

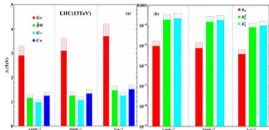


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# Probing Neutral Triple Gauge Couplings at the LHC, CEPC and SPPC

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#### EDITORS' SUGGESTION

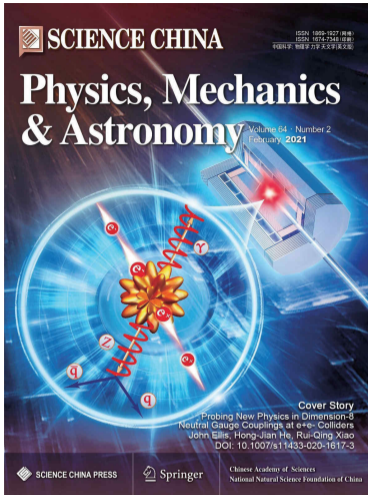
Probing neutral triple gauge couplings at the LHC and future hadron colliders

Many searches for new physics can be parameterized by higher-dimension operators in effective field theories. In this work, the authors show a consistent translation of dimension-8 operators into triple gauge boson form factors and analyze the expected experimental reach. Incorporating the full Standard Model symmetry requires an additional term which has been neglected in earlier work, leading to significantly different results.

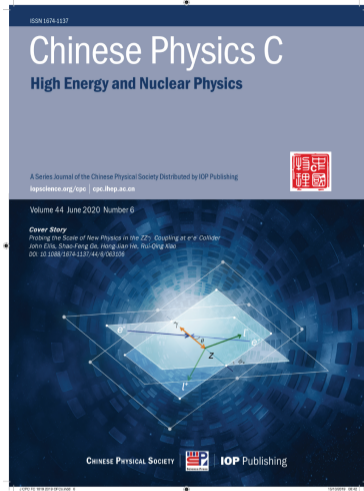
John Ellis, Hong-Jian He, and Rui-Qing Xiao

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Chin.Phys.C 44 (2020) 6, 063106

John Ellis, Hong-Jian He, Rui-Qing Xiao, Phys.Rev.D(Letter) (2023), in Press [ arXiv:2308.16887 ]

SMEFT is a model independent way to look for BSM physics

- Higher-dimensional operators as relics of higher energy physics, e.g., dimension-6:

$$\mathcal{L}_{eff} = \sum_i \frac{c_i}{\Lambda^2} \mathcal{O}_i = \sum_i \frac{\text{sign}(c_j)}{\Lambda_j^2} \mathcal{O}_i$$

- Operators constrained by  $SU(2) \times U(1)$  symmetry, assuming usual quantum numbers for SM particles
- Constrain operator coefficients with global analysis of experimental data;
- Non-zero  $c_i$  would indicate BSM: Masses, spins, quantum numbers of new particles?
- Dimension-8 contributions scaled by quartic power of new physics scale:

$$\Delta \mathcal{L}_{dim-8} = \sum_i \frac{\tilde{c}_i}{\tilde{\Lambda}^4} \mathcal{O}_i = \sum_i \frac{\text{sign}(\tilde{c}_i)}{\tilde{\Lambda}_i^4} \mathcal{O}_i$$

- Study processes without dimension-6 contributions, e.g.,  $\gamma\gamma \rightarrow \gamma\gamma$ ,  $gg \rightarrow \gamma\gamma$ ...
- Neutral triple-gauge couplings (nTGCs):  $Z\gamma Z^*$ ,  $Z\gamma\gamma^*$

Assuming only Lorentz and  $U(1)_{em}$  gauge invariance

$$\begin{aligned}\Gamma_{ZZV}^{\alpha\beta\mu}(q_1, q_2, q_3) &= \frac{(q_3^2 - m_V^2)}{m_Z^2} \left[ f_4^V (q_3^\alpha g^{\mu\beta} + q_3^\beta g^{\mu\alpha}) - f_5^V \epsilon^{\mu\alpha\beta\rho} (q_1 - q_2)_\rho \right], \\ \Gamma_{Z\gamma V}^{\alpha\beta\mu}(q_1, q_2, q_3) &= \frac{(q_3^2 - m_V^2)}{m_Z^2} \left\{ h_1^V (q_2^\mu g^{\alpha\beta} - q_2^\alpha g^{\mu\beta}) + \frac{h_2^V}{m_Z^2} q_3^\alpha [(q_2 q_3) g^{\mu\beta} - q_2^\mu q_3^\beta] \right. \\ &\quad \left. - h_3^V \epsilon^{\mu\alpha\beta\rho} q_{2\rho} - \frac{h_4^V}{m_Z^2} q_3^\alpha \epsilon^{\mu\beta\rho\sigma} P_\rho q_{2\sigma} \right\}.\end{aligned}$$

$f_{4,5}^V$  and  $h_{1,2,3,4}^V$  are function of  $q_i^2$ , but treated as constant in experimental analysis

$$\begin{aligned}\mathcal{L}_{NP} &= \frac{e}{m_Z^2} \left[ - [f_4^\gamma (\partial_\mu F^{\mu\beta}) + f_4^Z (\partial_\mu Z^{\mu\beta})] Z_\alpha (\partial^\alpha Z_\beta) + [f_5^\gamma (\partial^\sigma F_{\sigma\mu}) + f_5^Z (\partial^\sigma Z_{\sigma\mu})] \tilde{Z}^{\mu\beta} Z_\beta \right. \\ &\quad - [h_1^\gamma (\partial^\sigma F_{\sigma\mu}) + h_1^Z (\partial^\sigma Z_{\sigma\mu})] Z_\beta F^{\mu\beta} - [h_3^\gamma (\partial_\sigma F^{\sigma\rho}) + h_3^Z (\partial_\sigma Z^{\sigma\rho})] Z^\alpha \tilde{F}_{\rho\alpha} \\ &\quad - \left\{ \frac{h_2^\gamma}{m_Z^2} [\partial_\alpha \partial_\beta \partial^\rho F_{\rho\mu}] + \frac{h_2^Z}{m_Z^2} [\partial_\alpha \partial_\beta (\square + m_Z^2) Z_\mu] \right\} Z^\alpha F^{\mu\beta} \\ &\quad \left. + \left\{ \frac{h_4^\gamma}{2m_Z^2} [\square \partial^\sigma F^{\rho\alpha}] + \frac{h_4^Z}{2m_Z^2} [(\square + m_Z^2) \partial^\sigma Z^{\rho\alpha}] \right\} Z_\sigma \tilde{F}_{\rho\alpha} \right],\end{aligned}$$

The conventional nTGC form factor formalism was adopted by previous LHC experimental analysis, **but it disregards  $SU(2) \times U(1)$  of SM!**

\* G. J. Gounaris, J. Layssac, and F. M. Renard, Phys. Rev. D 61 (2000) 073013

The following CPC and CPV nTGC operators include Higgs doublets:

$$\mathcal{O}_{\tilde{B}W}^{(\text{CPC})} = i H^\dagger \tilde{B}_{\mu\nu} W^{\mu\rho} \{D_\rho, D^\nu\} H + \text{h.c.},$$

$$\mathcal{O}_{\tilde{B}\tilde{W}}^{(\text{CPC})} = i H^\dagger (D_\sigma \tilde{W}_{\mu\nu}^a W^{a\mu\sigma} + D_\sigma \tilde{B}_{\mu\nu} B^{\mu\sigma}) D^\nu H + \text{h.c.},$$

$$\tilde{\mathcal{O}}_{BW}^{(\text{CPV})} = i H^\dagger B_{\mu\nu} W^{\mu\rho} \{D_\rho, D^\nu\} H + \text{h.c.},$$

$$\tilde{\mathcal{O}}_{WW}^{(\text{CPV})} = i H^\dagger W_{\mu\nu} W^{\mu\rho} \{D_\rho, D^\nu\} H + \text{h.c.},$$

$$\tilde{\mathcal{O}}_{BB}^{(\text{CPV})} = i H^\dagger B_{\mu\nu} B^{\mu\rho} \{D_\rho, D^\nu\} H + \text{h.c.},$$

The dimension-8 nTGC operators containing pure gauge fields only:

$$g\mathcal{O}_{G+}^{(\text{CPC})} = \tilde{B}_{\mu\nu} W^{a\mu\rho} (D_\rho D_\lambda W^{a\nu\lambda} + D^\nu D^\lambda W_{\lambda\rho}^a),$$

$$g\mathcal{O}_{G-}^{(\text{CPC})} = \tilde{B}_{\mu\nu} W^{a\mu\rho} (D_\rho D_\lambda W^{a\nu\lambda} - D^\nu D^\lambda W_{\lambda\rho}^a),$$

$$g\tilde{\mathcal{O}}_{G+}^{(\text{CPV})} = B_{\mu\nu} W^{a\mu\rho} (D_\rho D_\lambda W^{a\nu\lambda} + D^\nu D^\lambda W_{\lambda\rho}^a),$$

$$g\tilde{\mathcal{O}}_{G-}^{(\text{CPV})} = B_{\mu\nu} W^{a\mu\rho} (D_\rho D_\lambda W^{a\nu\lambda} - D^\nu D^\lambda W_{\lambda\rho}^a),$$

# Neutral Triple Gauge Vertices with on-shell $Z\gamma$

Dimension-8 SMEFT:

$$\Gamma_{Z\gamma Z^*(G_+)}^{\alpha\beta\mu}(q_1, q_2, q_3) = -\frac{v(q_3^2 - M_Z^2)}{M_Z [\Lambda_{G_+}^4]} \left( q_3^2 q_{2\nu} \epsilon^{\alpha\beta\mu\nu} + 2q_2^\alpha q_{3\nu} q_{2\sigma} \epsilon^{\beta\mu\nu\sigma} \right),$$

$$\Gamma_{Z\gamma\gamma^*(G_+)}^{\alpha\beta\mu}(q_1, q_2, q_3) = -\frac{s_W v q_3^2}{c_W M_Z [\Lambda_{G_+}^4]} \left( q_3^2 q_{2\nu} \epsilon^{\alpha\beta\mu\nu} + 2q_2^\alpha q_{3\nu} q_{2\sigma} \epsilon^{\beta\mu\nu\sigma} \right),$$

$$\Gamma_{Z\gamma Z^*(\tilde{B}W)}^{\alpha\beta\mu}(q_1, q_2, q_3) = \frac{v M_Z (q_3^2 - M_Z^2)}{[\Lambda_{\tilde{B}W}^4]} \epsilon^{\alpha\beta\mu\nu} q_{2\nu},$$

$$\Gamma_{Z\gamma\gamma^*(G_-)}^{\alpha\beta\mu}(q_1, q_2, q_3) = -\frac{s_W v M_Z}{c_W [\Lambda_{G_-}^4]} \epsilon^{\alpha\beta\mu\nu} q_{2\nu} q_3^2.$$

Conventional form factor parameterization:  $\Gamma_{Z\gamma V^*}^{\alpha\beta\mu}(q_1, q_2, q_3) = \frac{e(q_3^2 - M_V^2)}{M_Z^2} \left( h_3^V q_{2\nu} \epsilon^{\alpha\beta\mu\nu} + \frac{h_4^V}{M_Z^2} q_2^\alpha q_{3\nu} q_{2\sigma} \epsilon^{\beta\mu\nu\sigma} \right),$

Full  $SU(2) \times U(1)$  gauge constraints:  $\Gamma_{Z\gamma V^*}^{\alpha\beta\mu(8)}(q_1, q_2, q_3) = \frac{e(q_3^2 - M_V^2)}{M_Z^2} \left[ \left( h_3^V + h_5^V \frac{q_3^2}{M_Z^2} \right) q_{2\nu} \epsilon^{\alpha\beta\mu\nu} + \frac{h_4^V}{M_Z^2} q_2^\alpha q_{3\nu} q_{2\sigma} \epsilon^{\beta\mu\nu\sigma} \right],$

$\mathcal{O}(E^5)$  terms must cancel each other in amplitude with longitudinal  $Z$ :

$$\mathcal{T}[f\bar{f} \rightarrow Z_L \gamma] = h_3^V \mathcal{O}(E^3) + h_4^V \mathcal{O}(E^5) + h_5^V \mathcal{O}(E^5) = \Lambda_j^{-4} \mathcal{O}(E^3).$$

$\mathcal{T}[f\bar{f} \rightarrow Z_L \gamma]$  as contributed by the gauge-invariant dimension-8 nTGC operators must obey **the equivalence theorem (ET)**:

$$\mathcal{T}_{(8)}[Z_L, \gamma_T] = \mathcal{T}_{(8)}[-i\pi^0, \gamma_T] + B = \mathcal{O}(E^3),$$

## Why doubly off-shell?

At  $pp$  colliders  $Z^* \rightarrow \nu \bar{\nu}$  cannot be separated from  $Z \rightarrow \nu \bar{\nu}$ .

CPC:

$$\Gamma_{Z^* \gamma \gamma^*}^{\alpha\beta\mu}(q_1, q_2, q_3) = \frac{e}{M_Z^2} \left( h_{31}^\gamma + \frac{\hat{h}_3^\gamma q_1^2}{M_Z^2} \right) q_3^2 q_{2\nu} \epsilon^{\alpha\beta\mu\nu} + \frac{e s_W \hat{h}_4 q_3^2}{2 c_W M_Z^4} (2 q_2^\alpha q_{3\nu} q_{2\sigma} \epsilon^{\beta\mu\nu\sigma} + q_3^2 q_{2\nu} \epsilon^{\alpha\beta\mu\nu}),$$

$$\Gamma_{Z^* \gamma Z^*}^{\alpha\beta\mu}(q_1, q_2, q_3) = \frac{e(q_3^2 - q_1^2)}{M_Z^2} \left[ \hat{h}_3^Z q_{2\nu} \epsilon^{\alpha\beta\mu\nu} + \frac{\hat{h}_4}{2M_Z^2} (2q_2^\alpha q_{3\nu} q_{2\sigma} \epsilon^{\beta\mu\nu\sigma} + q_3^2 q_{2\nu} \epsilon^{\alpha\beta\mu\nu}) \right].$$

CPV:

$$\Gamma_{Z^* \gamma \gamma^*}^{\alpha\beta\mu}(q_1, q_2, q_3) = \frac{e}{M_Z^2} \left( h_{11}^\gamma + \frac{\hat{h}_1^\gamma q_1^2}{M_Z^2} \right) q_3^2 (q_2^\alpha g^{\mu\beta} - q_2^\mu g^{\alpha\beta}) + \frac{e s_W \hat{h}_2 q_3^2}{2 c_W M_Z^4} (q_1^2 q_2^\alpha g^{\mu\beta} - q_3^2 q_2^\mu g^{\alpha\beta}),$$

$$\Gamma_{Z^* \gamma Z^*}^{\alpha\beta\mu}(q_1, q_2, q_3) = \frac{e(q_3^2 - q_1^2)}{M_Z^2} \left[ \hat{h}_1^Z (q_2^\alpha g^{\mu\beta} - q_2^\mu g^{\alpha\beta}) + \frac{\hat{h}_2}{2M_Z^2} (q_1^2 q_2^\alpha g^{\mu\beta} - q_3^2 q_2^\mu g^{\alpha\beta}) \right],$$

## Matching Form Factors to Dimension-8 Operators

$$\hat{h}_4 = -\frac{v^2 M_Z^2}{s_W c_W [\Lambda_{G^+}^4]}, \quad \hat{h}_3^Z = \frac{v^2 M_Z^2}{2 s_W c_W [\Lambda_{BW}^4]},$$

$$\hat{h}_3^\gamma = -\frac{v^2 M_Z^2}{2 c_W^2 [\Lambda_{G^-}^4]}, \quad h_{31}^\gamma = -\frac{v^2 M_Z^2}{s_W c_W [\Lambda_{BW}^4]},$$

$$\hat{h}_1^Z = \frac{v^2 M_Z^2}{4 c_W s_W} \left( \frac{c_W^2 - s_W^2}{[\Lambda_{WB}^4]} - \frac{c_W s_W}{[\Lambda_{WW}^4]} + \frac{4 c_W s_W}{[\Lambda_{BB}^4]} \right),$$

$$h_{11}^\gamma = \frac{v^2 M_Z^2}{4 c_W s_W} \left( \frac{2 c_W s_W}{[\Lambda_{WB}^4]} - \frac{s_W^2}{[\Lambda_{WW}^4]} - \frac{4 c_W^2}{[\Lambda_{BB}^4]} \right),$$

$$\hat{h}_1^\gamma = \frac{v^2 M_Z^2}{4 c_W^2 [\Lambda_{G^-}^4]}, \quad \hat{h}_2 = -\frac{v^2 M_Z^2}{2 s_W c_W [\Lambda_{G^+}^4]}.$$

# Cross section of $f\bar{f} \rightarrow Z\gamma$

$$\sigma = \sigma_0(\text{SM}^2) + \sigma_1(\text{SM} \times \text{nTGC}) + \sigma_2(\text{nTGC}^2)$$

$$\sigma_0 = \frac{e^4(c_L^2 + c_R^2) Q^2 \left[ -(s - M_Z^2)^2 - 2(s^2 + M_Z^4) \ln \sin \frac{\delta}{2} \right]}{8\pi s_W^2 c_W^2 (s - M_Z^2) s^2} = \mathcal{O}(s^{-1}),$$

$$\begin{aligned} \sigma_1 &= \frac{e^2 c_L Q T_3 M_Z^2 (s - M_Z^2)}{4\pi s_W c_W s} \frac{1}{[\Lambda_{G+}^4]} - \frac{e^2 Q (c_L x_L - c_R x_R) M_Z^2 (s - M_Z^2) (s + M_Z^2)}{8\pi s_W c_W s^2} \frac{1}{[\Lambda_j^4]}, \\ &= \frac{e^2 c_L Q T_3 M_Z^2 (s - M_Z^2)}{4\pi s_W c_W s} \frac{h_4}{r_4^4} - \frac{e^2 Q (c_L x_L - c_R x_R) M_Z^2 (s - M_Z^2) (s + M_Z^2)}{8\pi s_W c_W s^2} \frac{h_3^V}{r_3^V} = h_4 \mathcal{O}(s^0) + h_3^V \mathcal{O}(s^0), \end{aligned}$$

$$\begin{aligned} \sigma_2 &= \frac{T_3^2 (s + M_Z^2) (s - M_Z^2)^3}{48\pi s} \frac{1}{\Lambda_{G+}^8} + \frac{(x_L^2 + x_R^2) M_Z^2 (s + M_Z^2) (s - M_Z^2)^3}{48\pi s^2} \frac{1}{\Lambda_j^8} + \text{cross terms} \\ &= \frac{T_3^2 (s + M_Z^2) (s - M_Z^2)^3}{48\pi s} \left( \frac{h_4}{r_4} \right)^2 + \frac{(x_L^2 + x_R^2) M_Z^2 (s + M_Z^2) (s - M_Z^2)^3}{48\pi s^2} \left( \frac{h_3^V}{r_3^V} \right)^2 + \text{cross terms} = (h_4)^2 \mathcal{O}(s^3) + (h_3^V)^2 \mathcal{O}(s^2) + \text{cross terms}, \end{aligned}$$

$$(x_L, x_R) = -Q s_W^2 (1, 1), \quad (\text{for } \mathcal{O}_j = \mathcal{O}_{G-}),$$

$$(x_L, x_R) = (T_3 - Q s_W^2, -Q s_W^2), \quad (\text{for } \mathcal{O}_j = \mathcal{O}_{\bar{B}W}),$$

$$(x_L, x_R) = -(T_3, 0), \quad (\text{for } \mathcal{O}_j = \mathcal{O}_{C+}).$$

Contribution of CPV nTGC to  $\sigma_1$  vanish

Contribution of CPV nTGC to  $\sigma_2$  has the same structure as that of the corresponding CPC nTGC



The full amplitude  $\mathcal{T}_{\sigma\sigma'\lambda}^{ss'}$  can be expressed as combination of  $\mathcal{T}_{ss'}(\lambda_Z\lambda_\gamma)$

$ss'$ : helicities of initial state fermions

$\sigma\sigma'$ : helicities of final state fermions

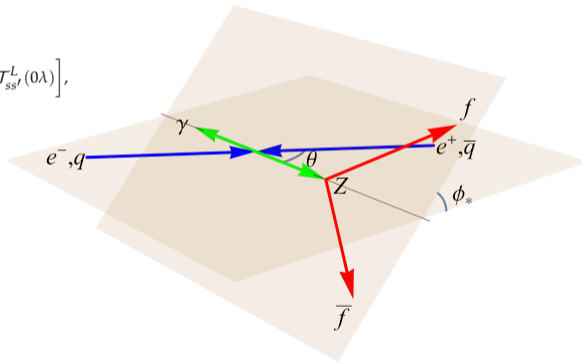
$\lambda_Z\lambda_\gamma$ : polarizations of  $Z\gamma$

$$\begin{aligned} \mathcal{T}_{\sigma\sigma'\lambda}^{ss'}(f\bar{f}\gamma) &= \frac{eM_Z\mathcal{D}_Z}{s_Wc_W} \left[ \sqrt{2}e^{i\phi_*} \left( f_R^\sigma \cos^2 \frac{\theta_*}{2} - f_L^\sigma \sin^2 \frac{\theta_*}{2} \right) \mathcal{T}_{ss'}^T(+\lambda) \right. \\ &\quad \left. + \sqrt{2}e^{-i\phi_*} \left( f_R^\sigma \sin^2 \frac{\theta_*}{2} - f_L^\sigma \cos^2 \frac{\theta_*}{2} \right) \mathcal{T}_{ss'}^T(-\lambda) + (f_R^\sigma + f_L^\sigma) \sin\theta_* \mathcal{T}_{ss'}^L(0\lambda) \right], \end{aligned}$$

$(f_L^\sigma, f_R^\sigma) = ((T_3 - Qs_W^2)\delta_{\sigma,-\frac{1}{2}}, -Qs_W^2\delta_{\sigma,\frac{1}{2}})$  denote the couplings of final states fermions

$$\cos\phi_* = \frac{(\mathbf{p}_{q,e^-} \times \mathbf{p}_Z) \cdot (\mathbf{p}_f \times \mathbf{p}_{\bar{f}})}{|\mathbf{p}_{q,e^-} \times \mathbf{p}_Z| |\mathbf{p}_f \times \mathbf{p}_{\bar{f}}|}.$$

At LHC,  $q$  can be emitted from either proton beam  $\rightarrow \cos\phi_*$  terms cancel out,  $\cos(2\phi_*) = 2\cos^2\phi_* - 1$  are not affected



Normalized angular distribution function at  $\mathcal{O}(1/\Lambda^0), \mathcal{O}(1/\Lambda^4), \mathcal{O}(1/\Lambda^8)$

$$f_{\phi_*}^0 = \frac{1}{2\pi} + \frac{3\pi^2 c_-^2 f_-^2 M_Z \sqrt{s} (s + M_Z^2) \cos \phi_* - 8c_+^2 f_+^2 M_Z^2 s \cos 2\phi_*}{16\pi c_+^2 f_+^2 [(s - M_Z^2)^2 + 2(s^2 + M_Z^4) \ln \sin \frac{\delta}{2}]} + \mathcal{O}(\delta),$$

$$f_{\phi_*}^1 = \frac{1}{2\pi} - \frac{3\pi(f_L^2 - f_R^2)(M_Z^2 + 5s) \cos \phi_*}{256(f_L^2 + f_R^2)M_Z \sqrt{s}} + \frac{s \cos 2\phi_*}{8\pi M_Z^2},$$

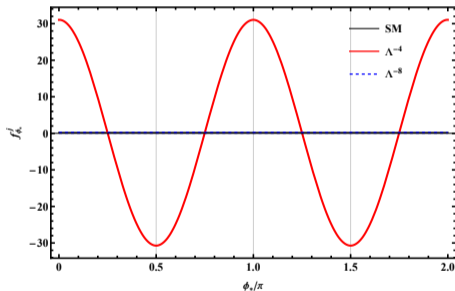
$$f_{\phi_*}^2 = \frac{1}{2\pi} - \frac{9\pi(f_L^2 - f_R^2)M_Z \sqrt{s} \cos \phi_*}{128(f_L^2 + f_R^2)(s + M_Z^2)},$$

$$(c_{\pm}^2, f_{\pm}^2) = (c_L^2 \pm c_R^2, f_L^2 \pm f_R^2)$$

Define

$$\mathcal{O}_1 = \left| \sigma_1 \int d\phi_* f_{\phi_*}^1 \times \text{sign}(\cos 2\phi_*) \right| = \mathcal{O}(s),$$

to get leading energy dependence of interference term.



$q\bar{q} \rightarrow Z\gamma \rightarrow l^-l^+\gamma$  at LHC

$$f_{\phi_*}^0 = \frac{1}{2\pi} + \frac{3\pi^2 c_-^2 f_-^2 M_Z \sqrt{s} (s + M_Z^2) \cos\phi_* - 8c_+^2 f_+^2 M_Z^2 s \cos 2\phi_*}{16\pi c_+^2 f_+^2 [(s - M_Z^2)^2 + 2(s^2 + M_Z^4) \ln \sin \frac{\delta}{2}]} + \mathcal{O}(\delta),$$

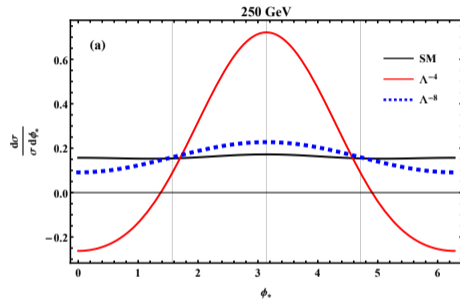
$$f_{\phi_*}^1 = \frac{1}{2\pi} - \frac{9\pi(c_L x_L + c_R x_R)(f_L^2 - f_R^2)\sqrt{s} \cos\phi_*}{128(c_L x_L - c_R x_R)(f_L^2 + f_R^2)M_Z} + \frac{s \cos 2\phi_*}{4\pi(s + M_Z^2)},$$

$$f_{\phi_*}^2 = \frac{1}{2\pi} - \frac{9\pi(x_L^2 - x_R^2)(f_L^2 - f_R^2)M_Z \sqrt{s} \cos\phi_*}{128(x_L^2 + x_R^2)(f_L^2 + f_R^2)(s + M_Z^2)},$$

Define

$$\mathcal{O}_1 = \left| \sigma_1 \int d\phi_* f_{\phi_*}^1 \times \text{sign}(\cos\phi_*) \right| = \mathcal{O}(s^{1/2}),$$

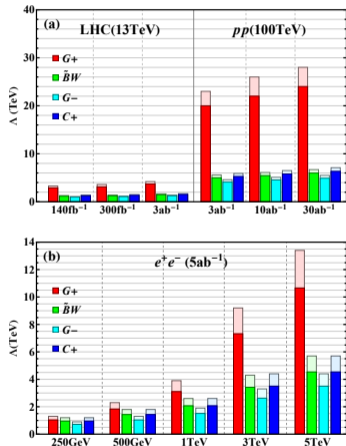
to get leading energy dependence of interference term.



$e^-e^+ \rightarrow Z\gamma \rightarrow d\bar{d}\gamma$  at CEPC

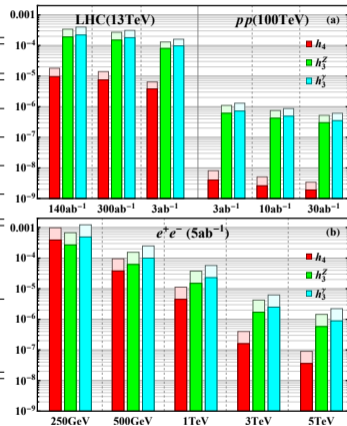
# Sensitivities of new physics scale (on-shell)

$\sqrt{s}$ (TeV)	$\mathcal{L}$ ( $\text{ab}^{-1}$ )	$\Lambda_{G+}$	$\Lambda_{G-}$	$\Lambda_{\tilde{B}W}$	$\Lambda_{C+}$
$e^+e^-$ (0.25)	5	(1.3, 1.6)	(0.90, 1.2)	(1.2, 1.3)	(1.2, 1.6)
$e^+e^-$ (0.5)	5	(2.3, 2.7)	(1.4, 1.7)	(1.8, 1.9)	(1.8, 2.2)
$e^+e^-$ (1)	5	(3.9, 4.7)	(1.9, 2.5)	(2.5, 2.6)	(2.6, 2.9)
$e^+e^-$ (3)	5	(9.2, 11.0)	(3.4, 4.3)	(4.3, 4.5)	(4.4, 5.2)
$e^+e^-$ (5)	5	(13.4, 15.9)	(4.4, 5.6)	(5.7, 5.9)	(5.7, 6.8)
LHC(13)	0.14	3.3	1.1	1.3	1.4
	0.3	3.6	1.2	1.4	1.5
	3	4.2	1.4	1.7	1.7
$pp$ (100)	3	23	4.6	5.6	5.9
	10	26	5.1	6.1	6.5
	30	28	5.5	6.7	7.1



# Sensitivities of form factors (on-shell)

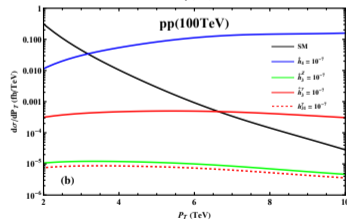
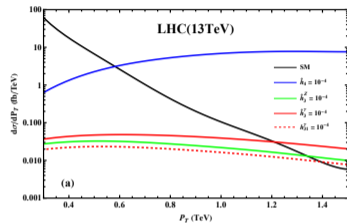
$\sqrt{s}$ (TeV)	$\mathcal{L}$ ( $\text{ab}^{-1}$ )	$ h_4 $	$ h_3^Z $	$ h_3^{\gamma} $
$e^+e^-$ (0.25)	5	$(3.9, 2.0) \times 10^{-4}$	$(2.7, 2.3) \times 10^{-4}$	$(4.9, 1.6) \times 10^{-4}$
$e^+e^-$ (0.5)	5	$(3.8, 1.9) \times 10^{-5}$	$(6.2, 5.2) \times 10^{-5}$	$(10, 3.7) \times 10^{-5}$
$e^+e^-$ (1)	5	$(4.5, 2.3) \times 10^{-6}$	$(1.5, 1.2) \times 10^{-5}$	$(2.3, 1.0) \times 10^{-5}$
$e^+e^-$ (3)	5	$(1.6, 0.84) \times 10^{-7}$	$(1.7, 1.4) \times 10^{-6}$	$(2.5, 1.0) \times 10^{-6}$
$e^+e^-$ (5)	5	$(3.6, 1.8) \times 10^{-8}$	$(5.8, 4.9) \times 10^{-7}$	$(8.9, 3.4) \times 10^{-7}$
LHC (13)	0.14	$9.6 \times 10^{-6}$	$1.9 \times 10^{-4}$	$2.2 \times 10^{-4}$
	0.3	$7.5 \times 10^{-6}$	$1.5 \times 10^{-4}$	$1.8 \times 10^{-4}$
	3	$3.8 \times 10^{-6}$	$0.80 \times 10^{-4}$	$0.97 \times 10^{-4}$
$pp$ (100)	3	$4.0 \times 10^{-9}$	$6.1 \times 10^{-7}$	$7.2 \times 10^{-7}$
	10	$2.6 \times 10^{-9}$	$4.2 \times 10^{-7}$	$4.9 \times 10^{-7}$
	30	$1.9 \times 10^{-9}$	$3.0 \times 10^{-7}$	$3.5 \times 10^{-7}$



# Sensitivity reaches via $pp(q\bar{q}) \rightarrow Z^* \gamma \rightarrow \nu\bar{\nu}\gamma$

$\sqrt{s}$ $\mathcal{L}(\text{ab}^{-1})$	13 TeV			100 TeV			
	0.14	0.3	3	3	10	30	
$ h_{4,2}  \times 10^6$	11	8.5	4.2	$ h_{4,2}  \times 10^9$	4.5	2.9	2.0
$ h_{3,1}^Z  \times 10^4$	2.2	1.7	0.90	$ h_{3,1}^Z  \times 10^7$	7.0	4.8	3.4
$ h_{3,1}^Y  \times 10^4$	1.6	1.3	0.67	$ h_{3,1}^Y  \times 10^7$	0.94	0.62	0.44
$ h_{31,11}^Y  \times 10^4$	2.5	2.0	1.0	$ h_{31,11}^Y  \times 10^7$	8.3	5.7	4.0

$\sqrt{s}$ $\mathcal{L}(\text{ab}^{-1})$	13 TeV			100 TeV		
	0.14	0.3	3	3	10	30
$\Lambda_{G+}$	3.2	3.5	4.1	23	25	28
$\Lambda_{G-}$	1.2	1.3	1.5	7.7	8.5	9.3
$\Lambda_{\tilde{B}W}$	1.3	1.4	1.6	5.4	5.9	6.4
$\Lambda_{\tilde{B}\tilde{W}}$	1.5	1.6	1.8	6.2	6.8	7.4
$\Lambda_{\tilde{G}+}$	2.7	2.9	3.5	19	21	23
$\Lambda_{\tilde{G}-}$	1.0	1.1	1.3	6.5	7.2	7.8
$\Lambda_{WW}$	0.93	1.0	1.2	3.9	4.3	4.6
$\Lambda_{WB}$	1.1	1.2	1.4	4.6	5.1	5.5
$\Lambda_{BB}$	1.3	1.4	1.7	5.6	6.2	6.8



- nTGCs provide unique probe of dimension-8 SMEFT operators
- We propose new nTGC form factor formalism which match Dimension-8 SMEFT  
Conventional nTGC form factor formalism disregards  $SU(2) \times U(1)$  of SM  
Off-shell effects modify experimental sensitivities significantly  
ATLAS and CMS are redoing the analysis
- Sensitivity in 3-4TeV range at LHC
- Sensitivity can reach 1TeV at CEPC
- Sensitivity can reach  $\mathcal{O}(20 - 30)$ TeV at SPPC





# CP-conserving Dimension-8 nTGC operators

We propose the pure gauge operators of dimension-8 ( $\mathcal{O}_{G+}, \mathcal{O}_{G-}$ ) that contribute to nTGCs and are independent of the dimension-8 operator involving the Higgs doublet.

$$g\mathcal{O}_{G+} = \tilde{B}_{\mu\nu} W^{a\mu\rho} (D_\rho D_\lambda W^{a\nu\lambda} + D^\nu D^\lambda W_{\lambda\rho}^a),$$

$$g\mathcal{O}_{G-} = \tilde{B}_{\mu\nu} W^{a\mu\rho} (D_\rho D_\lambda W^{a\nu\lambda} - D^\nu D^\lambda W_{\lambda\rho}^a),$$

$$\mathcal{O}_{\tilde{B}W} = iH^\dagger \tilde{B}_{\mu\nu} W^{H\rho} \{D_\rho, D^\nu\} H + \text{h.c.},$$

$$\mathcal{O}_{C+} = \tilde{B}_{\mu\nu} W^{a\mu\rho} \left[ D_\rho (\bar{\Psi}_L T^a \gamma^\nu \Psi_L) + D^\nu (\bar{\Psi}_L T^a \gamma_\rho \Psi_L) \right],$$

$$\mathcal{O}_{C-} = \tilde{B}_{\mu\nu} W^{a\mu\rho} \left[ D_\rho (\bar{\Psi}_L T^a \gamma^\nu \Psi_L) - D^\nu (\bar{\Psi}_L T^a \gamma_\rho \Psi_L) \right].$$

$\mathcal{O}_{C+}$  and  $\mathcal{O}_{C-}$  are connected to  $(\mathcal{O}_{G+}, \mathcal{O}_{G-}, \mathcal{O}_{\tilde{B}W})$  by the equation of motion:  $D^\nu W_{\mu\nu}^a = ig \left[ H^\dagger T^a D_\mu H - (D_\mu H)^\dagger T^a H \right] + g \bar{\Psi}_L T^a \gamma_\mu \Psi_L$

$$\mathcal{O}_{C+} = \mathcal{O}_{G-} - \mathcal{O}_{\tilde{B}W},$$

$$\mathcal{O}_{C-} = \mathcal{O}_{G+} - \{ iH^\dagger \tilde{B}_{\mu\nu} W^{H\rho} [D_\rho, D^\nu] H + i2(D_\rho H)^\dagger \tilde{B}_{\mu\nu} W^{H\rho} D^\nu H + \text{h.c.} \}.$$

Left side and right side have the same contribution to  $\psi\bar{\psi} \rightarrow Z\gamma$

3 independent nTGC operators

Only  $\Psi_L$  in  $\mathcal{O}_{C-} \rightarrow \mathcal{O}_{G+}$  can not contribute to  $\psi_R \bar{\psi}_R \rightarrow Z\gamma$

# Unitary Bounds

$$\Lambda_{G^+} > \frac{\sqrt{s}}{(24\sqrt{2}\pi)^{1/4}} \simeq 0.311\sqrt{s},$$

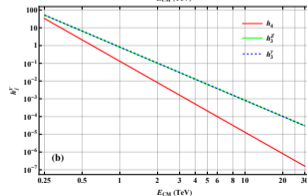
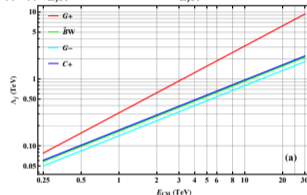
$$\Lambda_j > \left(\frac{c'_{L,R}M_Z}{12\sqrt{2}\pi}\right)^{1/4} (\sqrt{s})^{3/4} \simeq 0.203 (c'_{L,R})^{1/4} (\text{TeV}\sqrt{s^3})^{1/4},$$

$$|h_4| < \frac{24\sqrt{2}\pi v^2 M_Z^2}{s_W c_W s^2} \simeq \left(\frac{0.597 \text{ TeV}}{\sqrt{s}}\right)^4,$$

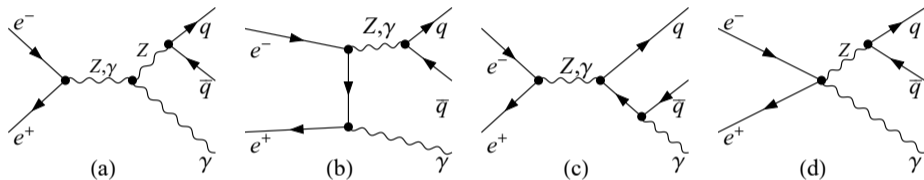
$$|h_3^V| < \frac{6\sqrt{2}\pi r_3^V}{s_W c_W c'_{L,R}} \frac{v^2 M_Z}{\sqrt{s^3}} \simeq \frac{0.350 r_3^V}{c'_{L,R}} \left(\frac{\text{TeV}}{\sqrt{s}}\right)^3,$$

$\sqrt{s}$ (TeV)	0.25	0.5	1	3	5	23
$\Lambda_{G^+}$ (TeV)	0.078	0.16	0.31	0.93	1.6	7.2
$\Lambda_{\tilde{B}W}$ (TeV)	0.058	0.098	0.16	0.37	0.55	1.7
$\Lambda_{G^-}$ (TeV)	0.050	0.084	0.14	0.32	0.47	1.5
$\Lambda_{C^+}$ (TeV)	0.060	0.10	0.17	0.39	0.57	1.8
$ h_4 $	33	2.1	0.13	0.0016	$2.1 \times 10^{-4}$	$4.6 \times 10^{-7}$
$ h_3^Z $	53	6.6	0.83	0.031	$6.7 \times 10^{-3}$	$6.8 \times 10^{-5}$
$ h_3^\gamma $	54	6.7	0.84	0.031	$6.7 \times 10^{-3}$	$6.9 \times 10^{-5}$

Unitary bounds ( $f\bar{f} \rightarrow Z\gamma$ ) are much weaker than our sensitivity bounds!



$$e^-e^+ \rightarrow q\bar{q}\gamma$$



- (a) nTGC s channel  $Z\gamma$
- (b) SM t and u channel  $Z\gamma$
- (c) Reducible SM backgrounds
- (d)  $\mathcal{O}_{C+}, \mathcal{O}_{C-}$  contribution

Diagrams of  $q\bar{q} \rightarrow l^-l^+\gamma$  have the same structure

# Sensitivity reaches at Lepton colliders

$\sqrt{s}$	$\mathcal{L}$	$\Lambda_{G^+}^{\ell,2\sigma}$	$\Lambda_{G^+}^{\ell,5\sigma}$	$\Lambda_{BW}^{\ell,2\sigma}$	$\Lambda_{BW}^{\ell,5\sigma}$
(energy)	( $\text{ab}^{-1}$ )	(unpol, pol)	(unpol, pol)	(unpol, pol)	(unpol, pol)
250 GeV	2	(0.93, 1.1)	(0.74, 0.87)	(0.56, 0.65)	(0.44, 0.51)
	5	(1.0, 1.2)	(0.83, 0.97)	(0.63, 0.73)	(0.49, 0.57)
500 GeV	2	(1.7, 2.0)	(1.3, 1.5)	(0.8, 1.0)	(0.64, 0.78)
	5	(1.9, 2.2)	(1.4, 1.7)	(0.90, 1.1)	(0.72, 0.87)
1 TeV	2	(2.8, 3.3)	(2.3, 2.7)	(1.2, 1.4)	(0.91, 1.1)
	5	(3.1, 3.7)	(2.6, 3.0)	(1.3, 1.6)	(1.0, 1.2)
3 TeV	2	(6.5, 7.7)	(5.1, 6.0)	(2.0, 2.5)	(1.6, 2.0)
	5	(7.3, 8.6)	(5.7, 6.7)	(2.2, 2.8)	(1.8, 2.2)
5 TeV	2	(9.5, 11.2)	(7.5, 8.8)	(2.6, 3.2)	(2.0, 2.6)
	5	(10.6, 12.5)	(8.4, 9.9)	(2.9, 3.6)	(2.2, 2.9)

$$e^-e^+ \rightarrow Z\gamma \rightarrow l^-l^+\gamma$$

$\sqrt{s}$	$\Lambda_{G^+}^{2\sigma}$	$\Lambda_{G^+}^{5\sigma}$	$\Lambda_{G^-}^{2\sigma}$	$\Lambda_{G^-}^{5\sigma}$	$\Lambda_{BW}^{2\sigma}$	$\Lambda_{BW}^{5\sigma}$	$\Lambda_{C^+}^{2\sigma}$	$\Lambda_{C^+}^{5\sigma}$
0.25	(1.3, 1.6)	(1.0, 1.2)	(0.9, 1.1)	(0.72, 0.89)	(1.2, 1.3)	(0.97, 1.0)	(1.2, 1.6)	(0.97, 1.2)
0.5	(2.3, 2.7)	(1.9, 2.2)	(1.3, 1.7)	(1.1, 1.3)	(1.8, 1.9)	(1.4, 1.4)	(1.8, 2.2)	(1.4, 1.7)
1	(3.9, 4.7)	(3.2, 3.7)	(1.9, 2.4)	(1.6, 1.9)	(2.6, 2.6)	(2.0, 2.1)	(2.6, 2.9)	(2.0, 2.4)
3	(9.2, 11.0)	(7.2, 8.6)	(3.3, 4.2)	(2.7, 3.3)	(4.3, 4.5)	(3.5, 3.6)	(4.4, 5.2)	(3.4, 4.1)
5	(13.4, 15.9)	(10.8, 12.7)	(4.4, 5.5)	(3.4, 4.4)	(5.7, 5.9)	(4.5, 4.7)	(5.7, 6.8)	(4.5, 5.5)

$$e^-e^+ \rightarrow Z\gamma \rightarrow q\bar{q}\gamma$$

The sensitivity limits on  $\Lambda$  are shown in pair inside the parentheses of each entry and correspond to the cases with (unpolarized, polarized)  $e^\mp$  beams, which are marked with (blue, red) colors. We choose a sample integrated luminosity  $\mathcal{L}=5\text{ab}^{-1}$  and the  $e^\mp$  beam polarizations  $(P_L^e, P_R^e) = (0.9, 0.65)$ .