

# Improving Heavy Dirac Neutrino Prospects at Future Hadron Colliders Using Machine Learning

**Jie Feng (冯劼)**  
**Sun Yat-Sen University**  
**(中山大学)**

In collaboration with Prof. Hong-Hao Zhang (张宏浩) from SYSU, Prof. Yong-Chao Zhang (张永超) from SEU,  
Prof. Qi-Shu Yan (晏启树) from UCAS and Dr. Yu-Pan Zeng (曾育盼) from GDOU

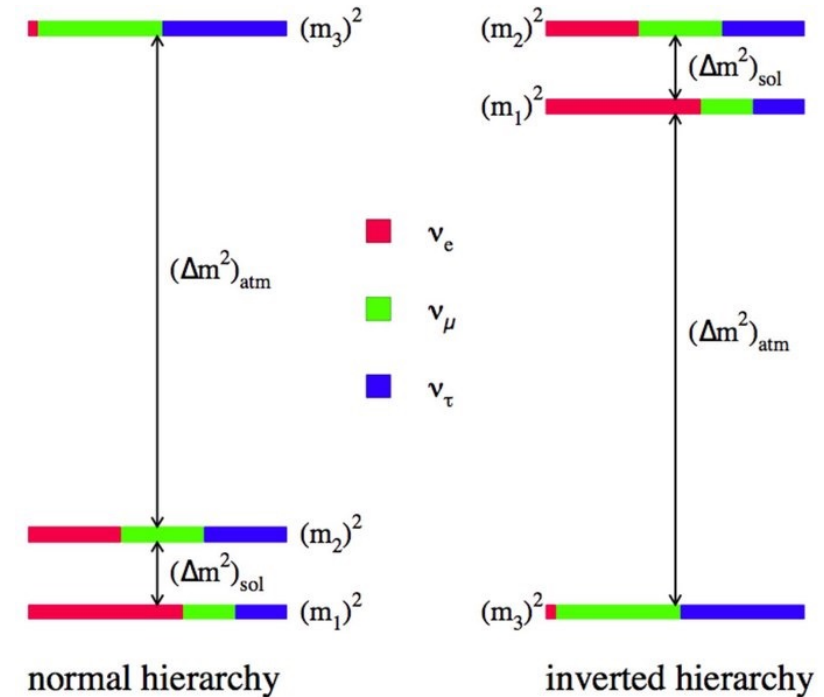
# Introduction

## ➤ Neutrino mass

- Confirmed by Neutrino Oscillation experiments (Super-Kamiokande, Sudbury, Daya Bay, ...)
- 3 neutrino mass states.

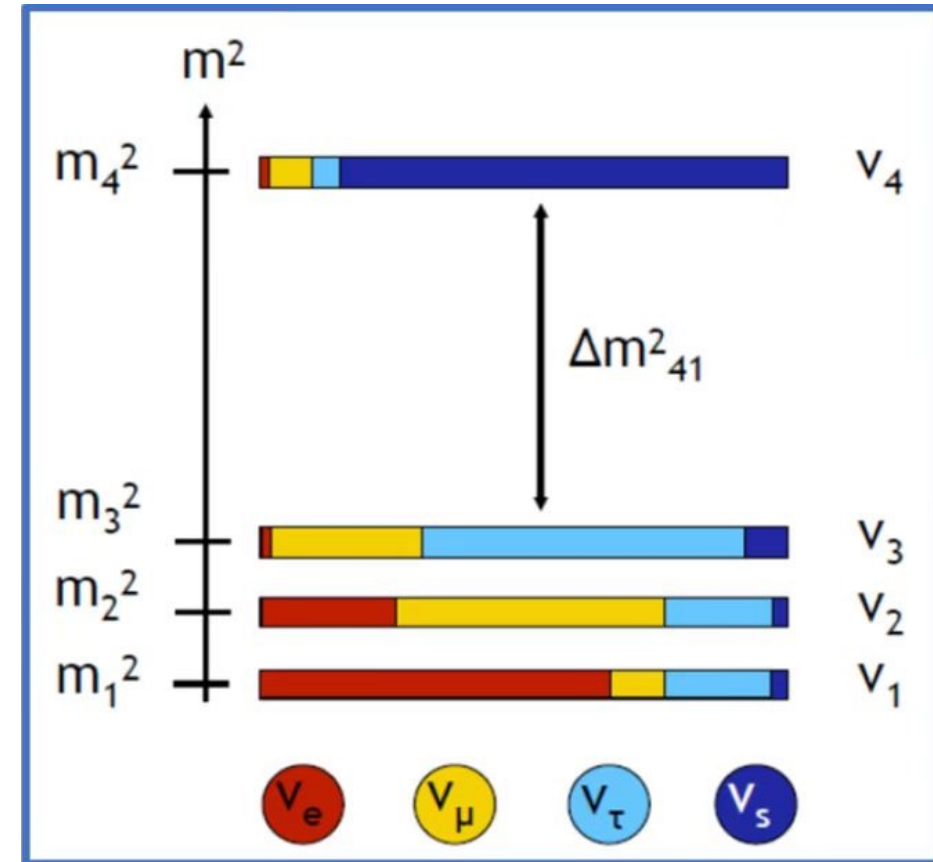
## ➤ In particle physics

- Beyond the Standard Model (SM) description
  - *New physics!*



# Introduction

- Seesaw mechanisms provide natural explanations of the tiny neutrino masses.
- Type-I : Prof. Tsutomu Yanagida
- Type-II : many others...
- Type-III: Prof. Xiao-Gang He



# Inverse seesaw

➤ The Yukawa Lagrangian is given by [1,2]

$$-\mathcal{L}_Y = Y_{\alpha\beta} \bar{L}_\alpha \Phi N_{R,\beta} + M_{N,\alpha\beta} \bar{S}_{L,\alpha} N_{R,\beta} + \frac{1}{2} \mu_{S,\alpha\beta} \bar{S}_{L,\alpha} S_{L,\beta}^C + \text{H. c.}$$

$L_\alpha = (\nu_\alpha, \ell_\alpha)^T$  - Standard Model lepton doublet

$\Phi$  - Standard Model Higgs doublet

$S_L^C \equiv S_L^T C^{-1}$  - charge conjugate of  $S_L$

$M_N$  - Dirac mass term

$\mu_S$  - Majorana mass term

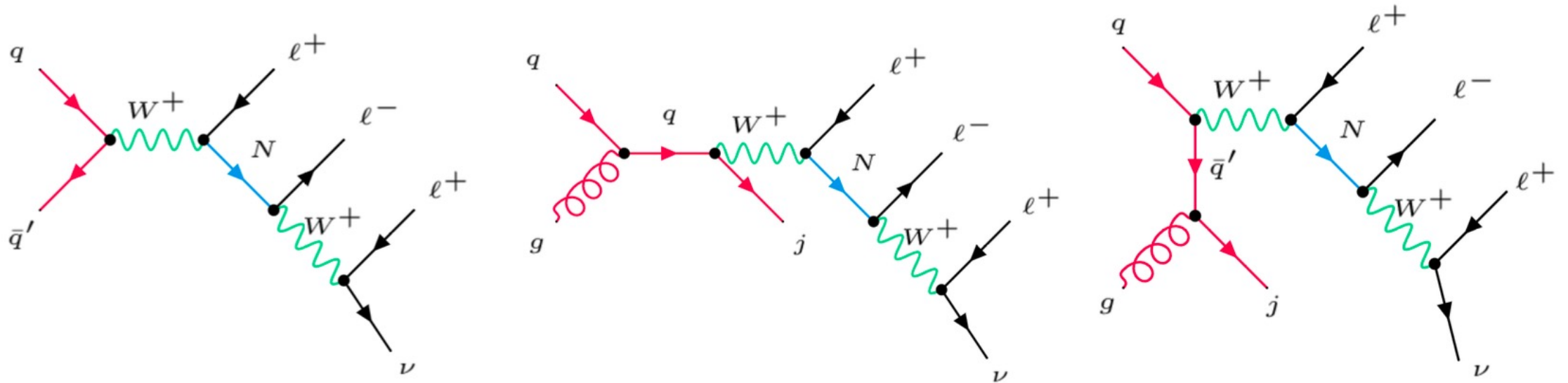
[1] R.N. Mohapatra, PRL 56 (1986) 561

[2] R.N. Mohapatra and J.W.F. Valle, PRD 34 (1986) 1642

# Inverse seesaw

➤ In the limit of  $\|\mu_S\| \ll \|M_N\|$  (with  $\|\mu_S\| \equiv \sqrt{\text{tr}(x^\dagger x)}$ ), the primary signature of heavy neutrinos at the hadron colliders are <sup>[3,4]</sup>:

$$pp \rightarrow \ell_\alpha^\pm N \rightarrow \ell_\alpha^\pm \ell_\beta^\mp W^\pm \rightarrow \ell_\alpha^\pm \ell_\beta^\mp \ell_\gamma^\pm \nu$$



[3] C. Degrande *et al.*, PRD 94 (2016) 053002 (arXiv:1602.06957)

[4] arXiv:1408.0983, 1706.02298

# Inverse seesaw

➤ The heavy neutrino  $N$  will decay [5,6]:

$$\Gamma(N \rightarrow \ell^- W^+) = \frac{\alpha_W |V_{\ell N}|^2}{16} \frac{m_N^3}{m_W^2} \left(1 - \frac{m_W^2}{m_N^2}\right)^2 \left(1 + \frac{m_W^2}{m_N^2}\right)$$

$$\Gamma(N \rightarrow \nu_\ell Z) = \frac{\alpha_W |V_{\ell N}|^2}{32 \cos^2 \theta_W} \frac{m_N^3}{m_Z^2} \left(1 - \frac{m_Z^2}{m_N^2}\right)^2 \left(1 + \frac{m_Z^2}{m_N^2}\right)$$

$$\Gamma(N \rightarrow \nu_\ell h) = \frac{\alpha_W |V_{\ell N}|^2}{32} \frac{m_N^3}{m_W^2} \left(1 - \frac{m_h^2}{m_N^2}\right)^2$$

[5] A. Pilaftsis, Z. Phys. C 55 (1992) 275

[6] W. Buchmuller and C. Greub, Nucl. Phys. B 363 (1991) 345

# Inverse seesaw

➤ The heavy neutrino  $N$  will decay [5,6]:

$$\Gamma(N \rightarrow \ell^- W^+) = \frac{\alpha_W |V_{\ell N}|^2}{16} \frac{m_N^3}{m_W^2} \left(1 - \frac{m_W^2}{m_N^2}\right)^2 \left(1 + \frac{m_W^2}{m_N^2}\right)$$

$$\Gamma(N \rightarrow \nu_\ell Z) = \frac{\alpha_W |V_{\ell N}|^2}{32 \cos^2 \theta_W} \frac{m_N^3}{m_Z^2} \left(1 - \frac{m_Z^2}{m_N^2}\right)^2 \left(1 + \frac{m_Z^2}{m_N^2}\right)$$

$$\Gamma(N \rightarrow \nu_\ell h) = \frac{\alpha_W |V_{\ell N}|^2}{32} \frac{m_N^3}{m_W^2} \left(1 - \frac{m_h^2}{m_N^2}\right)^2$$

[5] A. Pilaftsis, Z. Phys. C 55 (1992) 275

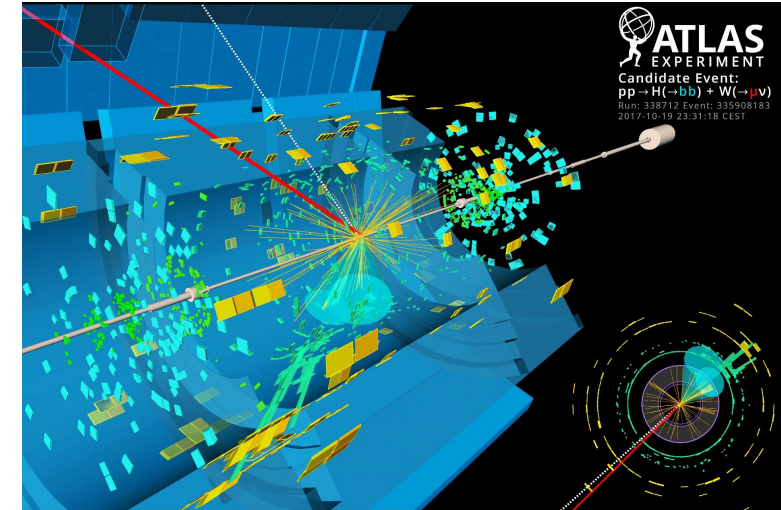
[6] W. Buchmuller and C. Greub, Nucl. Phys. B 363 (1991) 345

# Collider analysis – Signal generation

➤ The final states of the signature in the detector:  
electrons, muons, jets, ...

➤ Measurements of each particle in the detector:

- $p_T$  - transverse momentum
- $\eta$  - pseudorapidity
- $\phi$  - azimuthal angle



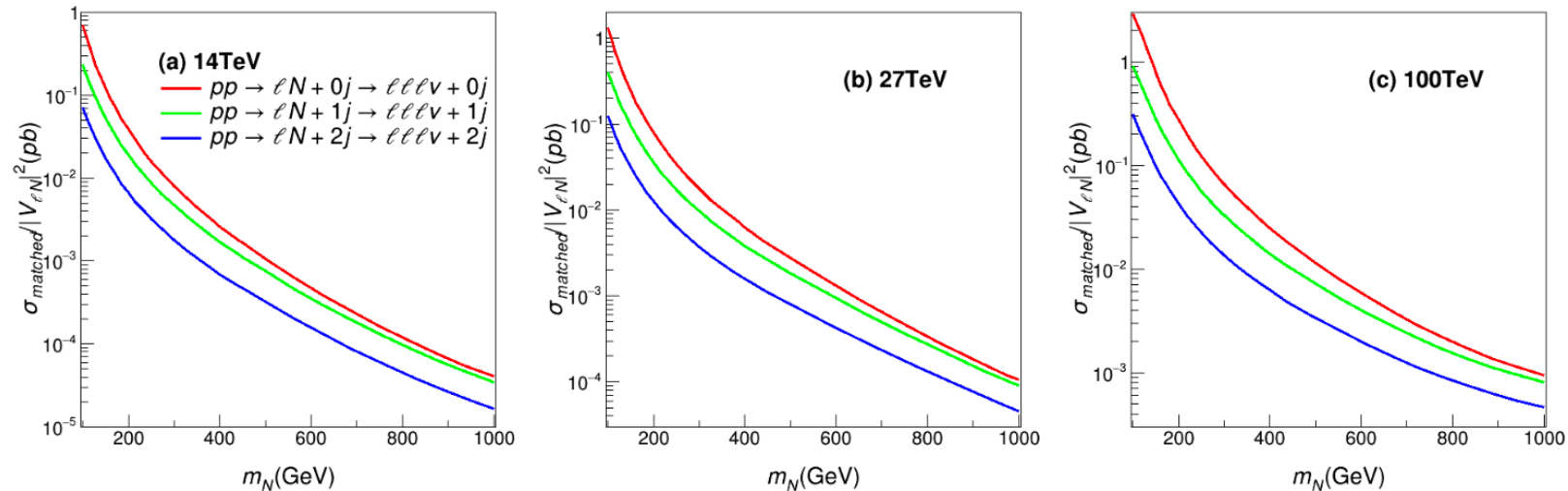
➤ Geometrical acceptance cuts from ATLAS:  $p_T^{\ell, \text{leading}} > 20 \text{ GeV}$

$\sqrt{s}$ (TeV)	electron		muon		jet	
	$p_T$ (GeV)	$ \eta $	$p_T$ (GeV)	$ \eta $	$p_T$ (GeV)	$ \eta $
14	>10	< 2.47	>10	< 2.7	> 20	< 4.5
27	>10	< 2.47	>10	< 2.7	> 30	< 4.5
100	>15	< 2.47	>15	< 2.7	> 45	< 4.5



# Collider analysis – Signal generation

## ➤ Cross sections of trilepton signal process



- Cross sections increase with higher center of mass energies.
- Cross sections with 2jets are much smaller than those with 1jet. It is safe to neglect events with higher jet multiplicity  $n_j \geq 3$ .

# Collider analysis – Signal generation

- Assuming either  $|V_{eN}| \neq 0$  or  $|V_{\mu N}| \neq 0$ , in the charge space, the three leptons of an event can be either  $+ - +$  or  $- + -$ . All the resultant trilepton states are

mixing	trilepton states	signs ( $\pm \mp \pm$ )
$V_{eN}$	$eee$	$e^\pm e^\mp e^\pm$
	$ee\mu$	$e^\pm e^\mp \mu^\pm$
$V_{\mu N}$	$\mu\mu e$	$\mu^\pm \mu^\mp e^\pm$
	$\mu\mu\mu$	$\mu^\pm \mu^\mp \mu^\pm$

# Collider analysis – background generation

➤ The main background:

$$pp \rightarrow ZW^\pm \rightarrow \ell_1^\pm \ell_2^\mp \ell_3^\pm \nu$$

➤ Pre-selection:

- The total number of energetic charged leptons is exactly 3, i.e.  $n_e + n_\mu = 3$ .
- The invariant mass of the two leading leptons should be larger than 12 GeV, i.e.  $m_{\ell_1 \ell_2} > 12 \text{ GeV}$ .
- The number of jets is not larger than 2, i.e.  $n_j \leq 2$ .
- The missing transverse momentum  $E_T^{\text{miss}} = | - \sum_{\nu_i} \vec{p}_T(\nu_i) |$  is larger than 20 GeV, i.e.  $E_T^{\text{miss}} > 20 \text{ GeV}$ .

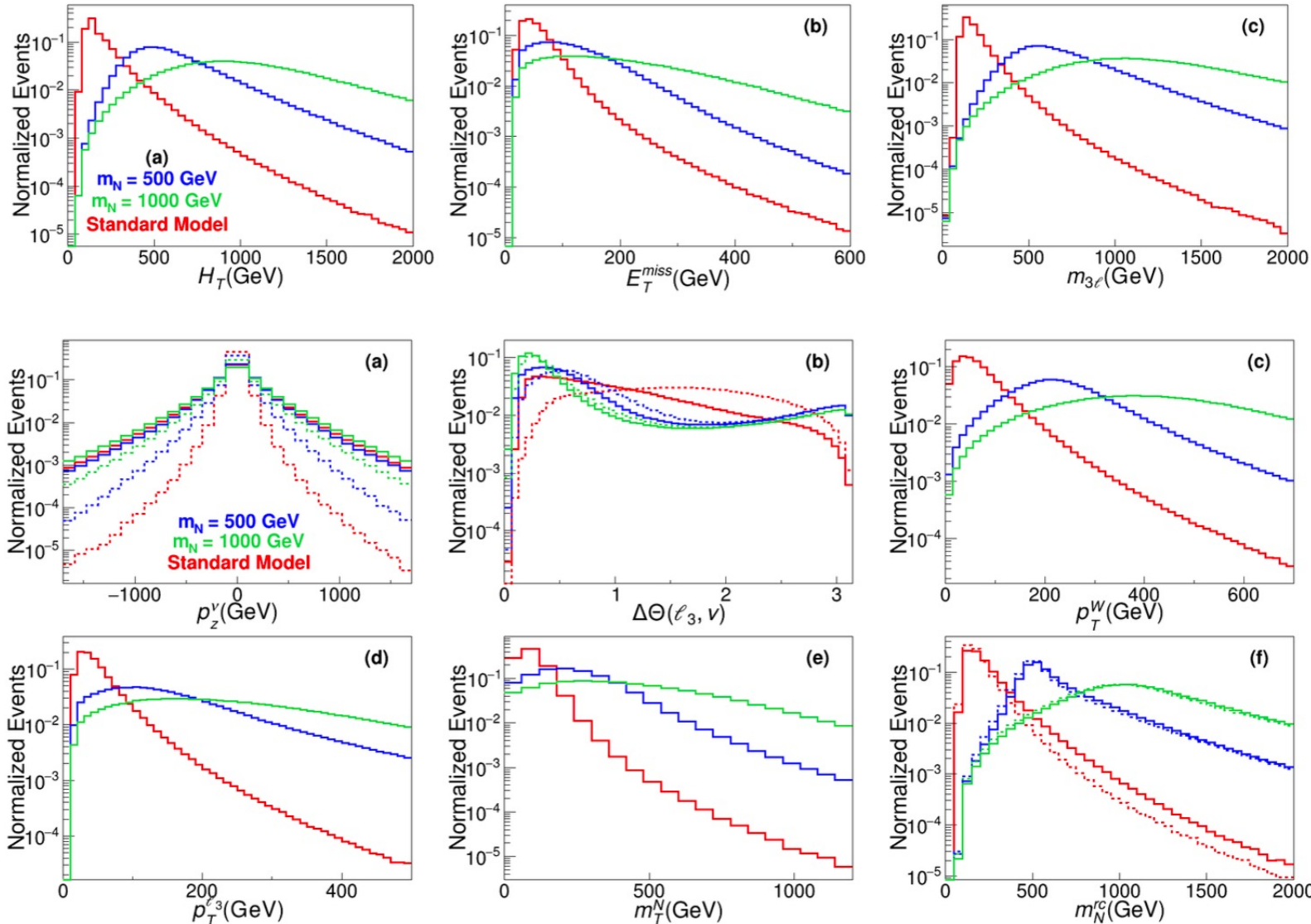
# Collider analysis – background generation

- Cross sections of all possible trilepton final state processes after pre-selections:

process	cross section (fb)	
	0-jet	1-jet
$ZW \rightarrow lll\nu$	29.10	20.50
$lll\nu$ (off-shell + interference)	1.65	0.84
$4l$	1.56	1.25

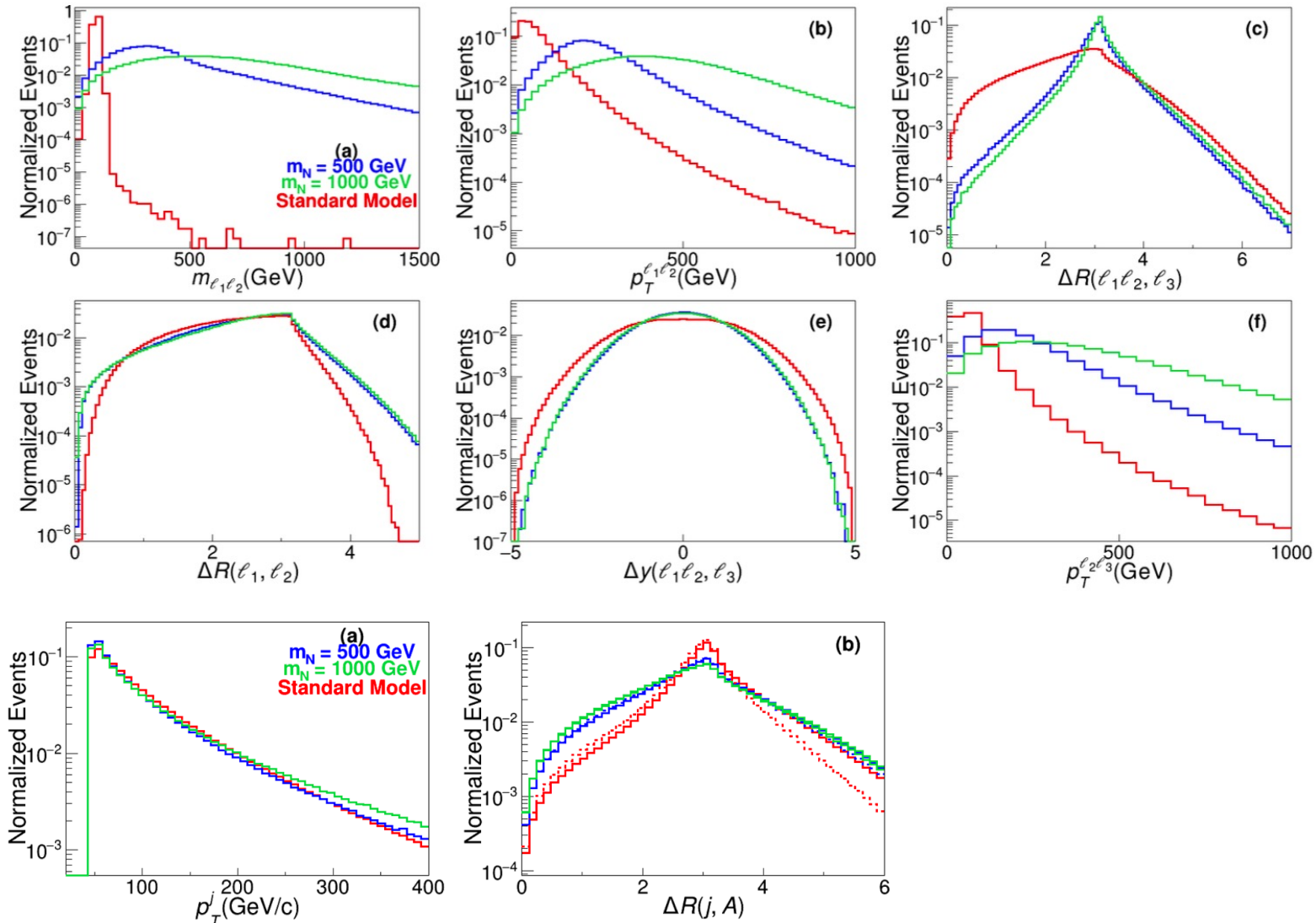
- The contributions of the off-shell and four-lepton processes to the standard model backgrounds are small. We can just scale the  $ZW$  background by 1.1 to take the other two into account.

# Collider analysis – Feature observables



Variables reconstructed from the 3-lepton measurements.

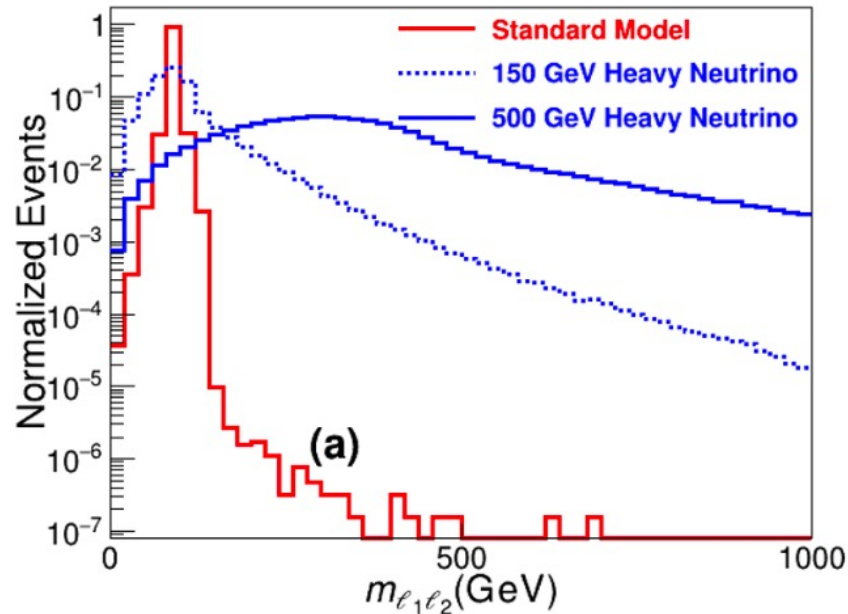
# Collider analysis – Feature observables



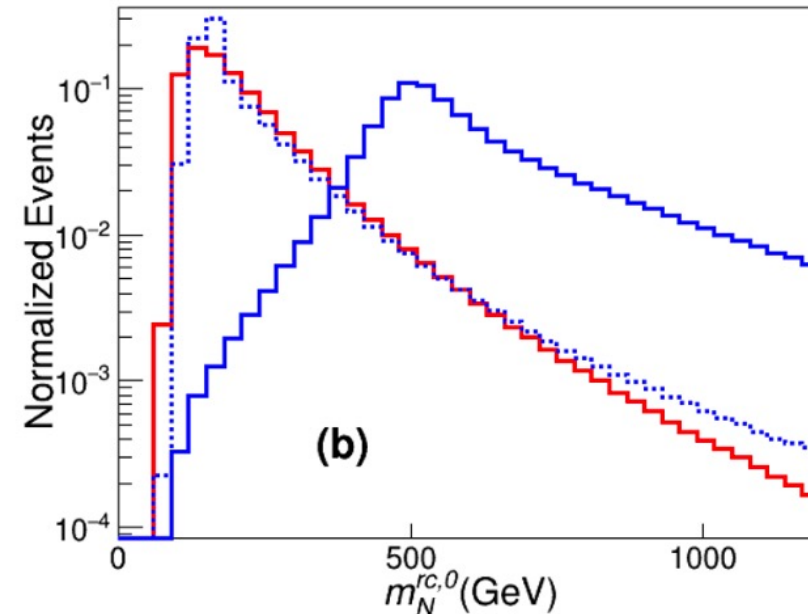
Variables reconstructed from the 3-lepton measurements.

# Collider analysis – Feature observables

- Variables with the largest separation power:



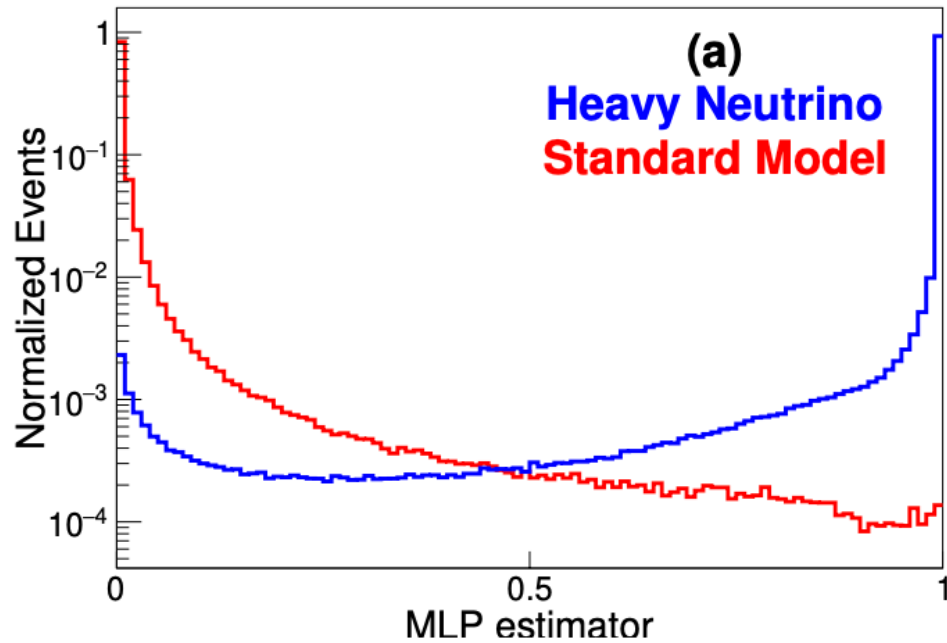
Z mass



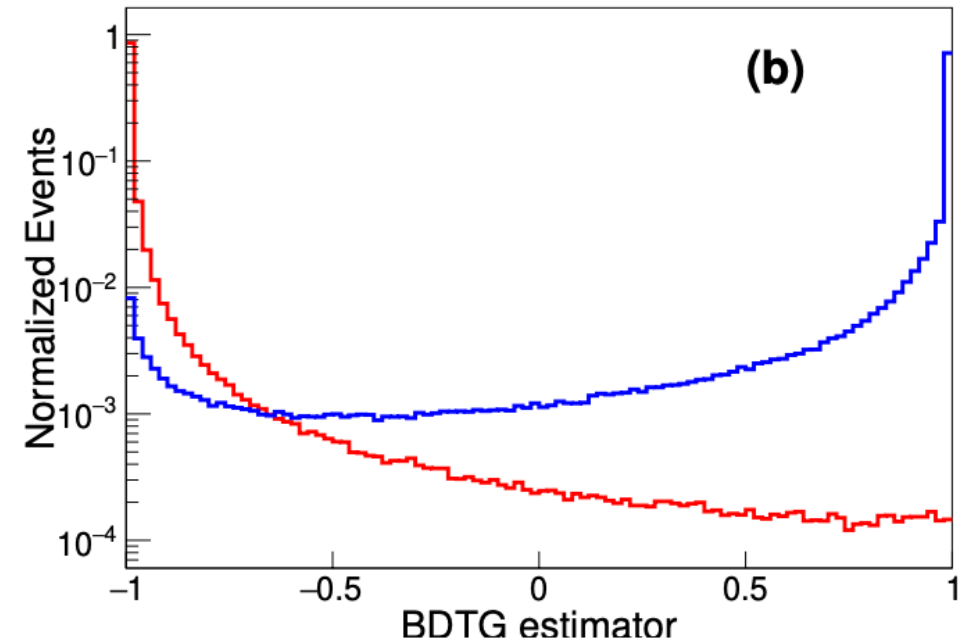
Heavy neutrino mass  
(calculated from W  
mass assumption)  $W^\pm \rightarrow \ell_\frac{3}{3}^\pm \nu$

# Collider analysis – Machine Learning (ML)

➤ The ML estimator distributions for  $m_N = 500$  GeV:



Multi-Layer Perceptron (MLP)

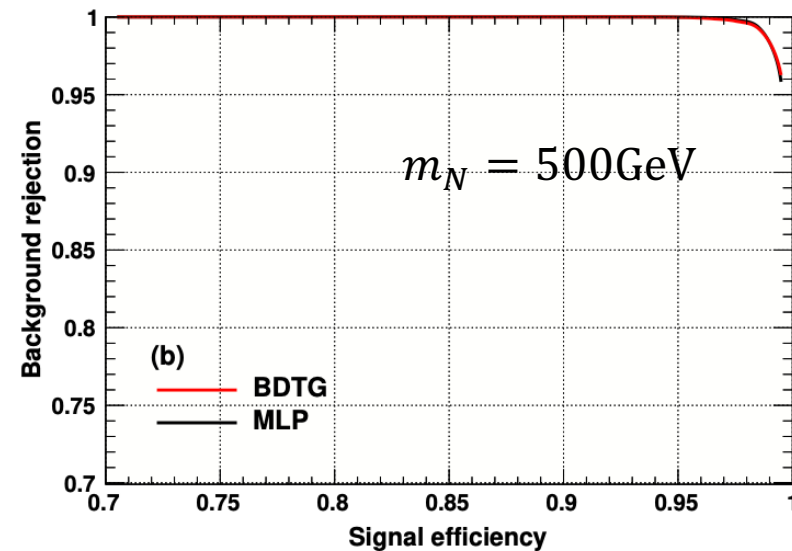
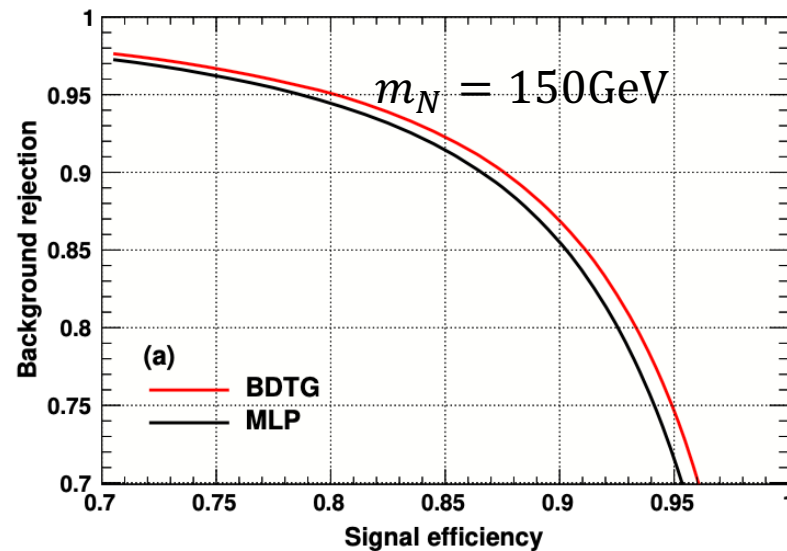


Boosted Decision Tree with Gradient boosting (BDTG)



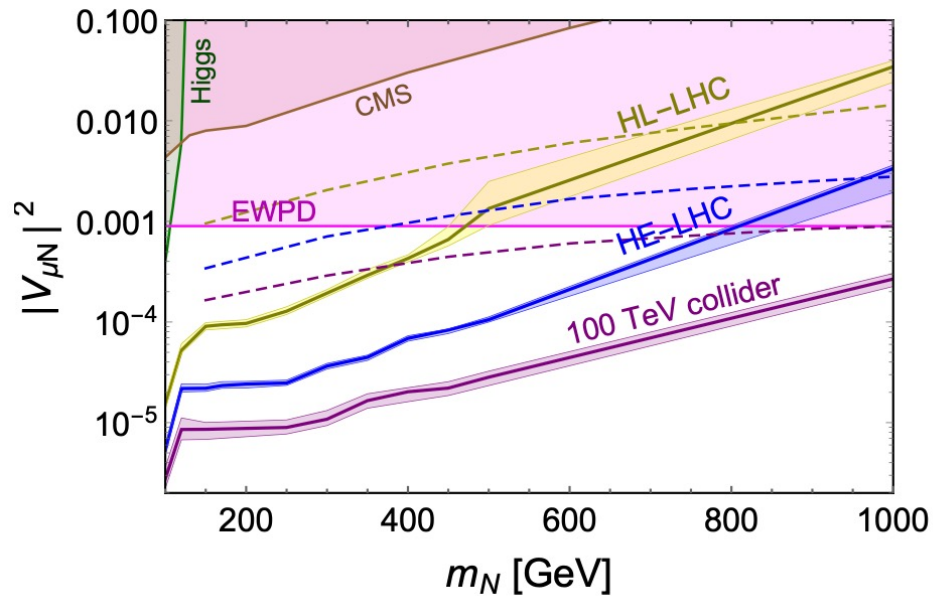
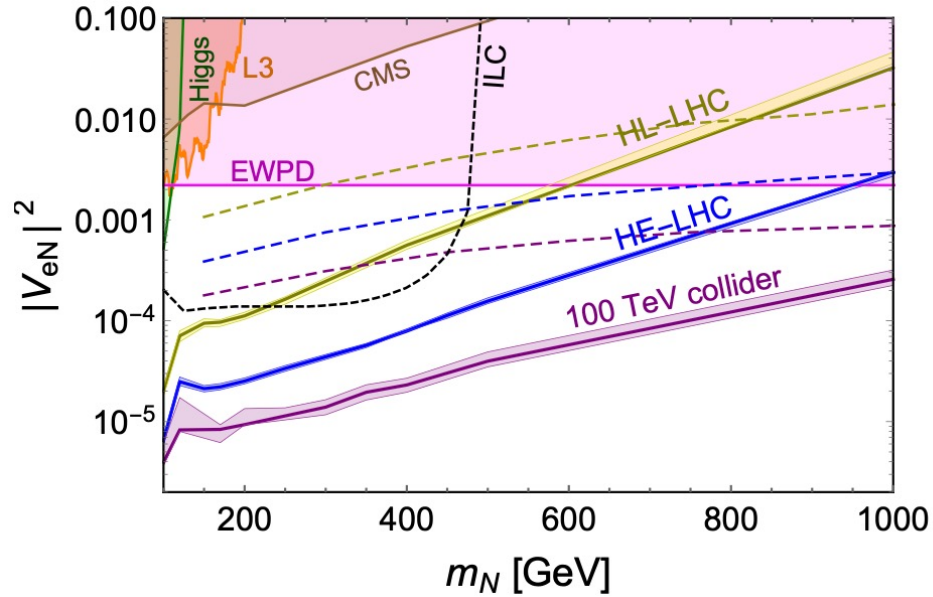
# Collider analysis – Machine Learning

- The signal efficiency and background rejection power:



- BDTG and MLP methods show compatible results.
- When the heavy neutrino mass goes to a higher value, the separation becomes better.

# Results



- Sensitivities of the heavy-light neutrino mixing  $|V_{eN}|^2$  (upper) and  $|V_{\mu N}|^2$  (lower) at 95% C.L. .
- With machine learning methods,  $|V_{lN}|^2$  can be improved up to  $O(10^{-6})$  for heavy neutrino mass  $m_N = 100$  GeV and  $O(10^{-4})$  for  $m_N = 1$  TeV.

$\sqrt{s} = 14$  TeV( $3ab^{-1}$ ),  $27$  TeV( $15ab^{-1}$ ), and  $100$  TeV( $30ab^{-1}$ )

# Summary

- By using the machine learning methods, we study the sensitivities of heavy pseudo-Dirac neutrino  $N$  in the inverse seesaw at the high-energy hadron colliders.
- We use either the Multi-Layer Perceptron or the Boosted Decision Tree with Gradient Boosting to analyze the kinematic observables and optimize the discrimination of background and signal events.
- It is found that the reconstructed  $Z$  boson mass and heavy neutrino mass play crucial roles in separating the signal from backgrounds.
- The prospects of heavy-light neutrino mixing  $|V_{lN}|^2$  (with  $l = e, \mu$ ) are estimated by using machine learning at the hadron colliders with  $\sqrt{s} = 14$  TeV, 27 TeV, and 100 TeV, and it is found that  $|V_{lN}|^2$  can be improved up to  $O(10^{-6})$  for heavy neutrino mass  $m_N = 100$  GeV and  $O(10^{-4})$  for  $m_N = 1$  TeV.

Thank you !