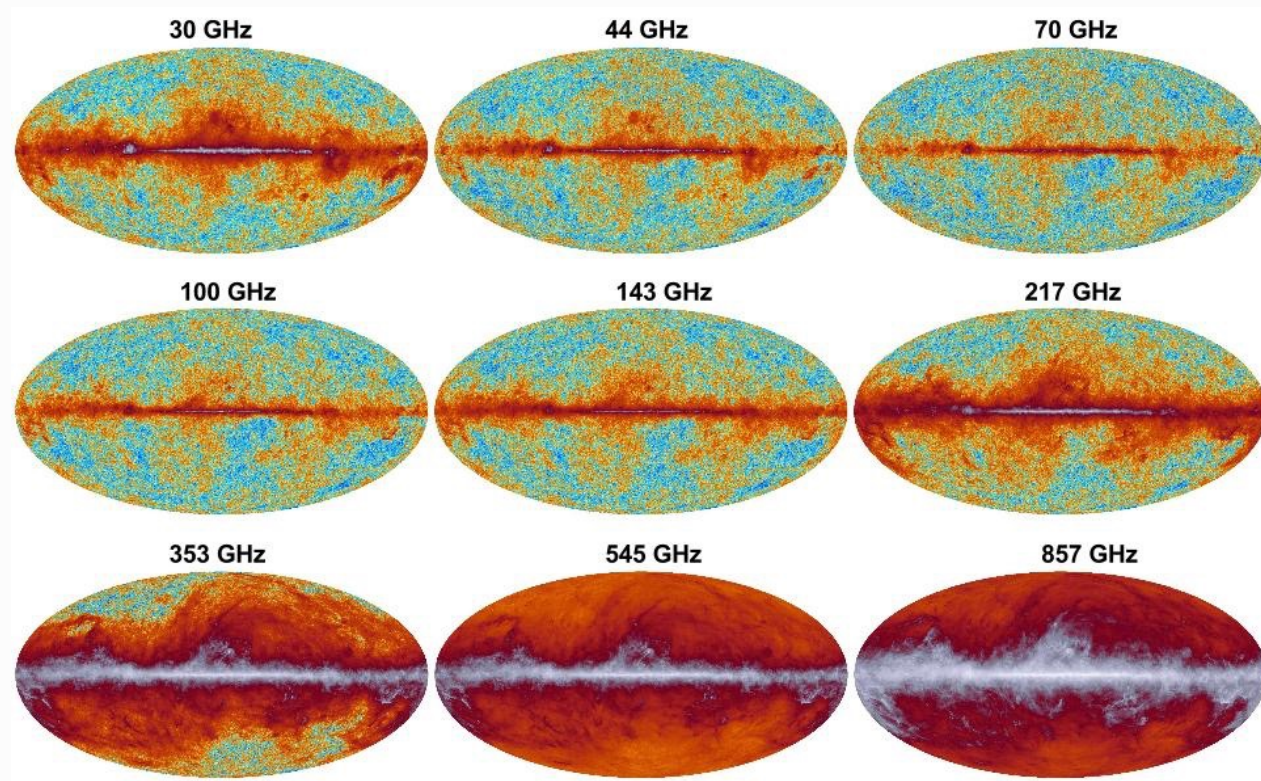
$$\delta^L = \delta_g + \underline{g\kappa} + \delta^S$$

- intrinsic clustering
- cosmic magnification
known dependence on g
- shot noise

$$T^{\text{obs}} = T_{\text{fore}} + \underline{T_{\text{CMB}}} + T_{\text{noise}}$$

- foreground contamination
- CMB
known dependence on frequency
- instrument noise

foreground removal in CMB



- template fitting
- internal linear combination (ILC)
- ...

Cosmic Magnification: Modified ILC

$$\delta^L = \delta_g + g\kappa + \delta^S$$

Modified internal linear combination

If g_i is known, we can construct an estimator

$$\hat{\kappa} = \sum_i w_i \delta_i^L = \sum_i w_i \delta_{g,i} + \kappa \sum_i w_i g_i + \sum_i w_i \delta_i^S$$

$$\delta_1^L = \delta_{g,1} + g_1 \kappa + \delta_1^S$$

$$\delta_2^L = \delta_{g,2} + g_2 \kappa + \delta_2^S$$

$\vdots$

$$\delta_n^L = \delta_{g,n} + g_n \kappa + \delta_n^S$$

$$\left\{ \begin{array}{l} \sum_i w_i = 0 \\ \sum_i w_i g_i = 1 \\ \left\langle \left(\sum_i w_i \delta_i^L \right)^2 \right\rangle \\ \text{minimized} \end{array} \right.$$

→ suppress the intrinsic clustering

→ unbiased estimator

→ minimize the noise

Divide into subsamples according to some galaxy property

Cosmic Magnification: Modified ILC

If g_i is known, we can construct an estimator

$$\hat{\kappa} = \sum_i w_i \delta_i^L = \sum_i w_i \delta_{g,i} + \kappa \sum_i w_i g_i + \sum_i w_i \delta_i^S$$

$$\left\{ \begin{array}{l} \sum_i w_i = 0 \\ \sum_i w_i g_i = 1 \\ \left\langle \left(\sum_i w_i \delta_i^L \right)^2 \right\rangle \\ \text{minimized} \end{array} \right.$$

→ suppress the
intrinsic clustering

→ unbiased estimator

→ minimize the noise

$$\sum_i w_i \delta_{g,i} \neq 0 \rightarrow \text{additive bias}$$

$$\sum_i w_i g_i \neq 1 \rightarrow \text{multiplicative bias}$$

→ statistical uncertainty

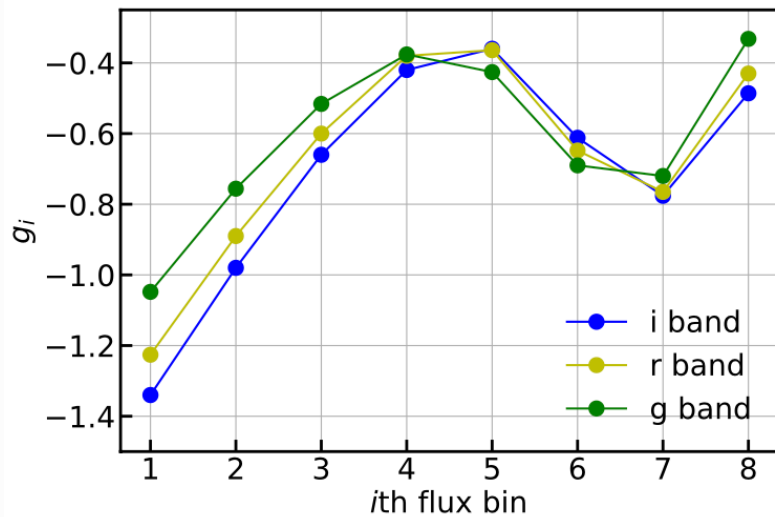
Numerical Validation

We use FASTPM to generate 200 halo catalogue at $z=1$, each spanning $10 \times 10 \text{ deg}^2$.

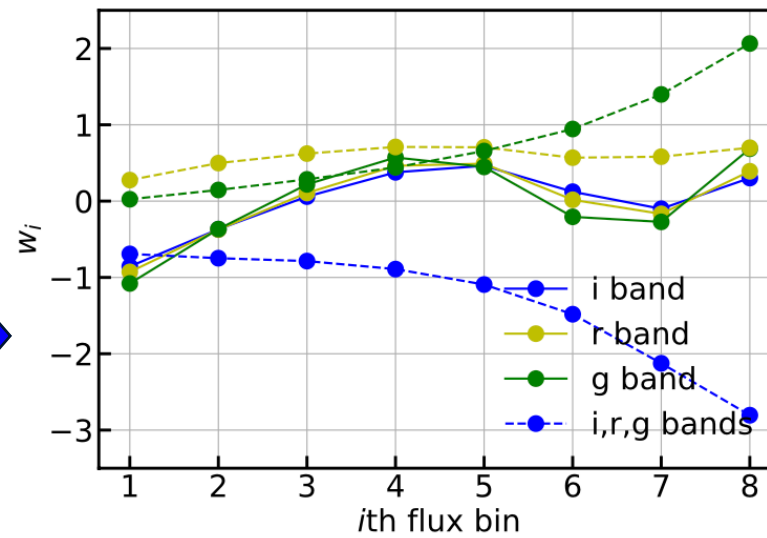
For each halo we randomly pick galaxies with same halo mass from CosmoDC2 catalogue.

We generate Gaussian lensing fields according to nonlinear lensing power spectrum at $z=1$.

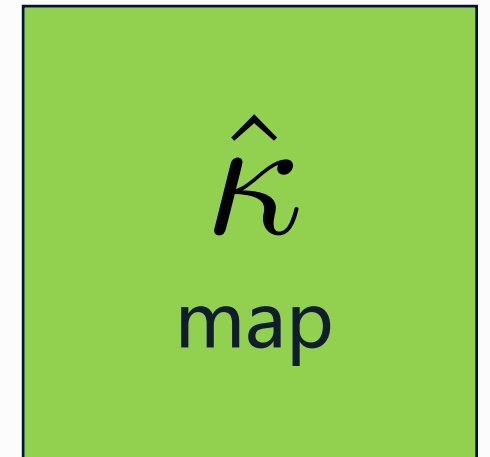
Lensed galaxy catalogue with r, i, g band photometry, $n \sim 12 \text{ arcmin}^{-2}$ for $0.8 < z^p < 1.2$.



measure lensing prefactor g



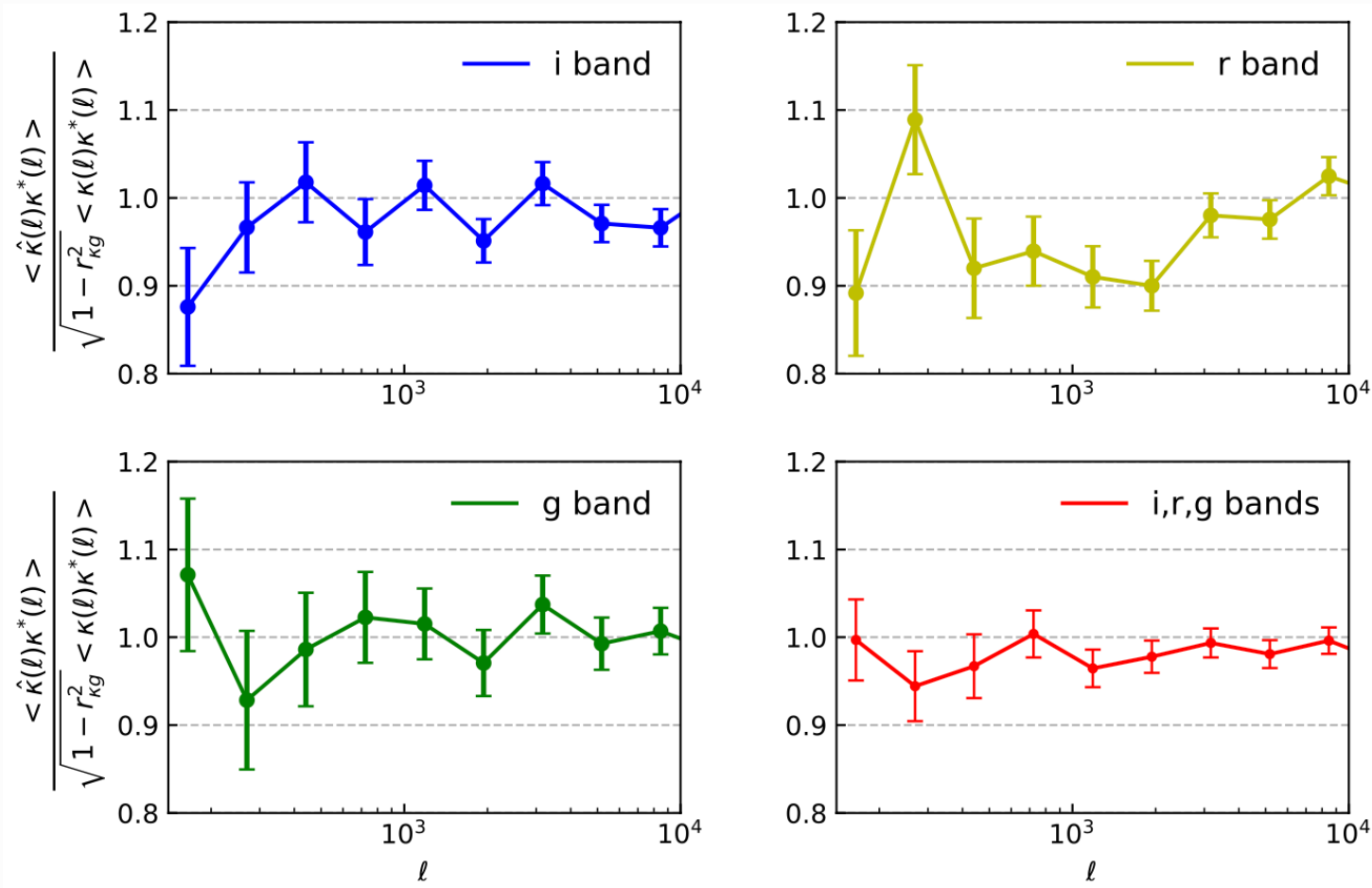
obtain the weighting w



$$\hat{\kappa} = \sum_i w_i \delta_i^L$$

Numerical Validation

How much true kappa is contained in the reconstructed kappa map



- Narrow photo-z bin $\Delta z=0.2$,

No obvious bias

5% level uncertainty in cross-correlation for LSST-like survey

How to improve ?

$$\delta^L = \delta_g + g\kappa + \delta^S$$

intrinsic
clustering

shot noise

$$\sum_i w_i = 0$$

$$\sum_i w_i \delta_{g,i} \neq 0 \quad \rightarrow \quad \text{systematic bias}$$

$$\delta^L = b\delta_m + g\kappa + \delta^S$$

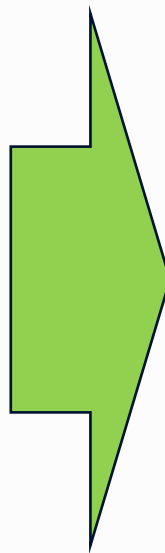
deterministic
bias

stochasticity

$$\sum_i w_i b_i = 0$$



if bias is known ...



Content

arXiv: 2306.15177

Ruijie MA +



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- **Weighting using estimated bias**
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Bias

$$\delta_{g,1} = b_1 \delta_m \quad \times \quad \delta_{g,2} = b_2 \delta_m$$

$$\mathbf{C} = \begin{pmatrix} P_{11}(k) & P_{12}(k) \\ P_{12}(k) & P_{22}(k) \end{pmatrix} = \begin{pmatrix} b_1^2 & b_1 b_2 \\ b_1 b_2 & b_2^2 \end{pmatrix} P_m(k)$$

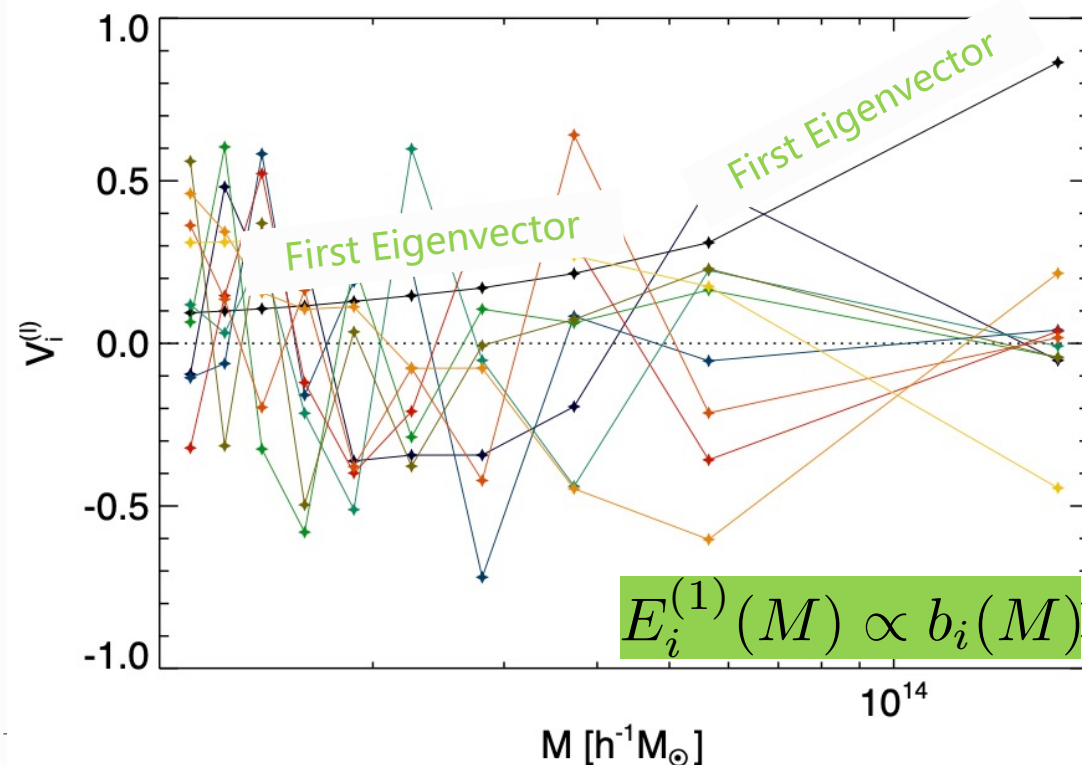
Bonoli & Pen 2009

➡
$$E^{(1)} = \frac{1}{\sqrt{b_1^2 + b_2^2}} (b_1, b_2)$$

In ideal case, the relative bias can be measured.



$$\sum_i w_i b_i = 0$$



Numerical Validation

- CosmicGrowth Suite (Jing 2019)

$L = 1200 \text{ Mpc}/h$

$N_p = 3072^3$

FoF halo

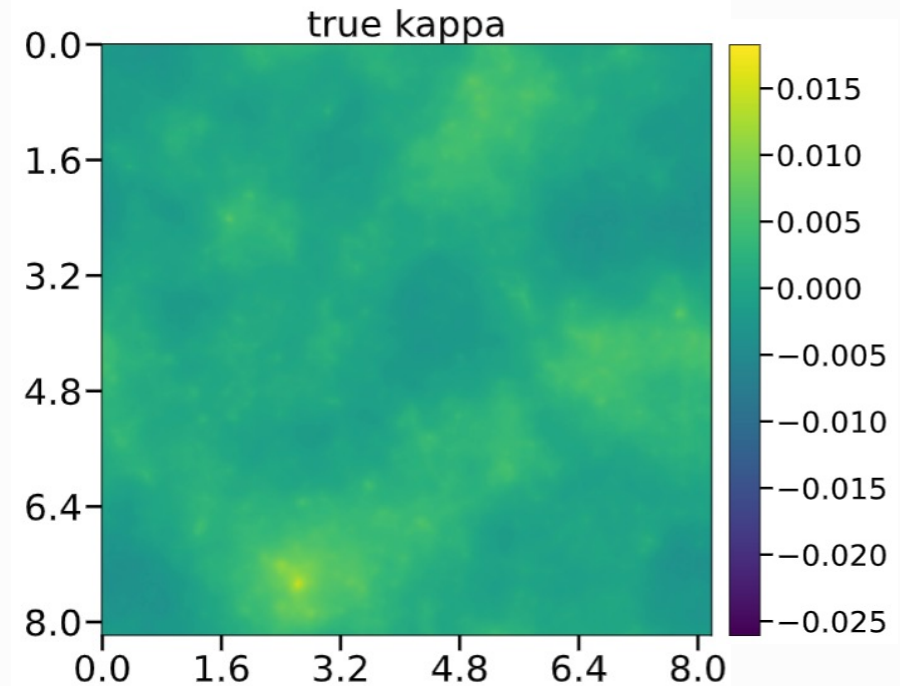
lightcone $8.2 \times 8.2 \text{ deg}^2$

20 lightcones

- CosmoDC2 (Korytov et al. 2019)

440 deg^2

ugrizY



Photometry band	<i>u</i>	<i>g</i>	<i>r</i>	<i>i</i>	<i>z</i>	<i>Y</i>
Magnitude cut	26.0	27.3	27.4	26.6	26.1	24.9
$\bar{n}$ of each band(arcmin ⁻²)	1.27	9.14	13.97	9.84	7.28	2.04
Number of flux bins	2	5	7	6	4	2

$$N_F = 26$$

Road map

Galaxy subsamples

➡ Auto and cross powers to form correlation matrix $\mathbf{C} = \begin{pmatrix} P_{11}(k) & P_{12}(k) \\ P_{12}(k) & P_{22}(k) \end{pmatrix}$

➡ Eigen decomposition to obtain the first eigen vector $E_i^{(1)} \propto b_i$

➡ Use this condition $\sum_i w_i E_i^{(1)} = 0$ to find w_i

➡ $\hat{\kappa} = \sum_i w_i \delta_i^L$

Error budget

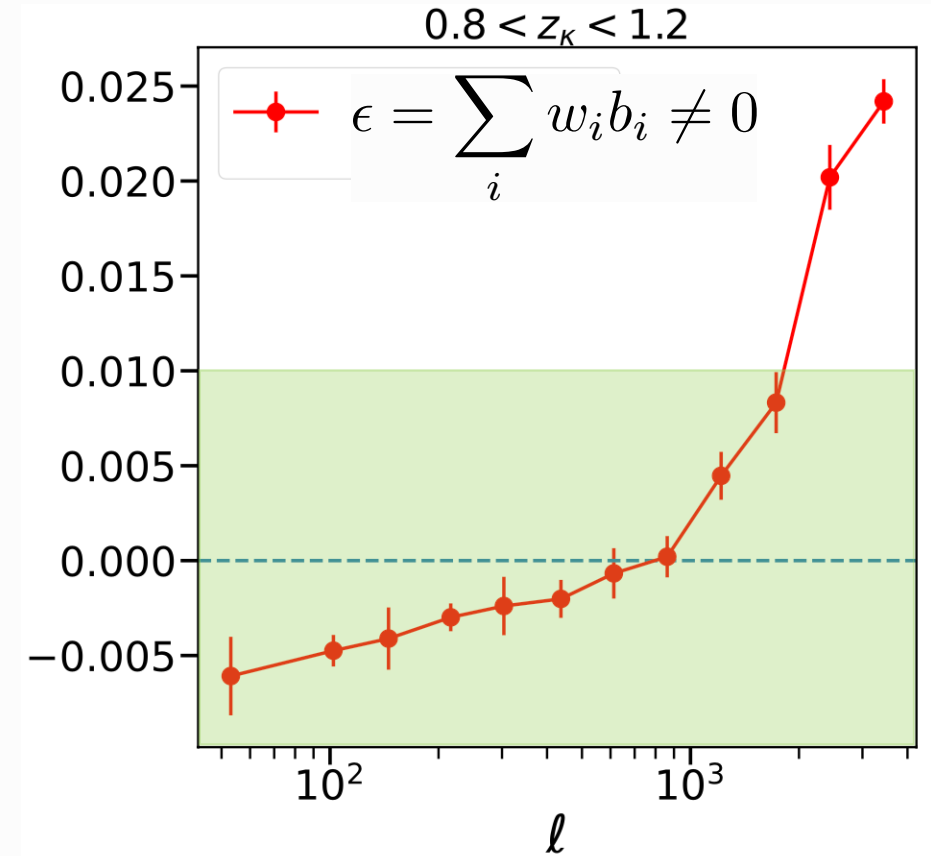
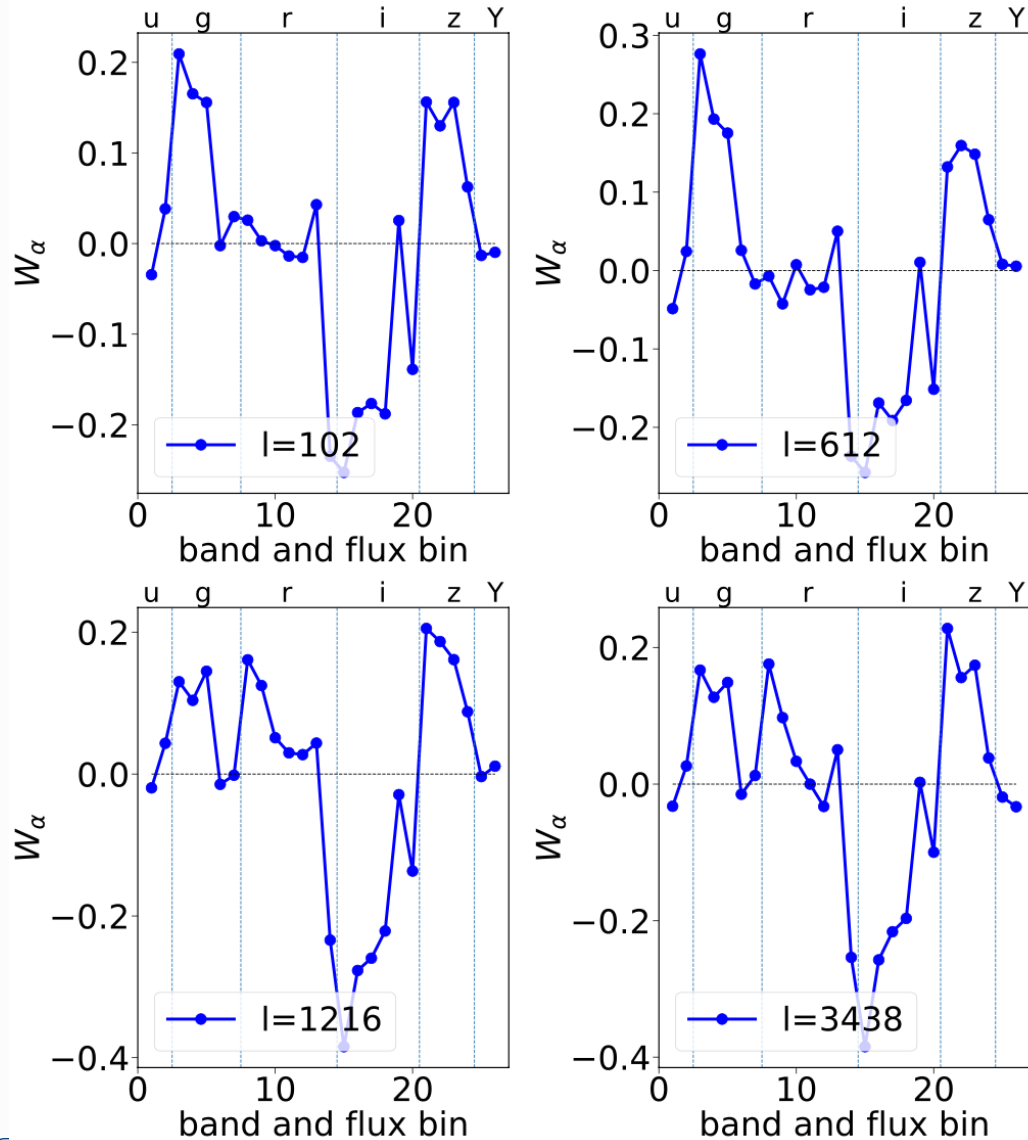
$$\begin{aligned} \hat{\kappa} &= \kappa \sum_i w_i g_i + \delta_m \sum_i w_i b_i + \sum_i w_i \delta_i^S \\ &= \kappa \quad + \epsilon \delta_m \quad + \sum_i w_i \delta_i^S \end{aligned}$$

Additive bias

Weighted shot noise

$$E_i^{(1)} \overset{?}{\propto} b_i \dots \epsilon = \sum_i w_i b_i \overset{?}{\neq} 0$$

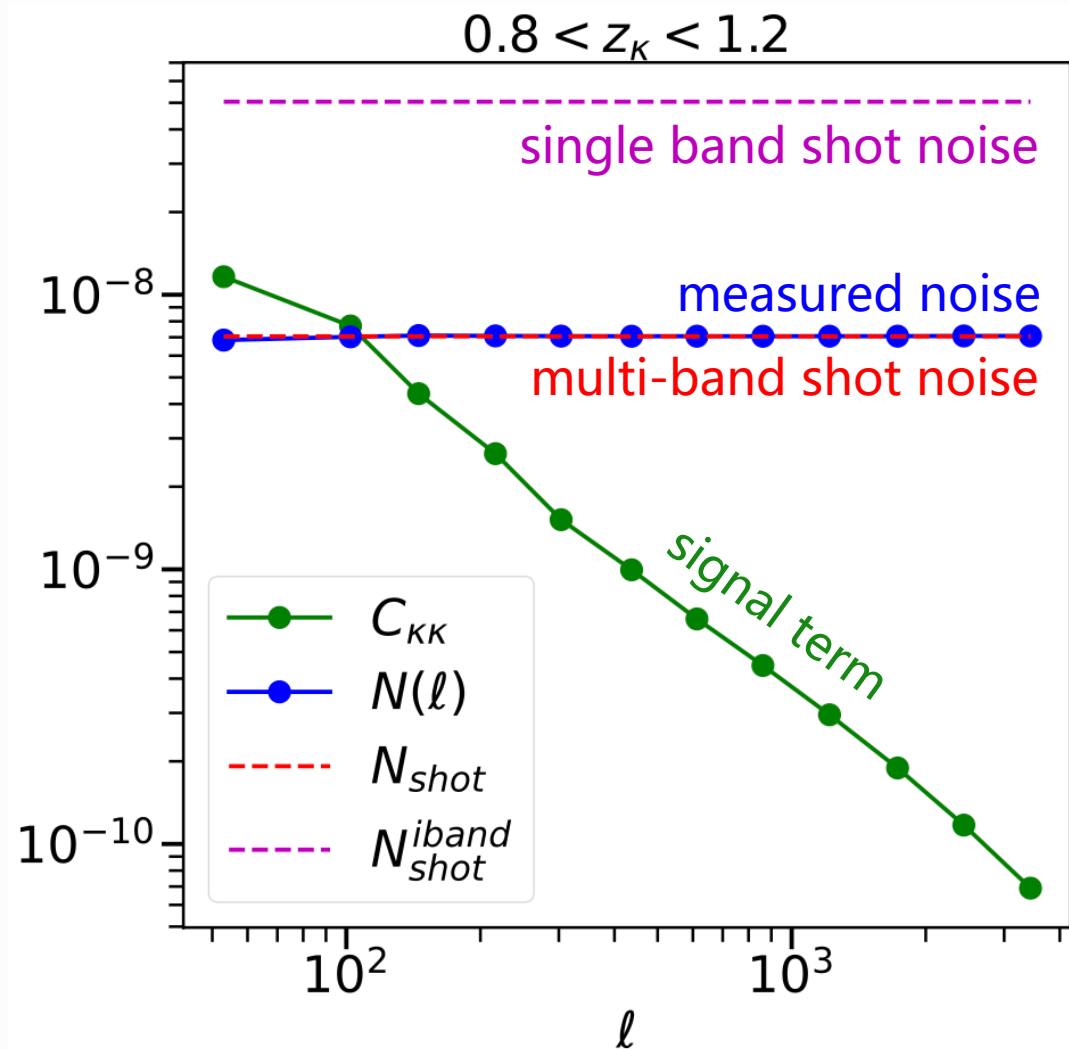
Numerical Validation



$$\hat{\kappa} = \kappa + \epsilon \delta_m + \sum_i w_i \delta_i^S$$

Intrinsic clustering is greatly suppressed by an order of 100 for $ell < 2000$.

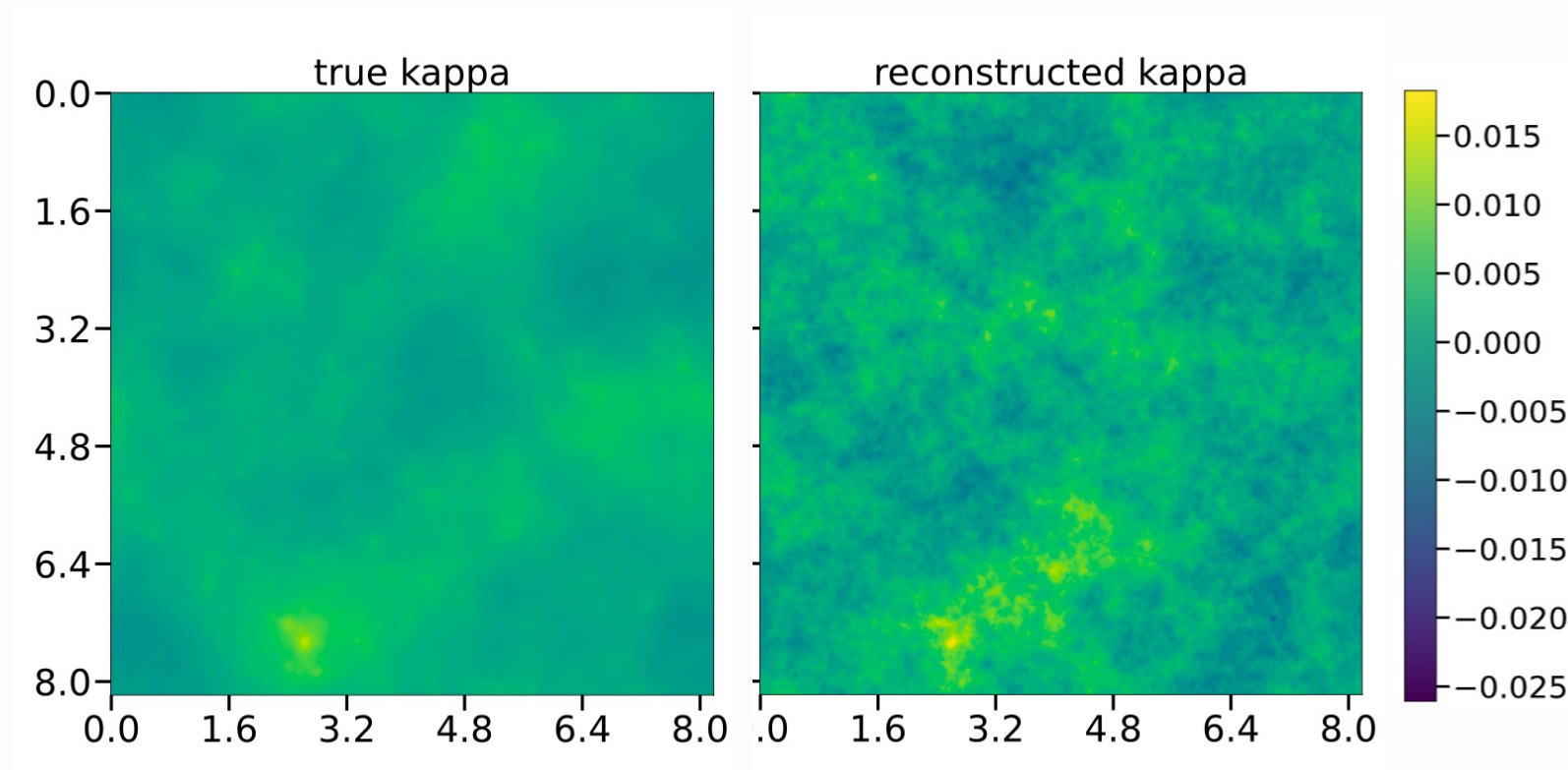
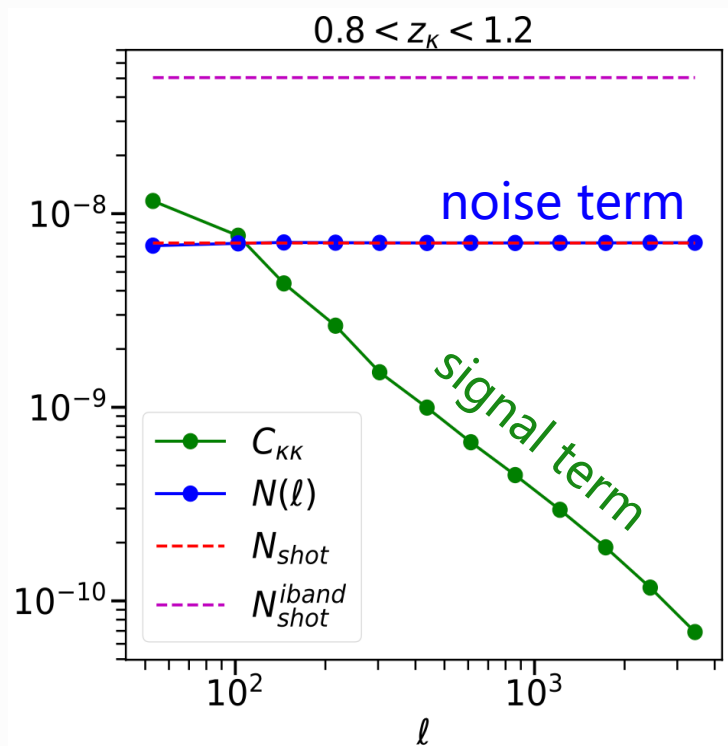
Error Budget



$$\hat{\kappa} = \underbrace{\kappa}_{\text{green}} + \underbrace{\epsilon \delta_m}_{\text{blue}} + \underbrace{\sum_i w_i \delta_i^S}_{\text{red}}$$

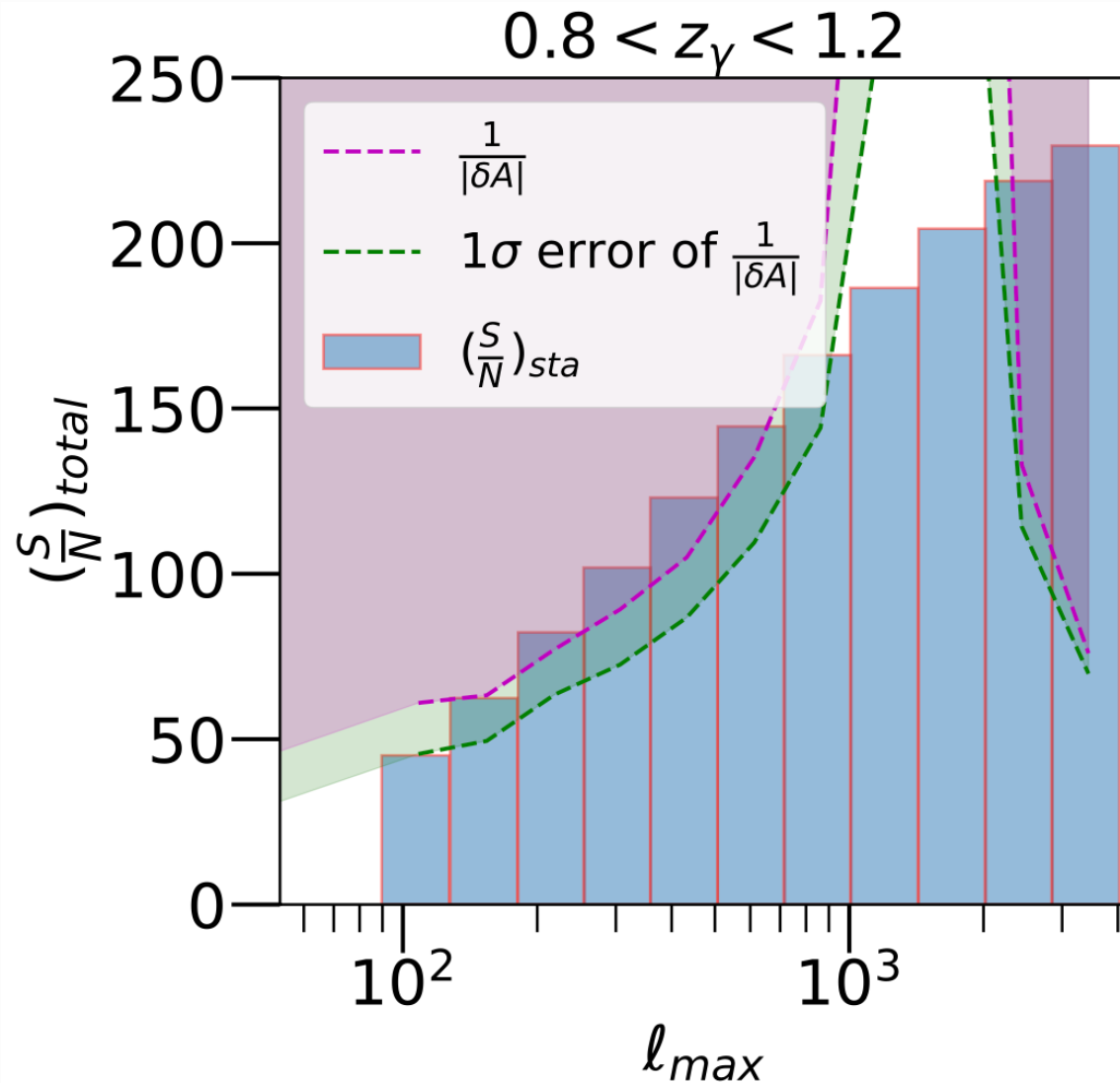
$$C_{\hat{\kappa}\hat{\kappa}}(\ell) = \underbrace{C_{\kappa\kappa}(\ell)}_{\text{green}} + \underbrace{N(\ell)}_{\text{blue}}$$

- **signal** dominated at $\ell < 200$
- **noise** dominated at $\ell > 200$
- **noise** is dominated by **shot noise**
- **multiband** is useful



The reconstructed kappa map is **noisy**.
The cross correlation with **external lensing field** will be much cleaner.

Cross with External



for $z_k \sim z_y \sim 1$, LSST-like survey
using $\ell < 2000$

cosmic magnification X cosmic shear
has

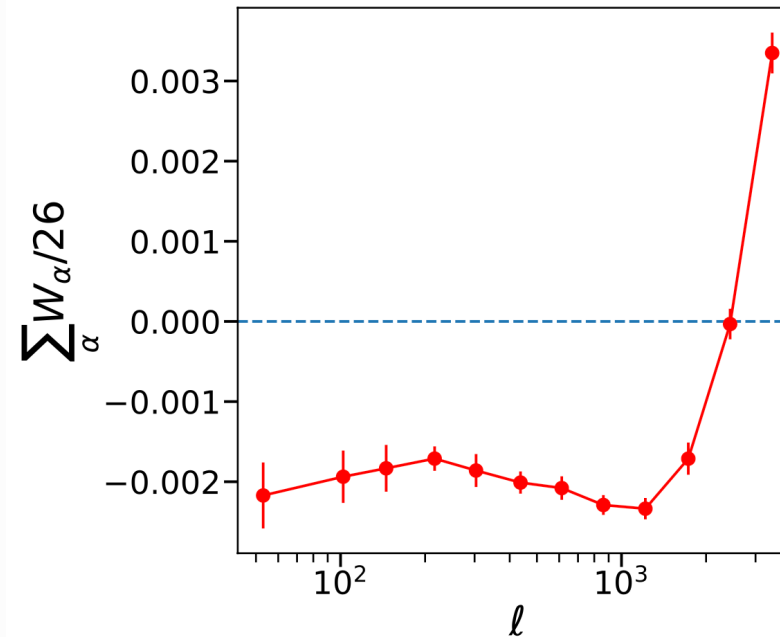
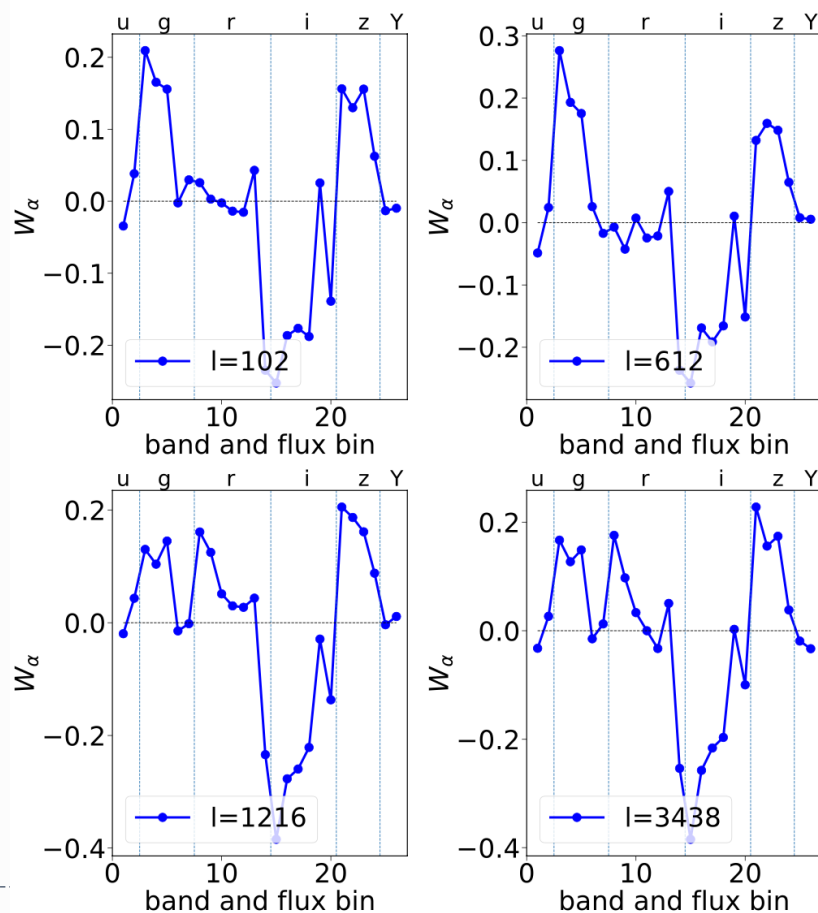
$S/N \sim 200$

Optimal weighting v.s. Modified ILC

$$\sum_i w_i g_i = 1$$

$$\sum_i w_i b_i = 0$$

$$\sum_i w_i = 0$$



Condition required by MILC is approximately satisfied

Content

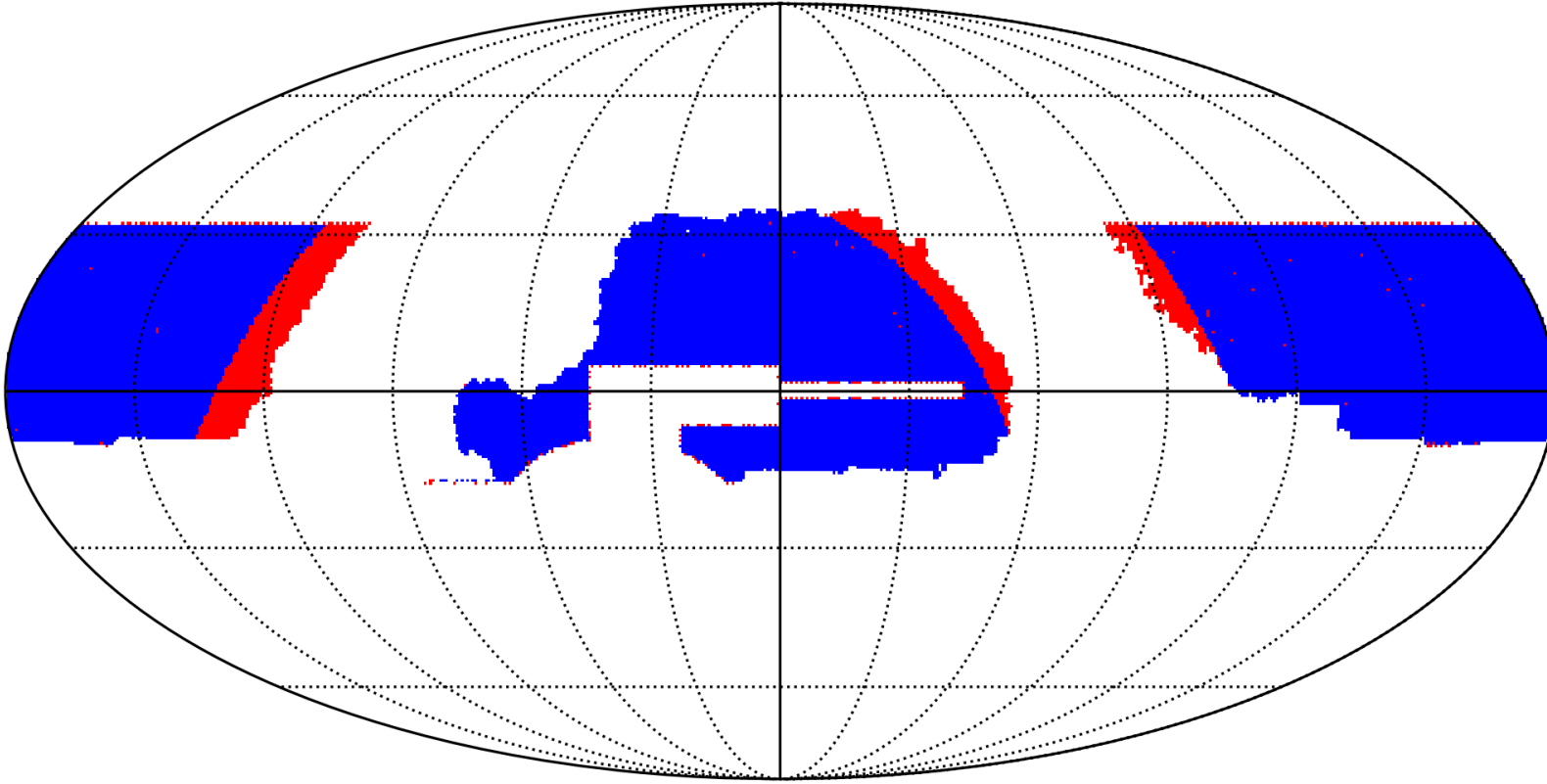
arXiv: 2310.15053

Jian QIN +



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Application in observation

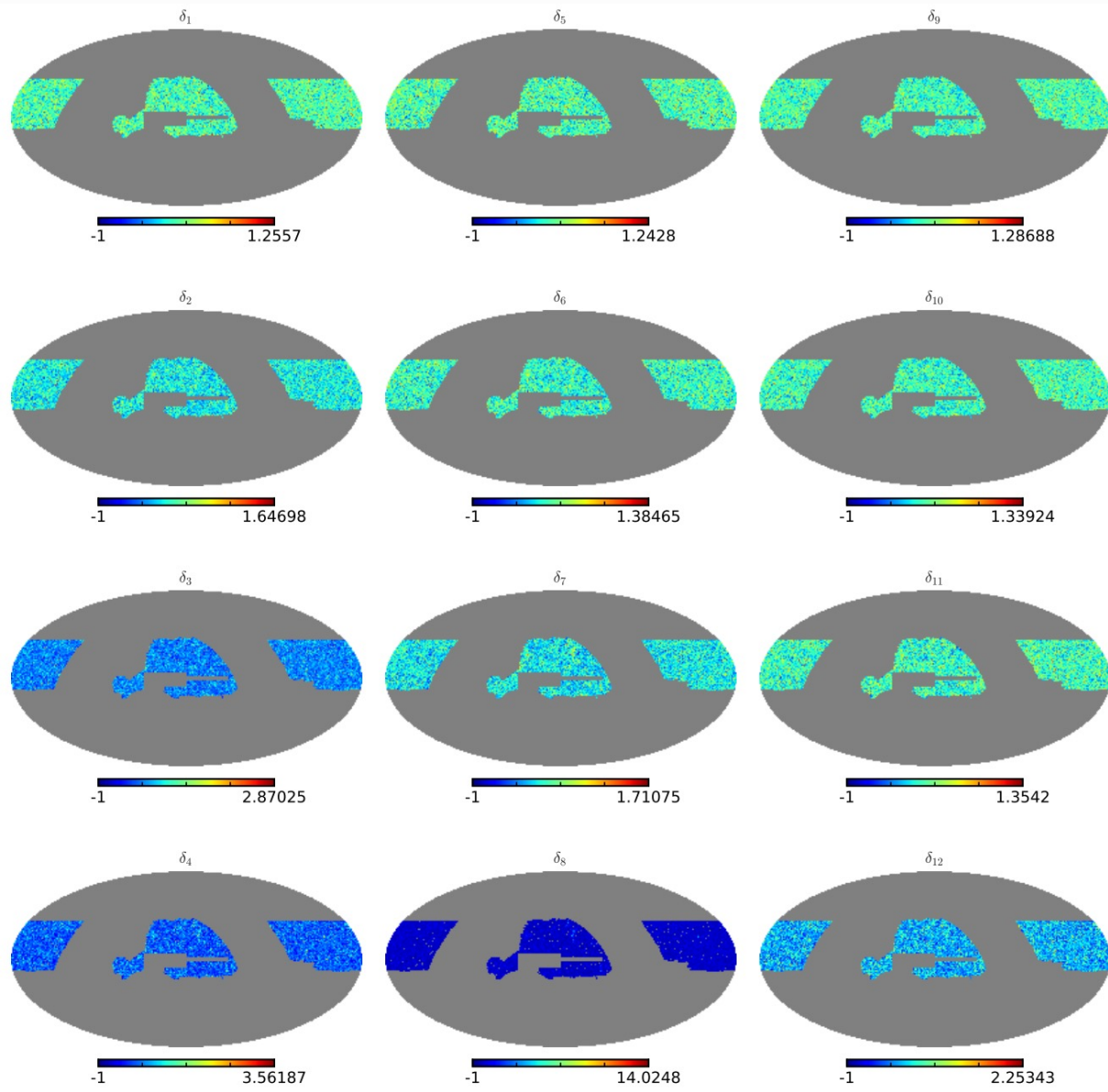


DECaLS DR9 galaxy distribution
for lensing magnification (MILC)
8365 deg²

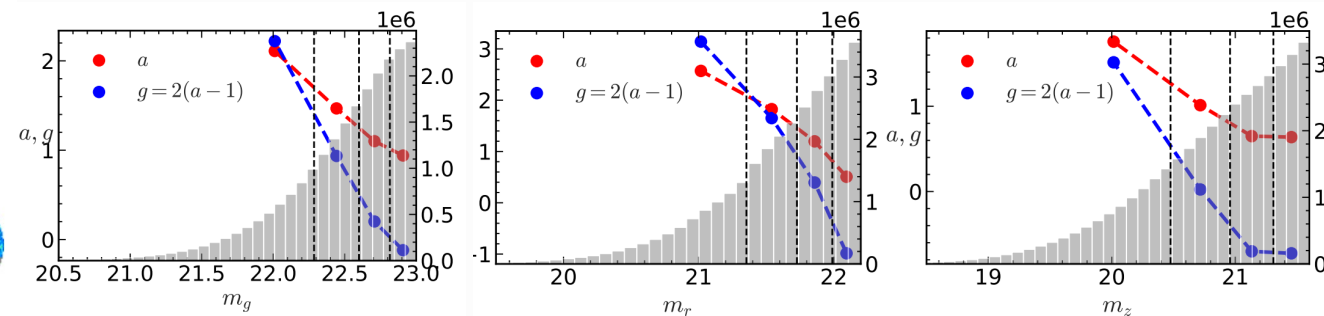
DECaLS DR8 shape catalogue
for cosmic shear
8960 deg²

$\xi^{\kappa\gamma}$

Application in observation



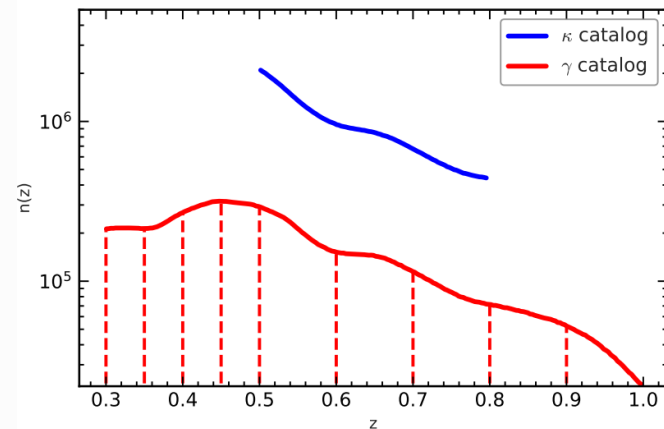
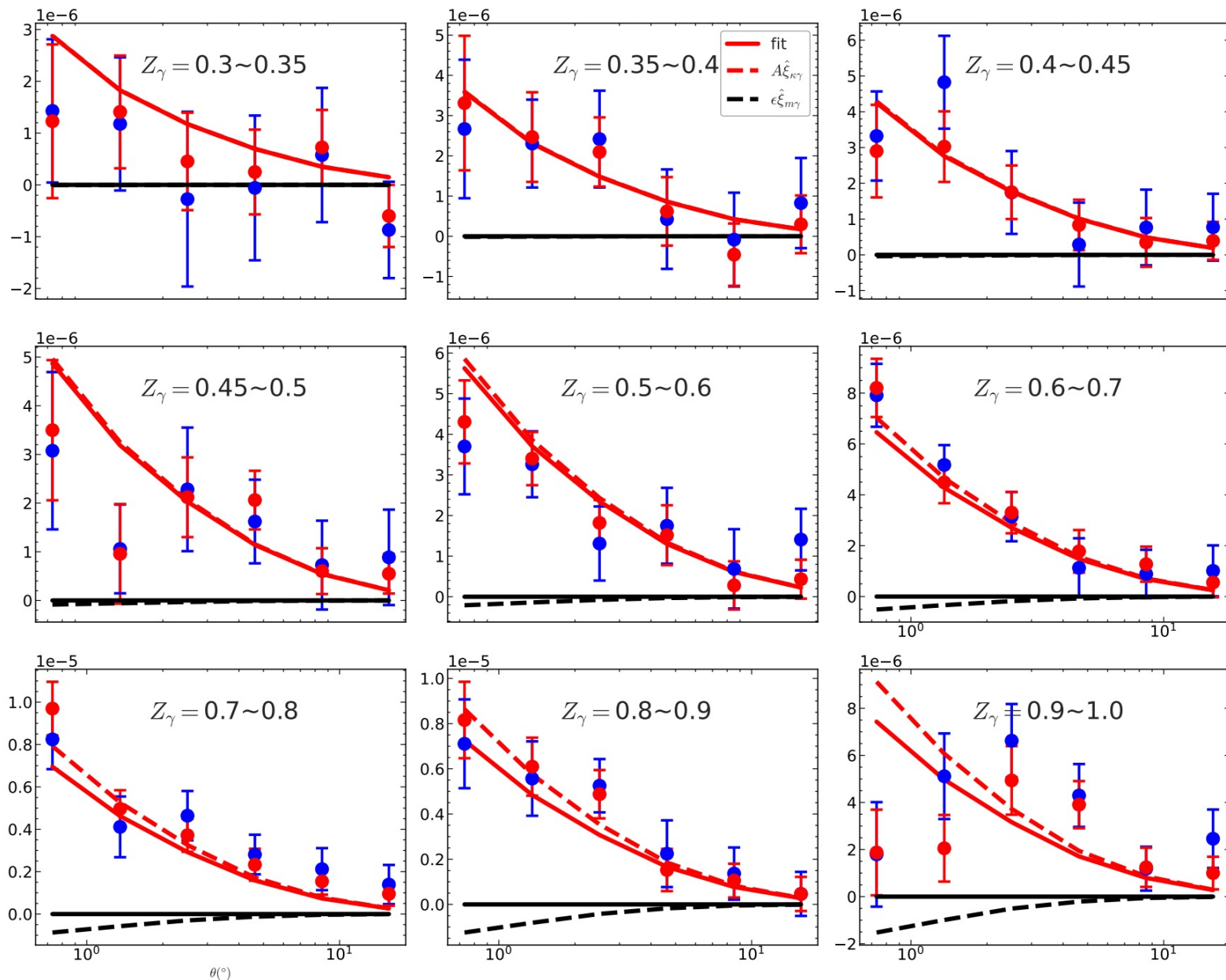
Sample	Magnitude Range	Galaxy Number	$\bar{n}(\text{arcmin}^{-2})$	<i>a</i>	<i>g</i>	<i>w</i>	band
1	(22.8, 23.0)	5590717	0.19	0.51	-0.99	-0.09	g
2	(22.6, 22.8)	5590717	0.19	1.20	0.40	-0.00	g
3	(22.3, 22.6)	5590717	0.19	1.83	1.65	0.09	g
4	(, 22.3)	5590717	0.19	2.57	3.14	0.20	g
5	(22.0, 22.2)	7740929	0.26	0.94	-0.12	0.04	r
6	(21.7, 22.0)	7740929	0.26	1.10	0.20	0.07	r
7	(21.4, 21.7)	7740929	0.26	1.47	0.94	0.06	r
8	(, 21.4)	7740929	0.26	2.11	2.22	0.03	r
9	(21.3, 21.6)	9882012	0.33	0.64	-0.72	-0.08	z
10	(21.0, 21.3)	9882012	0.33	0.65	-0.70	-0.11	z
11	(20.5, 21.0)	9882012	0.33	1.01	0.02	-0.11	z
12	(, 20.5)	9882012	0.33	1.76	1.51	-0.09	z



$$a = \frac{\log\left(\int_{f_1/(1+2\delta_F)}^{f_2/(1+2\delta_F)} n(F) dF\right) - \log\left(\int_{f_1}^{f_2} n(F) dF\right)}{2 \log(1+2\delta_F)}$$

$$g = 2(a - 1)$$

Application in observation



Imaging systematics not corrected
Imaging systematics corrected by RF

$$\xi_{\text{th}}^{\text{bestfit}} = A^{\text{bestfit}} \xi^{\kappa\gamma} + \epsilon^{\text{bestfit}} \xi^{m\gamma}$$

d.o.f = 52

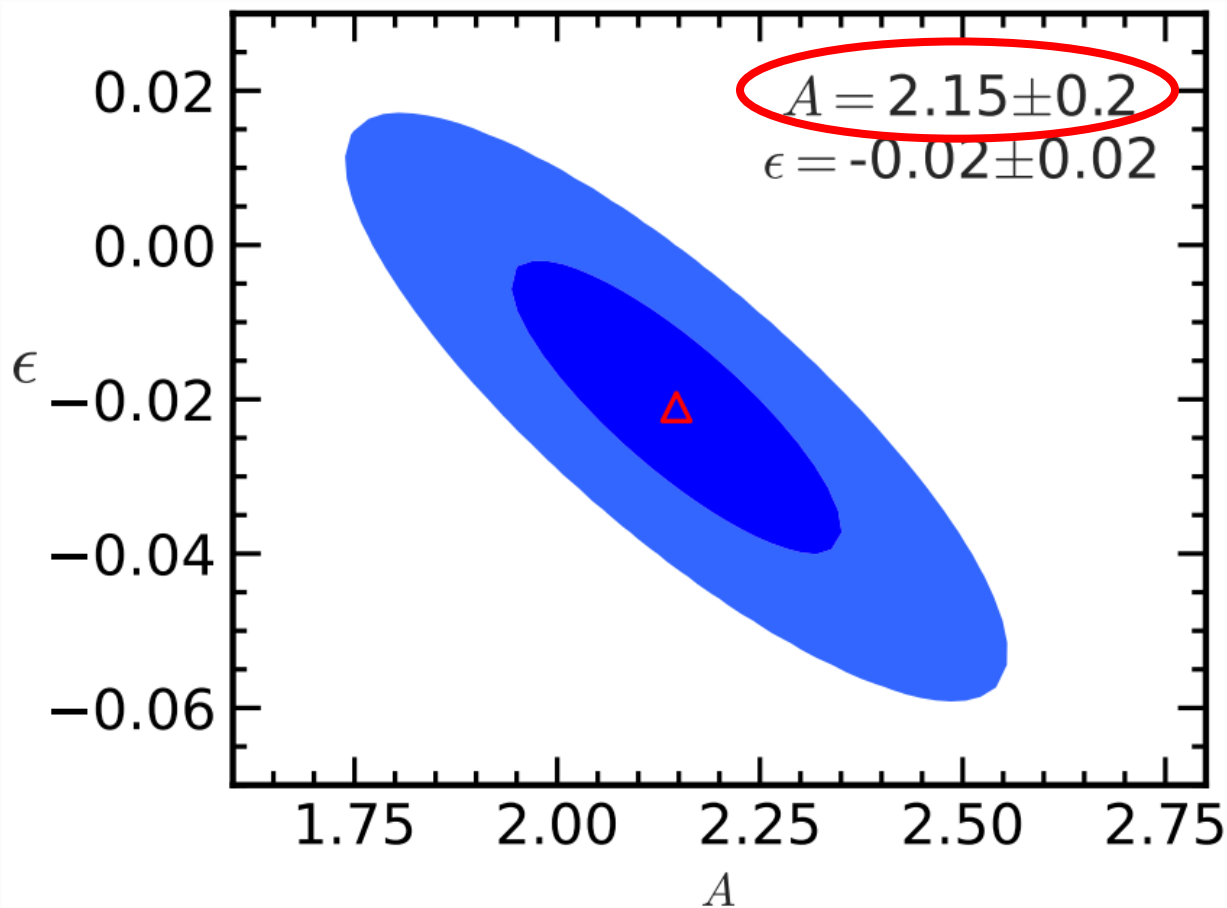
19.1 σ from null

$\chi^2_{\text{null}} = 367.6$

$\chi^2_{\text{min}} = 59$

10.7 σ from fitting

Application in observation



$$\xi_{\text{th}}^{\text{bestfit}} = A^{\text{bestfit}} \xi^{\kappa\gamma} + \epsilon^{\text{bestfit}} \xi^{m\gamma}$$

$$\hat{\kappa} = \underbrace{\kappa \sum_i w_i g_i}_{\text{Multiplicative bias}} + \underbrace{\delta_m \sum_i w_i b_i}_{\text{Additive bias}} + \sum_i w_i \delta_i^S$$

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Summary

- We are developing the various approaches to extract the cosmic magnification signal.
 - MILC, weighting using estimated bias, ...
- The intrinsic clustering is greatly suppressed ($\sim 100\times$) by these methods.
- The reconstructed kappa map is generally noisy.
- The numerical validation shows very promising results. The predicted S/N for $z_Y \sim z_K \sim 1$ cross correlation can reach ~ 200 for $\ell < 2000$ and LSST-like survey.
- The MILC method has been applied on multi-band observational data. We obtain a $\sim 10\sigma$ detection using DECaLS galaxies and shapes over 8365 deg^2 .
 - First direct lensing map over such a large sky area.
 - Multiplicative bias is identified, largely due to the g measurement.

THANK

YOU

Thank You!
