

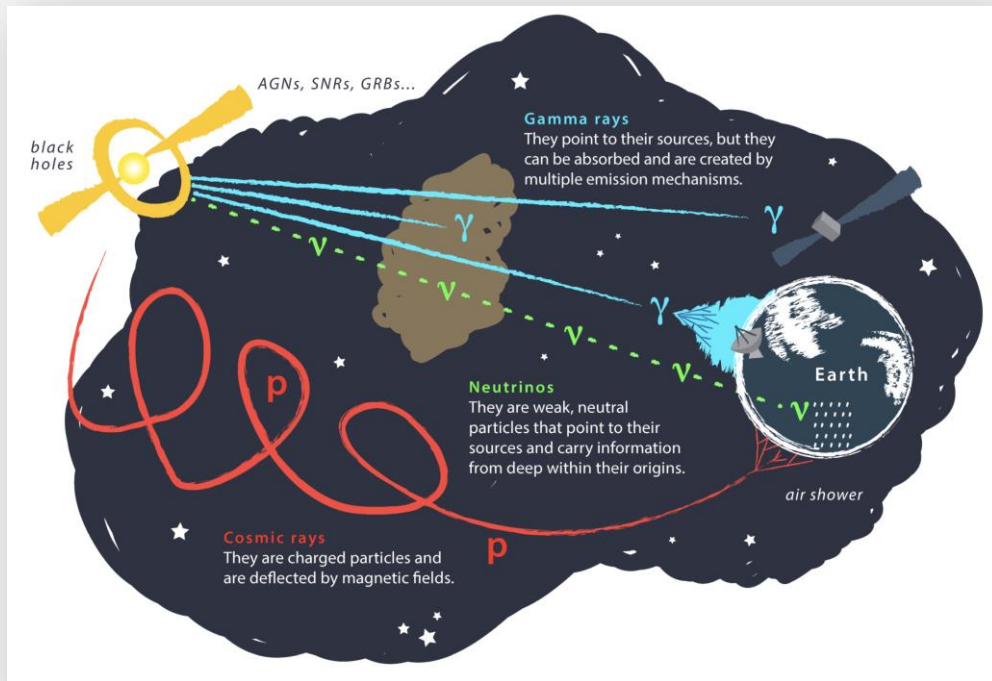
# Neutrino Reconstruction in TRIDENT Based on GNN

Cen Mo (莫岑)

for the TRIDENT collaboration

# Neutrino Telescope

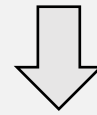
Probe origins of cosmic ray with **neutrino**.



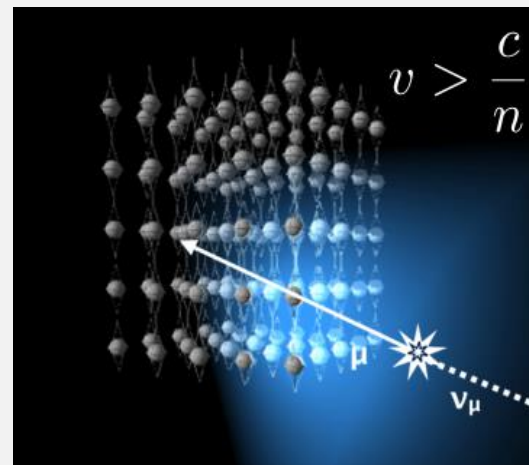
Juan Antonio Aguilar and Jamie Yang. IceCube/WIPAC

Astrophysical neutrino:

- Small flux  
 $E_\nu \Phi_\nu < 2 \times 10^{-8} \text{ GeV cm}^{-2} \text{ s}^{-2} \text{ sr}^{-1}$
- Small cross section  
 $\sigma \sim 10^{-33} \text{ cm}^2$  for  $E_\nu \sim 10 \text{ PeV}$



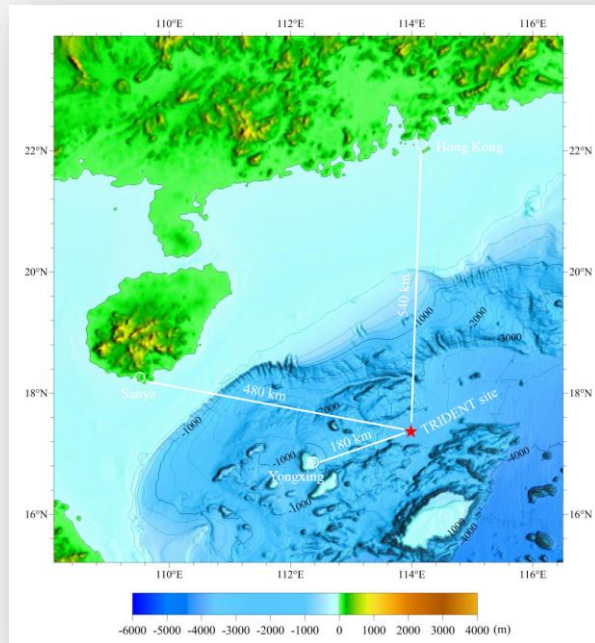
Use **sea water** as target



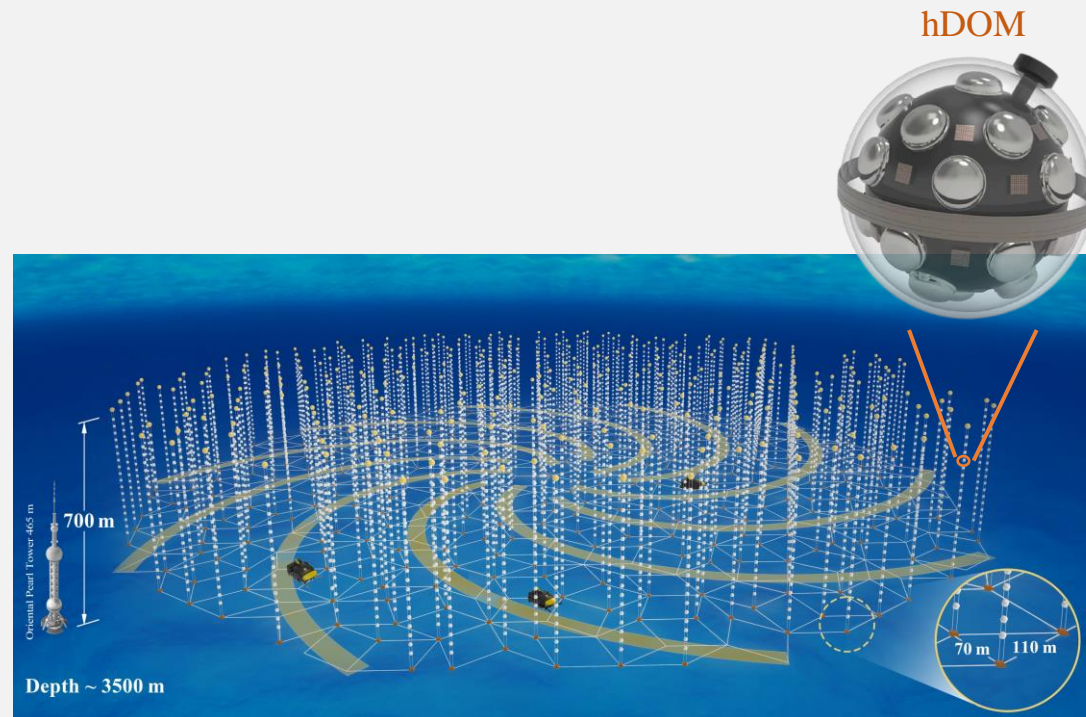
- Neutral-current interaction  
 $\nu_l + N \rightarrow \nu_l + X$
- Charged-current interaction  
 $\nu_l + N \rightarrow l + X$

# TRIDENT

- **TRIDENT**: TRopical DEep-sea Neutrino Telescope. [arXiv:2207.04519](https://arxiv.org/abs/2207.04519)
- To be located in the South China Sea.
- Penrose tiling structure with 2000m radius, 700m height, 3500m deep under sea level.



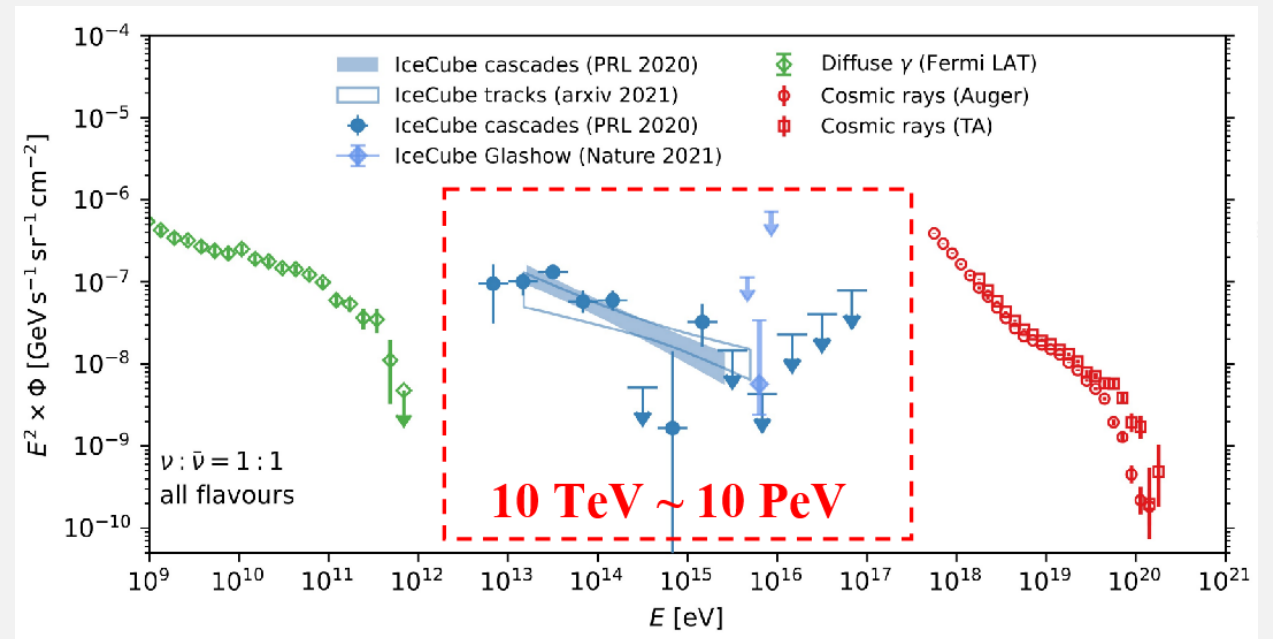
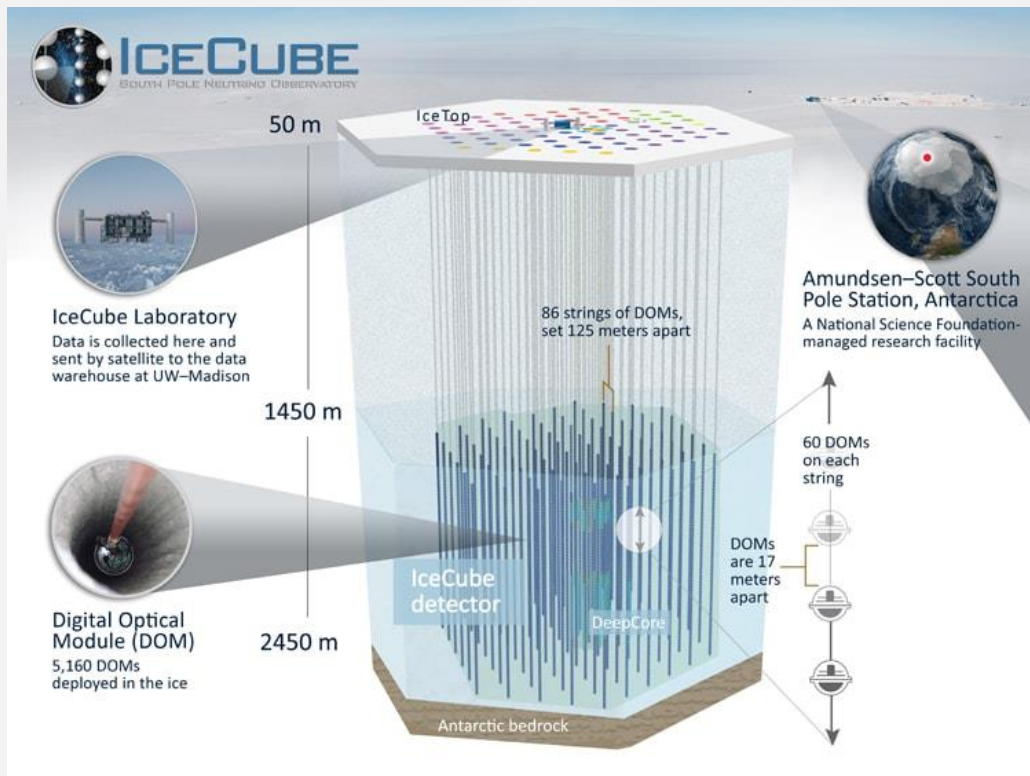
TRIDENT site



TRIDENT

# IceCube

- **The largest neutrino telescope.**
- Detected astrophysical neutrinos in 2013. [Science 342,1242856\(2013\)](https://doi.org/10.1126/science.1242856)

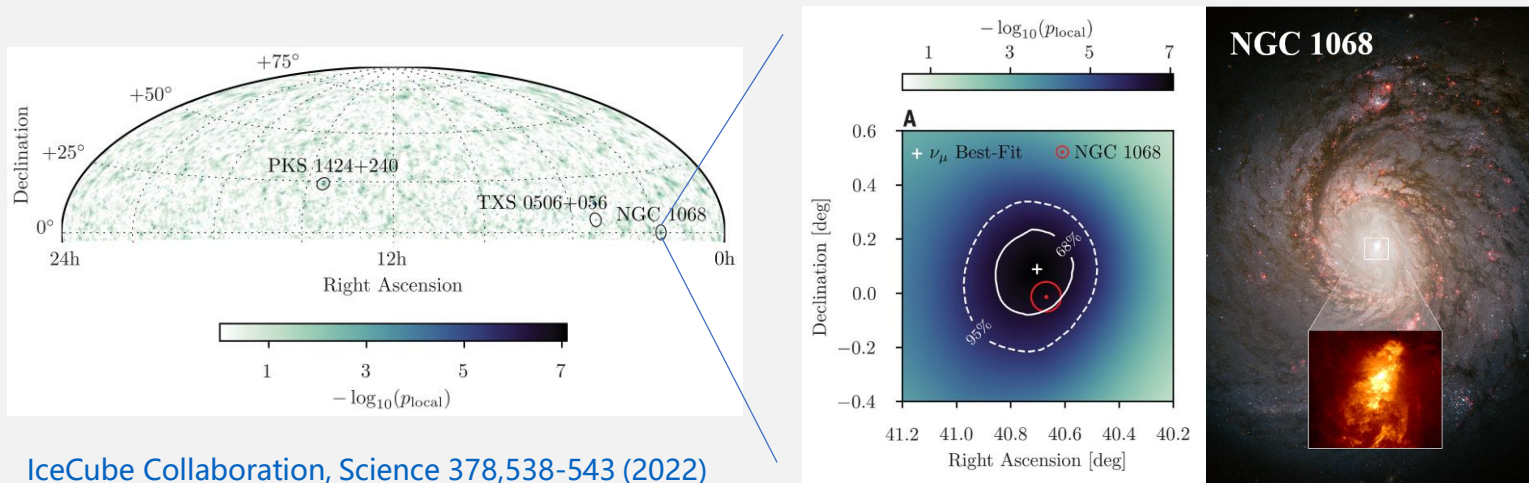


From Lu Lu, TeVPA, 2022

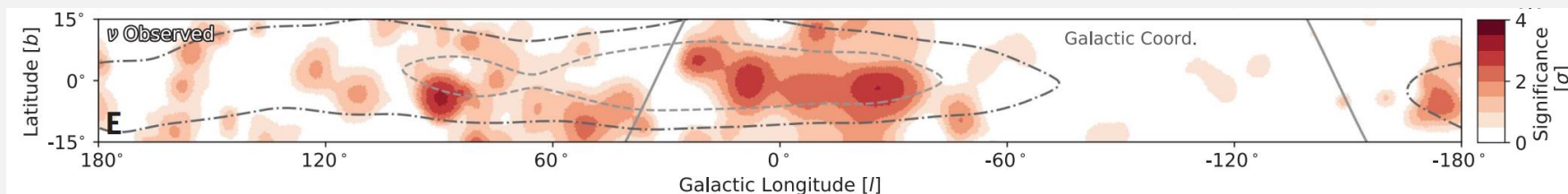


# Detection of Neutrino Sources

- Evidence for neutrino emission from the nearby active galaxy NGC 1068 (2022).

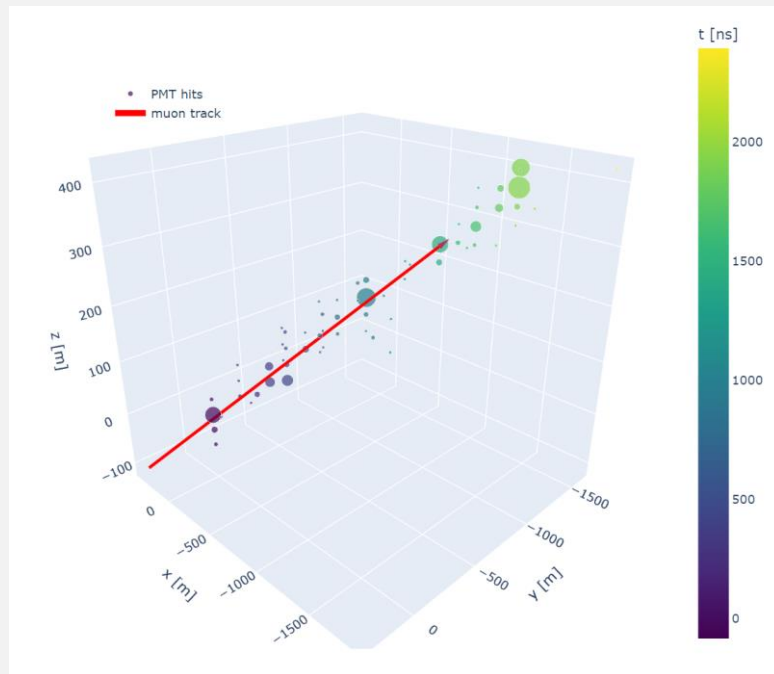


- Observation of high-energy neutrinos from the Galactic plane (2023)

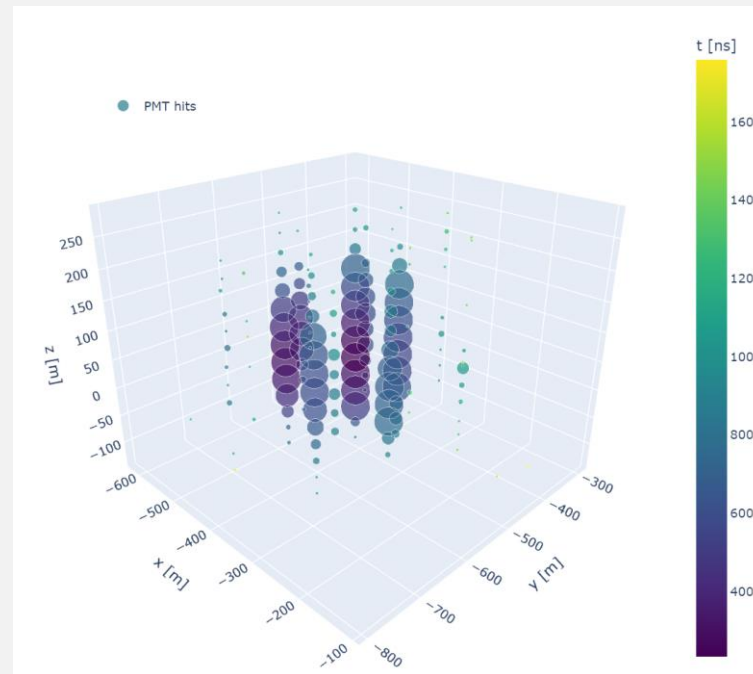
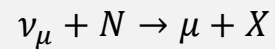


# Neutrino Events

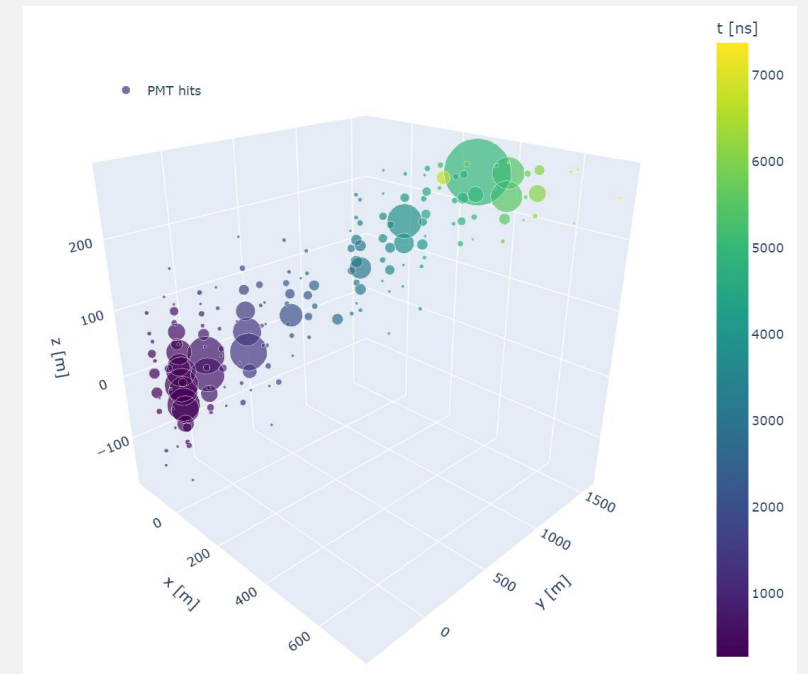
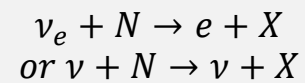
- Size of points: number of photo hits



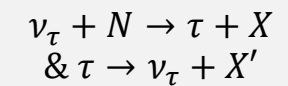
**Track**



**Cascade**



**Double bang**



# Simulation of Neutrino Events

## Neutrino event generator

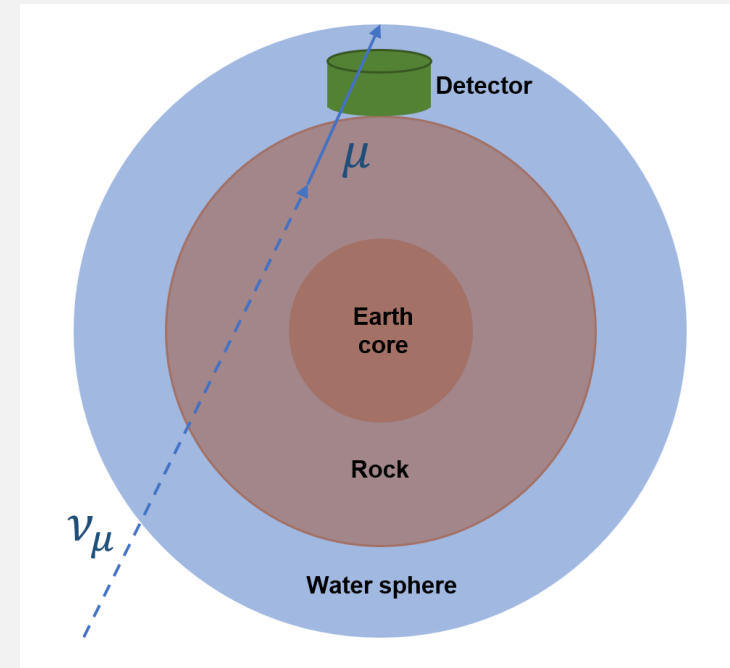
Based on CORSIKA8 ([arxiv:2208.14240](https://arxiv.org/abs/2208.14240)):

- A preliminary earth model is built.
- Scattering of  $\nu$  and  $p$  is simulated with PYTHIA8.
- Propagation of  $\mu$  is simulated with PROPOSAL.

## Detector simulation

Based on Geant4:

- Simulate the propagation of secondary particles.
- Accelerate Cherenkov photons simulation with [OptiX](#).



Preliminary earth model

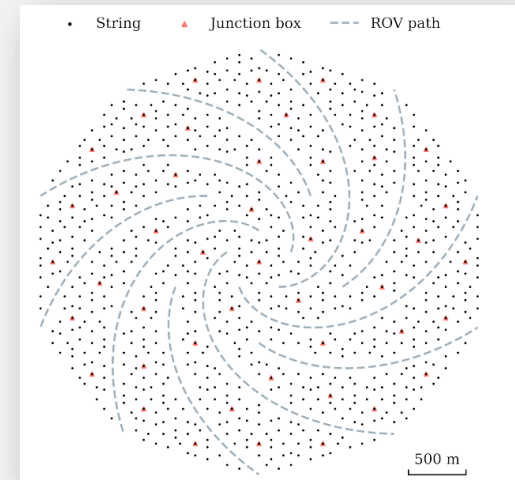
# Neural Network in Neutrino Telescope

## Neutrino telescope:

- Irregular detector geometry
- Sparse signal

Compared GNN and SSCNN ([arxiv:1706.01307](https://arxiv.org/abs/1706.01307)) performance:

- GNN **outperforms** SSCNN in terms of angular resolution in track-like events.



Top view of TRIDENT detectors

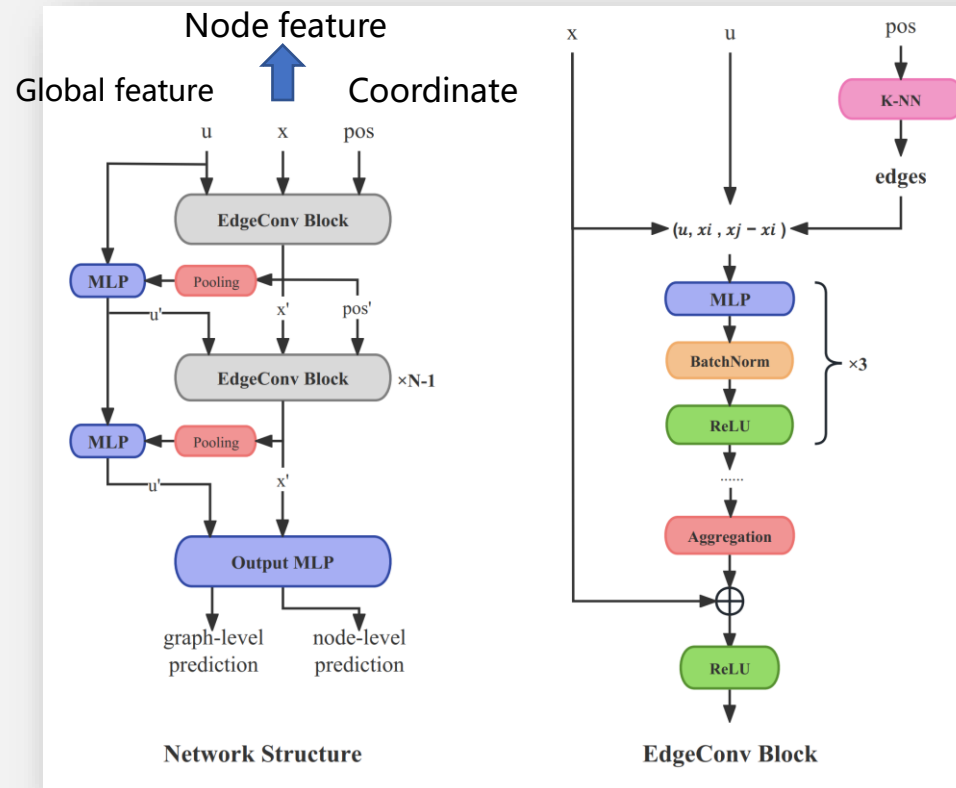
Use **point cloud** to represent neutrino events:

- Triggered DOMs → **Nodes** of point cloud
- Spacetime of DOMs → Coordinate of nodes,  $pos_i$ .
- DOM-measured time and charge → Features of nodes,  $x_i$ .



# TridentNet

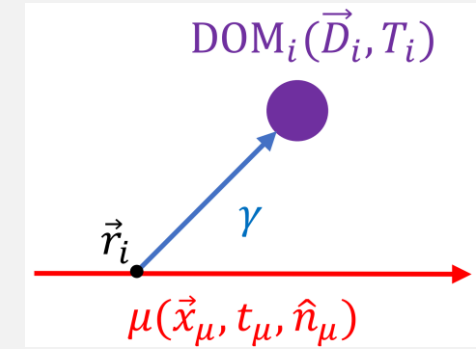
- TridentNet is built based on EdgeConv block: modified from EdgeConv block used in ParticleNet ([arxiv:1902.08570](https://arxiv.org/abs/1902.08570)).
- Both **graph-level** and **node-level** target can be predicted.



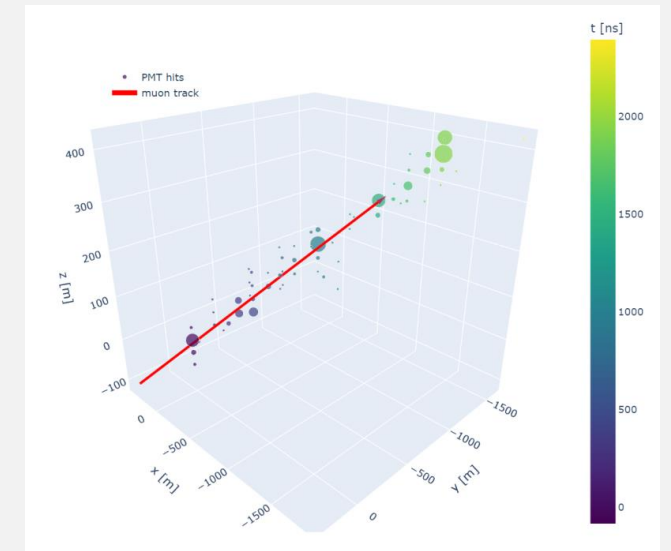
# Track-like Events Reconstruction

## Direction reconstruction

- **Input features:** location  $\vec{D}_i$ , first photon arrival time  $T_i$  and number of photo hits  $n_i$
- To make full use of the geometric feature of track-like events, the network is trained to predict  $\vec{r}_i$  for each  $\text{DOM}_i$ .
- **Loss function:** mean square error (MSE) with weight proportional to  $n_i$ :
 
$$\text{Loss} = \sum_i n_i \times \left| \overrightarrow{\text{output}_i} - \vec{r}_i \right|^2 / \sum_i n_i$$
- Linear fit on the predicted  $\vec{r}_i'$  then reconstructs  $\hat{n}_\mu$ .



$\mu$  emits photon and triggers  $\text{DOM}_i$

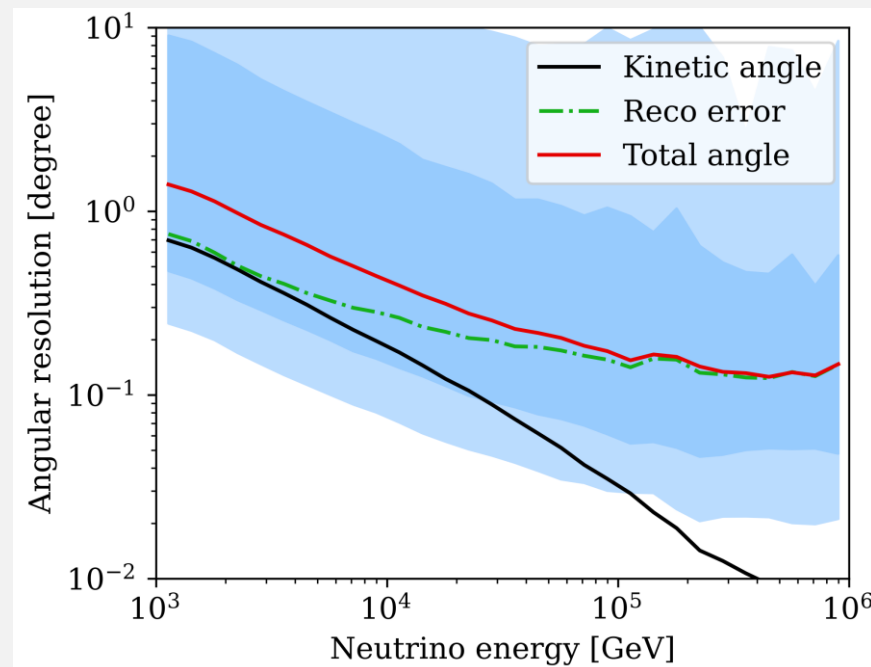


Track-like event display

# Track-like Events Reconstruction

## Direction reconstruction

- Model is trained on events with track length  $> 500\text{m}$ .
- Median angular error decreases from 1 degree to **0.1 degree** as the energy of  $\nu_\mu$  increases.



- Kinetic angle =  $\langle \vec{n}_\mu, \vec{n}_\nu \rangle$
- Reco error =  $\langle \vec{n}_\mu, \vec{n}_{recon} \rangle$
- Total angle =  $\langle \vec{n}_\nu, \vec{n}_{recon} \rangle$

# Track-like Events Reconstruction

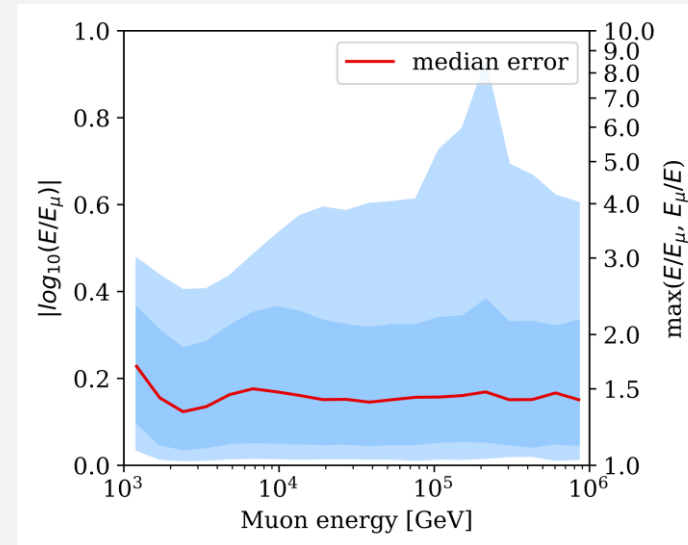
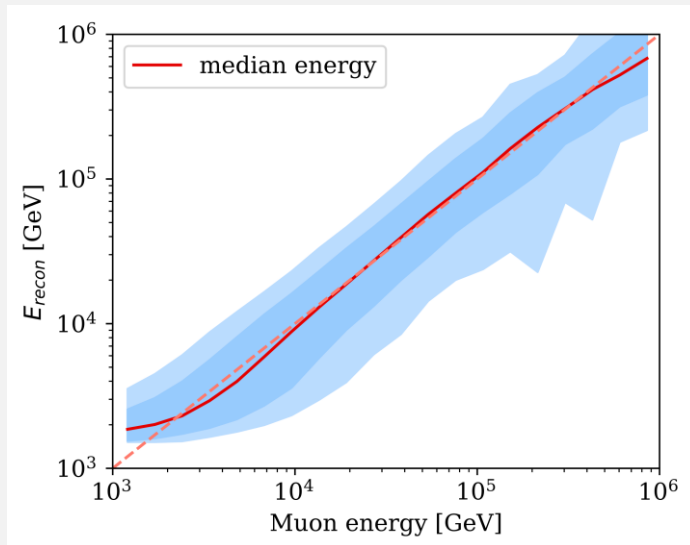
## Energy reconstruction

- Same input features as the direction reconstruction.
- Network is trained with **MSE loss** to predict  $\log_{10} E_{\mu}$ . Weight  $w = \log_{10} E_{\mu} - 2.5$  is applied:

$$Loss = w(\text{output} - \log_{10} E_{\mu})^2$$

- A shift term,  $b = 0.15$  is added to outputs of the model:

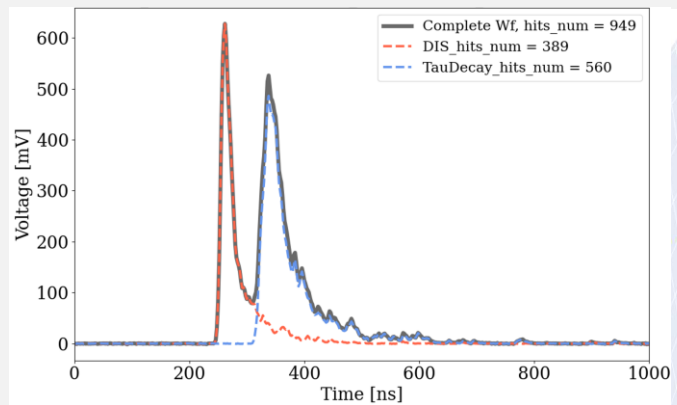
$$E_{recon} = 10^{\text{output}+b}$$



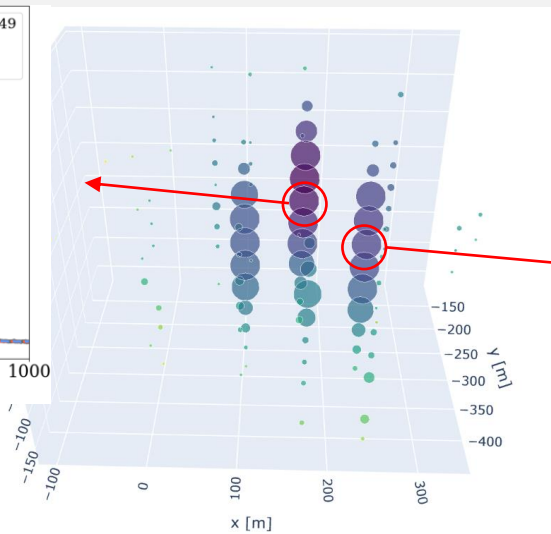
# Classification of $\nu_\tau$ and $\nu_e$

- **Input features:**
  - 10 brightest DOMs.
  - Location of DOM<sub>i</sub>.
  - **Waveform** with time length 2000ns.
- Network generates probabilities:  $output = (p_0, p_1)$ .
- **Cross-entropy loss** is used as the loss function:

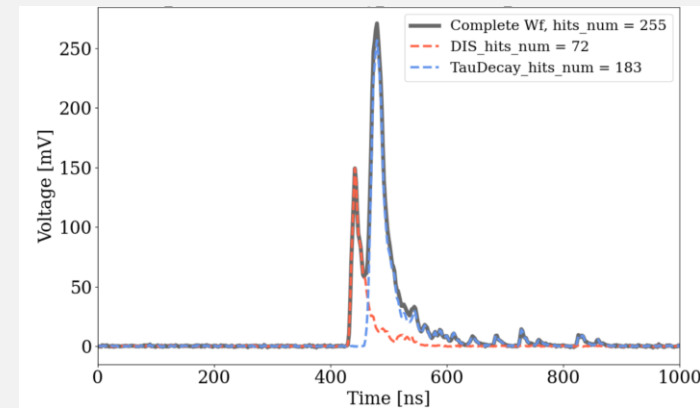
$$Loss = -y_0 \log(p_0) - y_1 \log(p_1)$$



Close to DIS vertex



Double bang

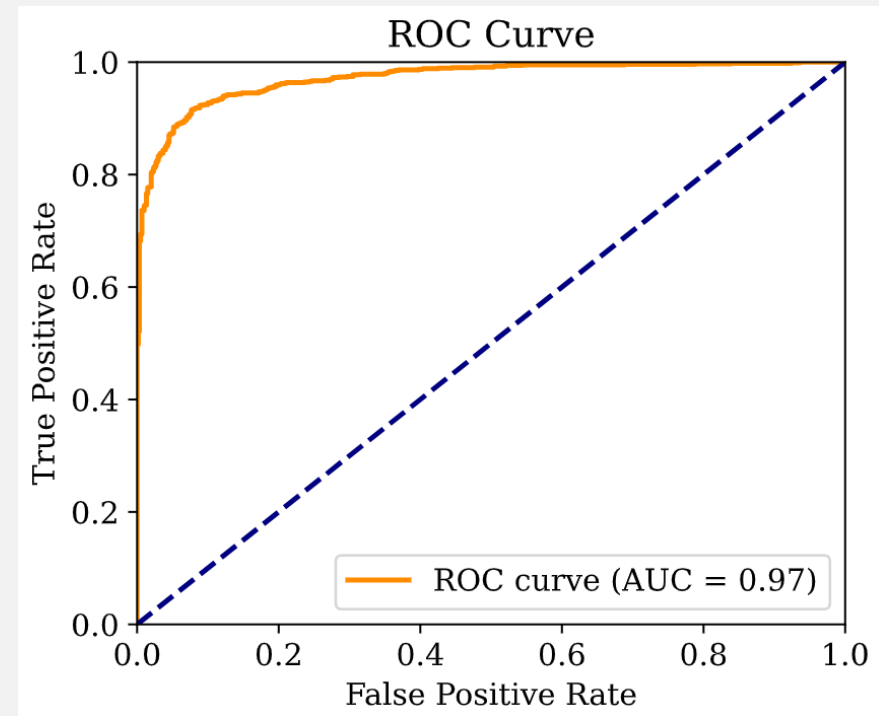
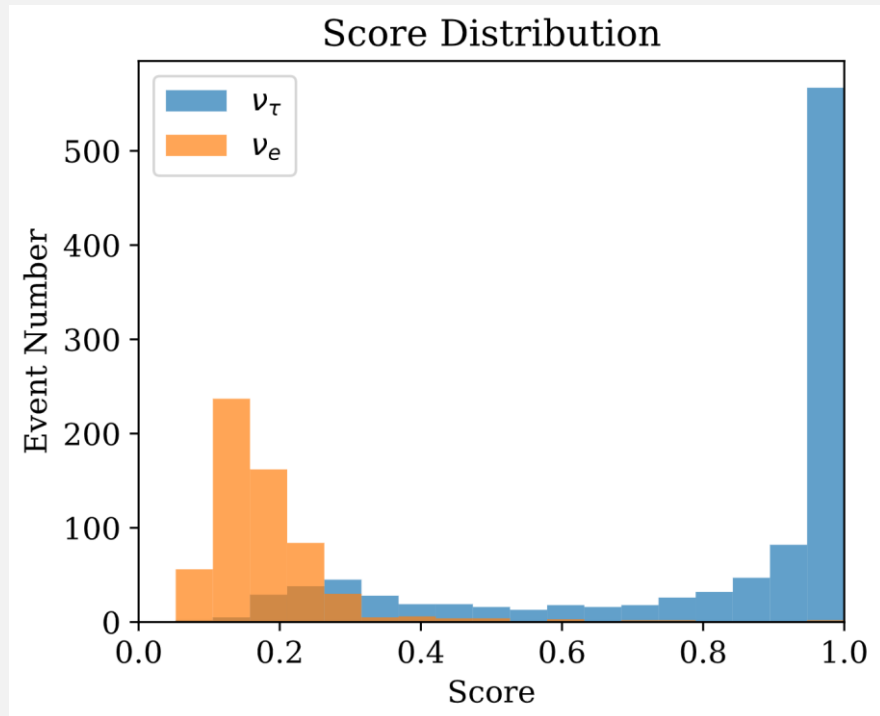


Close to decay vertex



# Classification of $\nu_\tau$ and $\nu_e$

- Take label of  $\nu_\tau = 1$ , label of  $\nu_e = 0$ :



# Cascade Reconstruction

## $\nu_e$ direction reconstruction

- **Input feature** of  $\text{DOM}_i$ :
  - Location of  $\text{DOM}_i$ .
  - Arrival time of the earliest photon.
  - Number of photons received in time window  $(10\text{ns} \times i, 10\text{ns} \times (i + 1)), i \in \{0, 1.. 99\}$
- Network is trained to predict  $\hat{n}_\nu$  with **MSE loss**:

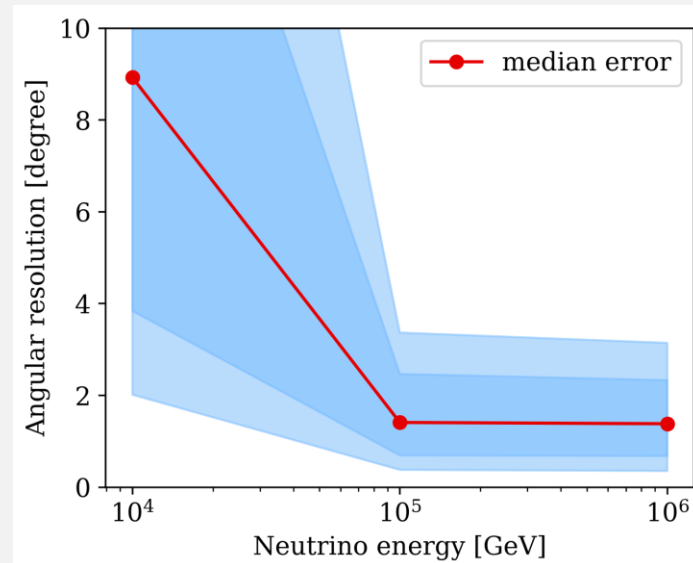
$$\text{Loss} = \left| \frac{\overrightarrow{\text{output}}}{|\text{output}|} - \hat{n}_\nu \right|^2$$

# Cascade Reconstruction

## $\nu_e$ direction reconstruction

- Network is only trained on  $\nu_e$  events with  $E_\nu = 100\text{TeV}$ .
- For different  $E_\nu$ , **linear scaling** to number of collected photons to cascade energy is applied:

$$n' = n \times \frac{100\text{TeV}}{E_\nu}$$



# Summary and Outlook

- Simulated neutrino events in TRIDENT are represented as point clouds and are reconstructed by TridentNet.
- GNN demonstrates high accuracy in neutrino telescope in tasks:
  - Reconstruction of direction and energy of track-like events.
  - Classification of  $\nu_\tau$  events and  $\nu_e$ .
  - Direction reconstruction of  $\nu_e$  events.
- Reconstruction of  $\nu_\tau$  and  $\nu_e$  events will be further studied.
- Classification between neutrino events and atmospheric muon events will be investigated.

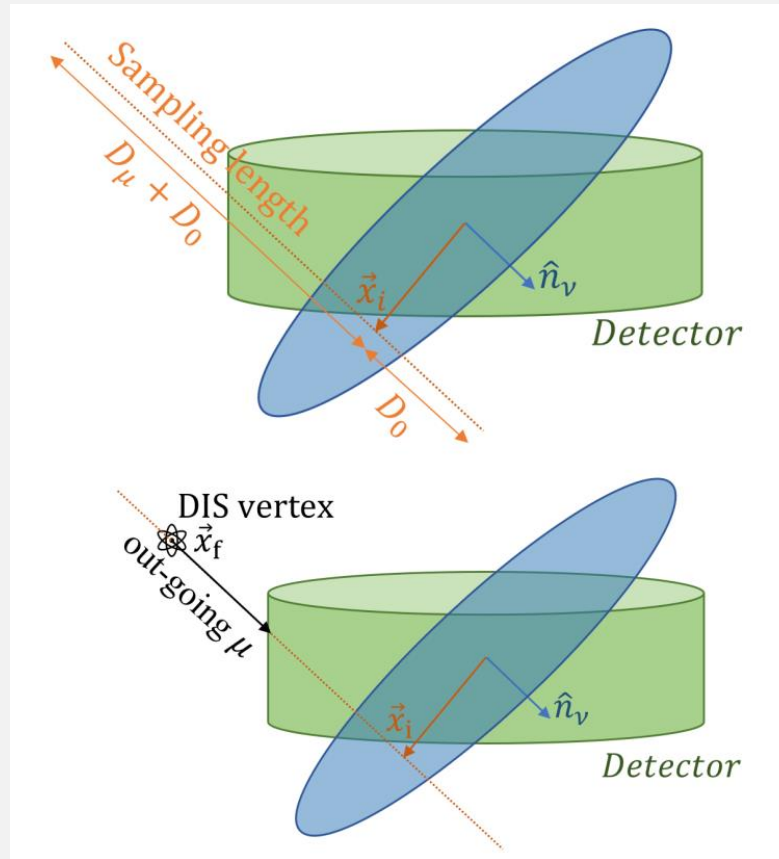
Thanks for listening!

# Backup

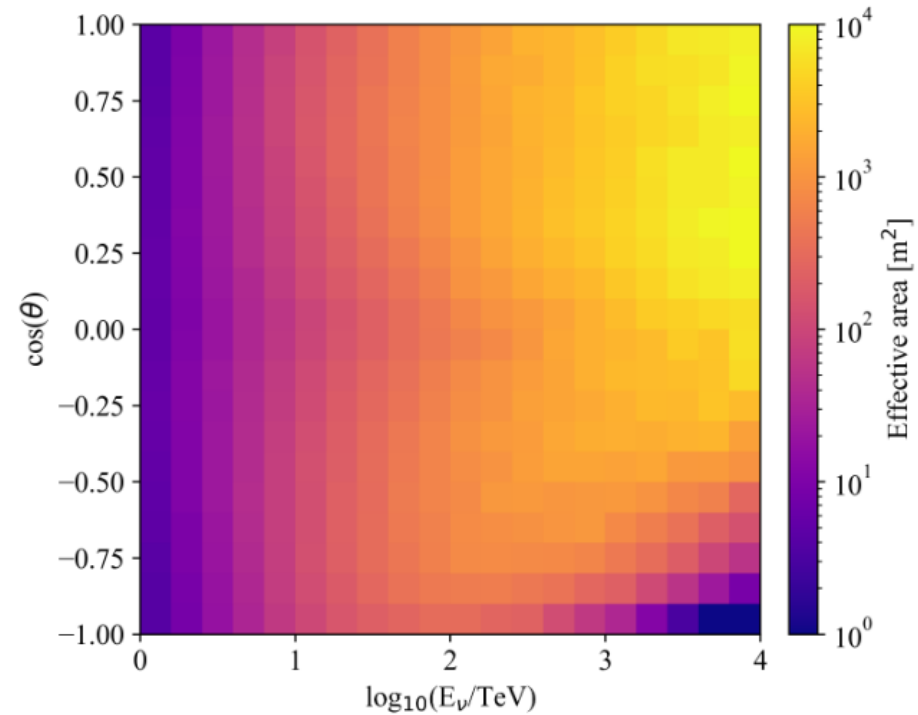
Email: [mo\\_cen@sjtu.edu.cn](mailto:mo_cen@sjtu.edu.cn)



# $v_\mu$ Vertex Sampling



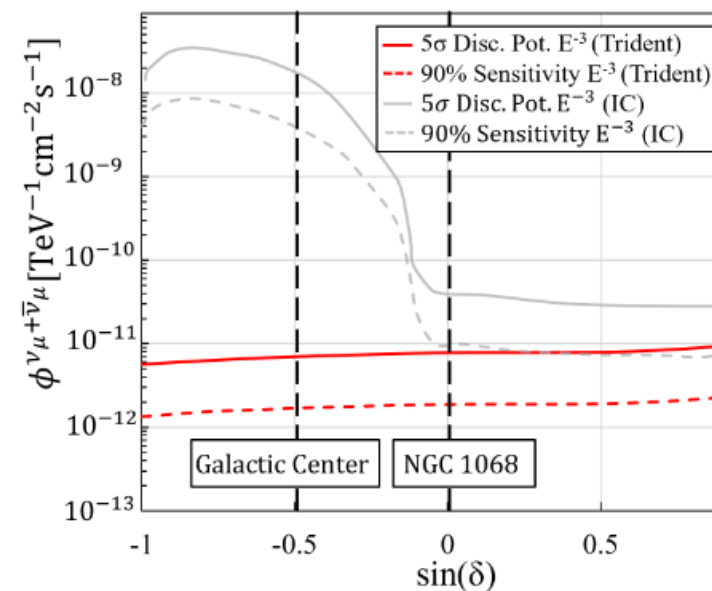
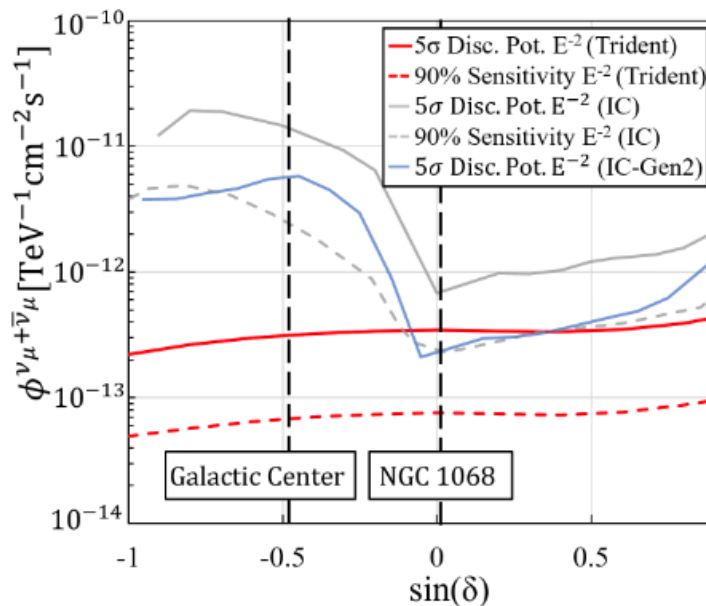
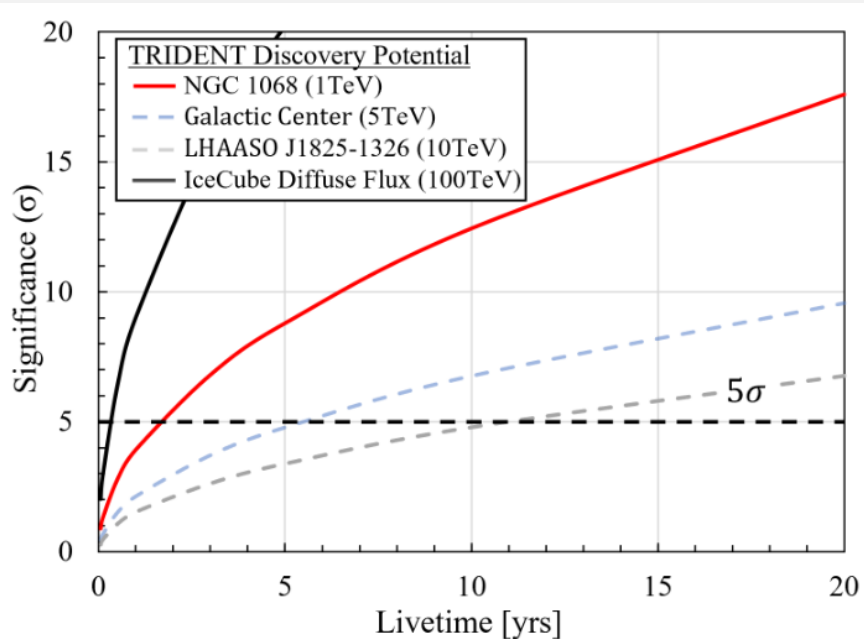
# Effective Area of $\nu_\mu$



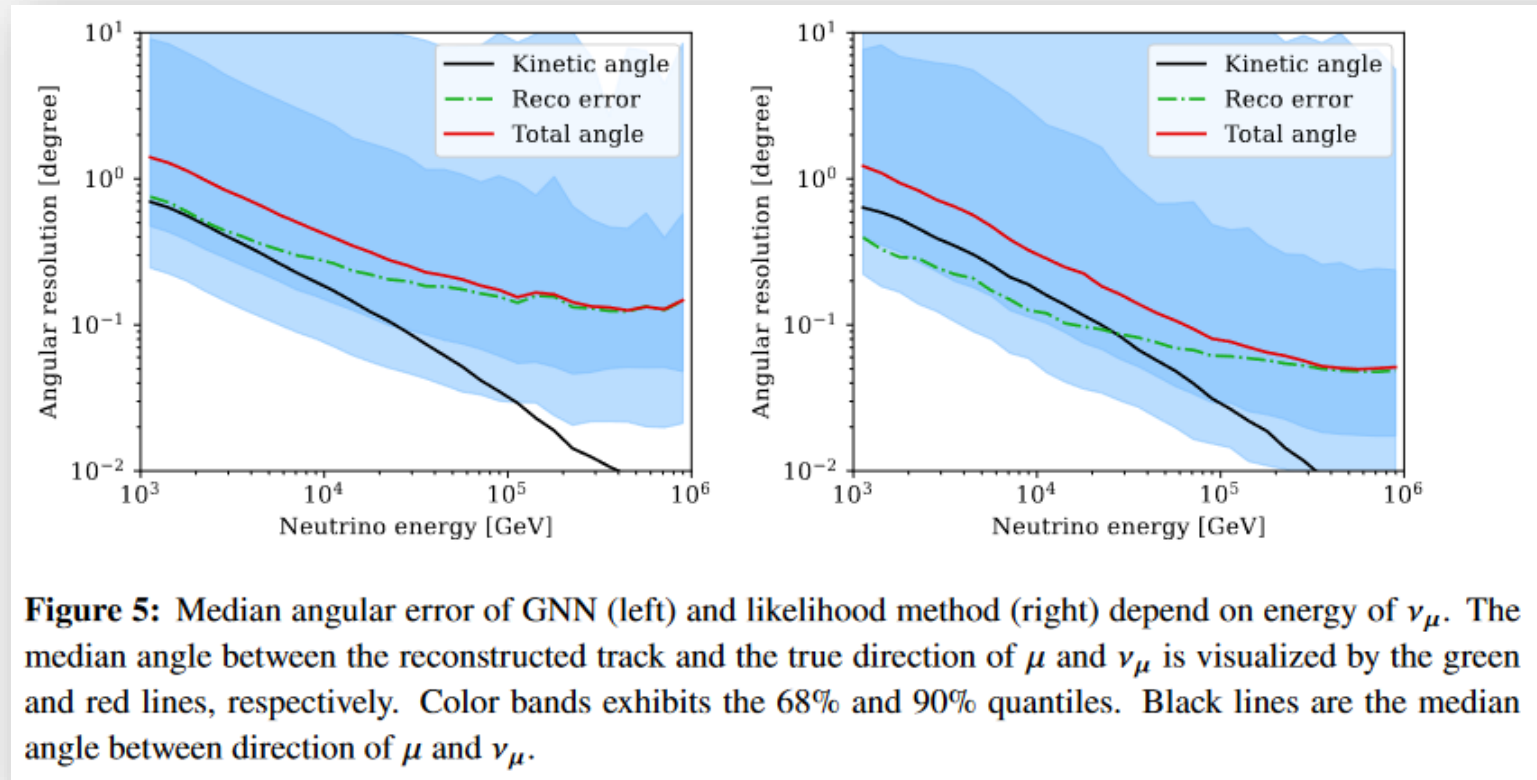
**Figure 15:** Effective areas at event reconstruction level for  $\nu_\mu$  track events as a function of primary neutrino energy and zenith angle in TRIDENT. At an energy of  $\sim 100$  TeV, the effective area for up-going events is expected to reach  $7 \times 10^2 \text{ m}^2$ . Only events with angular error less than 6 degree are selected to evaluate the effective area.

# Significance & Sensitivity

[arXiv:2207.04519](https://arxiv.org/abs/2207.04519)



# Comparison with Likelihood Method



# Track-like Events Reconstruction

## Direction reconstruction

- Model is trained on events with track length  $> 500\text{m}$ .
- Median angular error decreases from 1 degree to **0.1 degree** as the energy of  $\nu_\mu$  increases.

