



Probing Electroweak Phase Transition in the Singlet Standard Model at the LHC

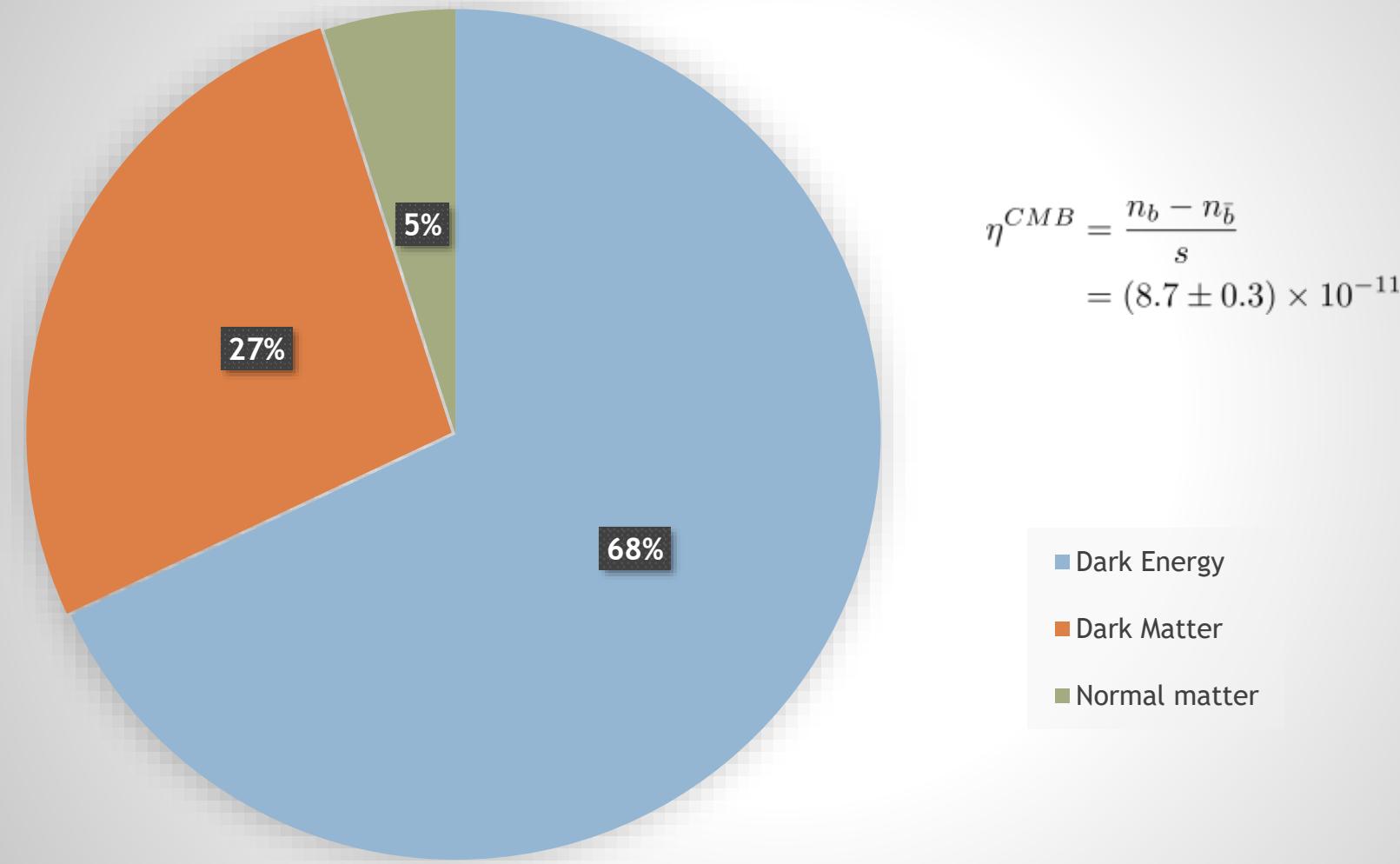
Wenxing Zhang (TDLI, SJTU),
Hao-Lin Li, Kun Liu, Michael Ramsey-Musolf, Yonghao Zeng

1

arXiv: 2303.03612



Cosmic Energy Budget



Baryon asymmetry of the Universe

44 different ways to create baryons in the Universe

- 1. GUT baryogenesis
- 2. GUT baryogenesis after preheating
- 3. Baryogenesis from primordial black holes
- 4. String scale baryogenesis
- 5. Affleck-Dine (AD) baryogenesis
- 6. Hybridized AD baryogenesis
- 7. No-scale AD baryogenesis
- 8. Single field baryogenesis
- 9. Electroweak (EW) baryogenesis
- 10. Local EW baryogenesis
- 11. Non-local EW baryogenesis
- 12. EW baryogenesis at preheating

- 13. SUSY EW baryogenesis
- 14. String mediated EW baryogenesis
- 15. Baryogenesis via leptogenesis
- 16. Inflationary baryogenesis
- 17. Resonant leptogenesis
- 18. Spontaneous baryogenesis
- 19. Coherent baryogenesis
- 20. Gravitational baryogenesis
- 21. Defect mediated baryogenesis
- 22. Baryogenesis from long cosmic strings
- 23. Baryogenesis from short cosmic strings
- 24. Baryogenesis from collapsing loops
- 25. Baryogenesis through collapse of vortons
- 26. Baryogenesis through axion domain walls
- 27. Baryogenesis through QCD domain walls
- 28. Baryogenesis through unstable domain walls
- 29. Baryogenesis from classical force
- 30. Baryogenesis from electrogenesis
- 31. B-ball baryogenesis
- 32. Baryogenesis from CPT breaking
- 33. Baryogenesis through quantum gravity
- 34. Baryogenesis via neutrino oscillations
- 35. Monopole baryogenesis
- 36. Axino induced baryogenesis

- 37. Gravitino induced baryogenesis
- 38. Radion induced baryogenesis
- 39. Baryogenesis in large extra dimensions
- 40. Baryogenesis by brane collision
- 41. Baryogenesis via density fluctuations
- 42. Baryogenesis from hadronic jets
- 43. Thermal leptogenesis
- 44. Nonthermal leptogenesis

Shaposhnikov, DISCRETE 08, 11, Dec

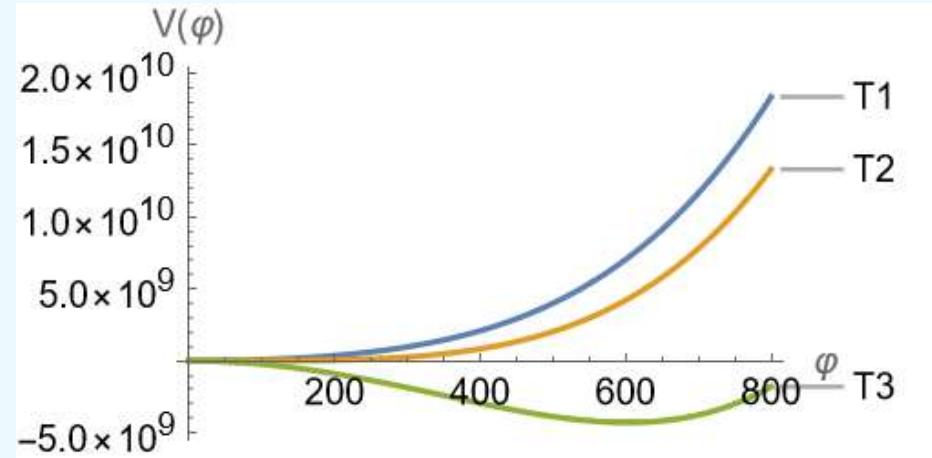
Sakharov conditions:

- Baryon number violating interactions.
- C and CP violation.
- Departure from thermal equilibrium.

A.Sakharov JETP 5, 24 (1967)

 **Sphaleron washout?
Strong First Order Electroweak Phase
Transition BSM**

Electroweak Phase Transition in the SM



$$V_{eff}(h, s, T) = V_0(h, s) + V_{CW}^{T=0}(h, s) + V_{T \neq 0}(h, s, T).$$

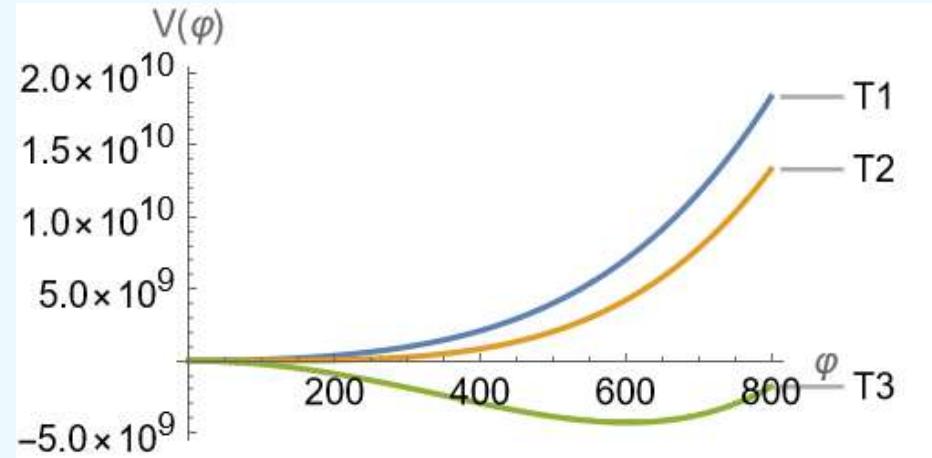
$$V_{CW}^{T=0} = \sum_k \frac{(-1)^{2s_k}}{64\pi^2} g_k [M_k^2]^2 \left(\log \frac{M_k^2}{\mu^2} + c_k \right),$$

$$\begin{aligned} V^{High-T}(h, s, T) \\ = V_0(h, s) + \frac{T^2}{48} (12m_t^2) + \frac{T^2}{24} (3m_G^2 + m_h^2 + m_s^2 + m_A^2 + 6M_W^2 + 3M_Z^2) \\ = V_0(h, s) + \frac{1}{2} \left(\frac{\lambda}{8} + \frac{\delta_2}{24} + \frac{3g_2^2 + g_1^2}{16} + \frac{y_t^2}{4} \right) h^2 T^2 + \frac{\delta_2 + d_2}{48} s^2 T^2. \end{aligned}$$

$$V_{eff}(\phi, T) \simeq D(T^2 - T_0^2) \phi^2 - ET\phi^3 + \frac{\bar{\lambda}}{4}\phi^4$$

→ Negative for $T < T_0$, non-zero minimum.

Electroweak Phase Transition in the SM



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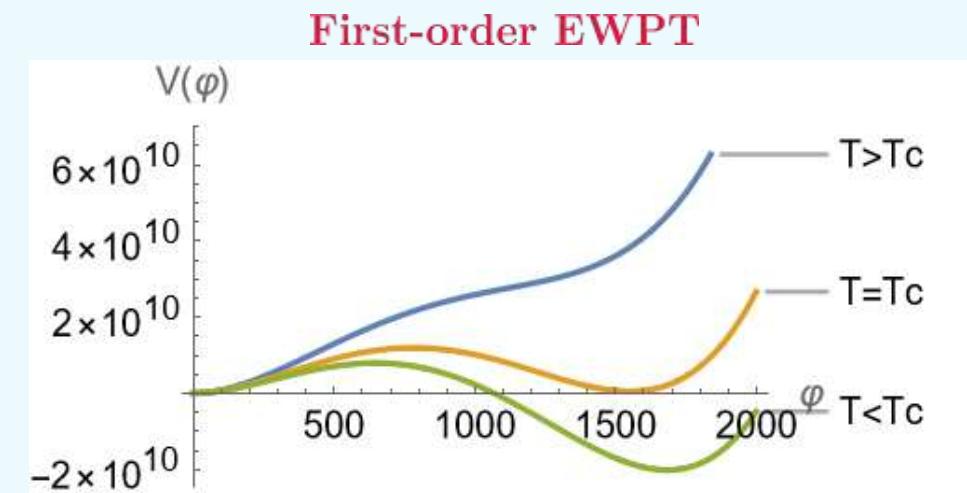
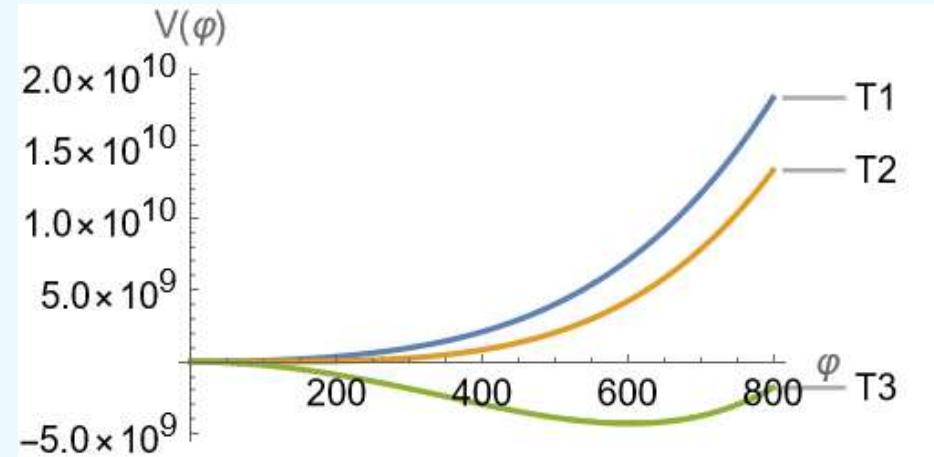
$$\begin{aligned} & V^{High-T}(h, s, T) \\ &= V_0(h, s) + \frac{T^2}{48} (12m_t^2) + \frac{T^2}{24} (3m_G^2 + m_h^2 + m_s^2 + m_A^2 + 6M_W^2 + 3M_Z^2) \\ &= V_0(h, s) + \frac{1}{2} \left(\frac{\lambda}{8} + \frac{\delta_2}{24} + \frac{3g_2^2 + g_1^2}{16} + \frac{y_t^2}{4} \right) h^2 T^2 + \frac{\delta_2 + d_2}{48} s^2 T^2. \end{aligned}$$

Generate barriers

$$V_{eff}(\phi, T) \simeq D(T^2 - T_0^2) \phi^2 - ET\phi^3 + \frac{\bar{\lambda}}{4}\phi^4$$

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Electroweak Phase Transition in the SM

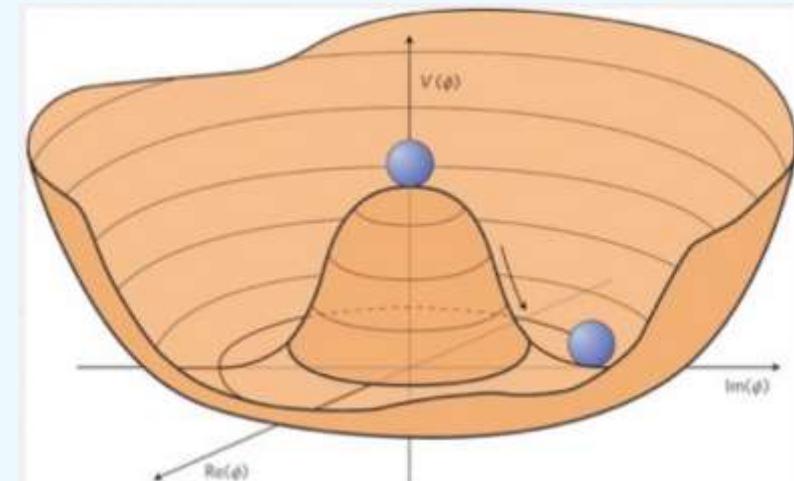


Generate barriers

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Wenxing Zhang, SPCS 2023

Negative for $T < T_0$



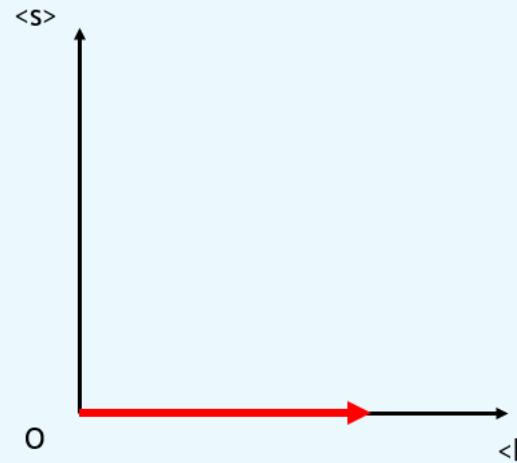
SM: Crossover!

TDLI, SJTU

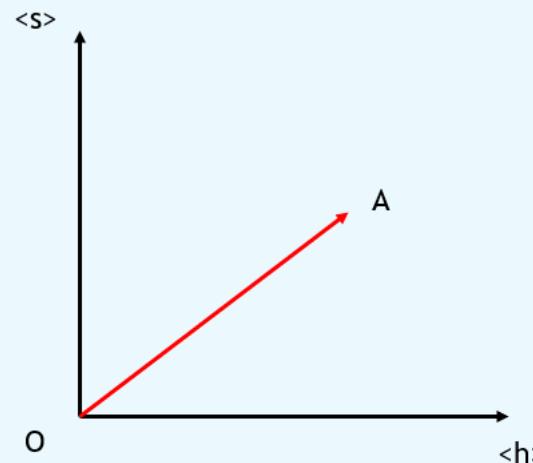
SFOEWPT in BSM: Multi-step EWPT

The simplest model in extended SM that generate multiple-step EWPT: the xSM.

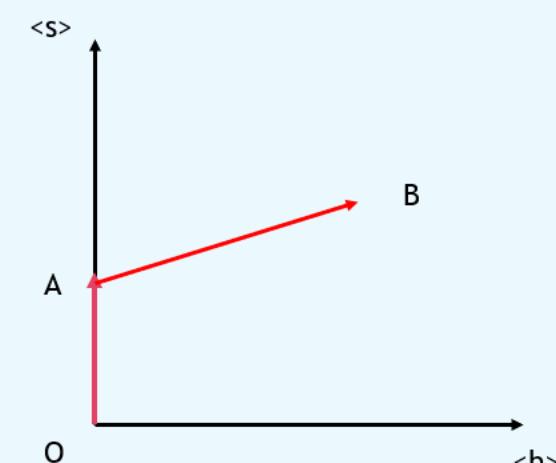
- a. The xSM can be a simplified model for many UV complete model that realise multiple-step SFOEWPT.
- b. The pheno of xSM is typical and representative to models that realise SFOEWPT.



a.



b.

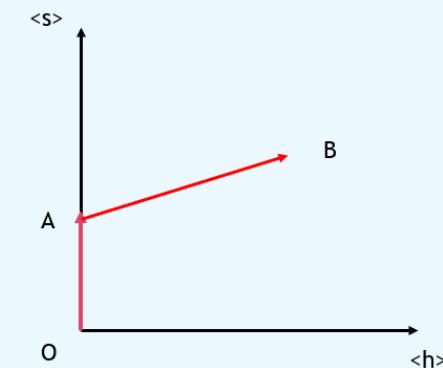
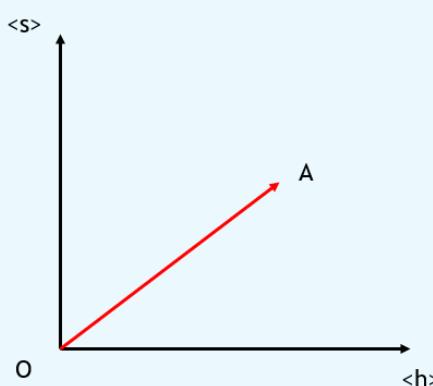
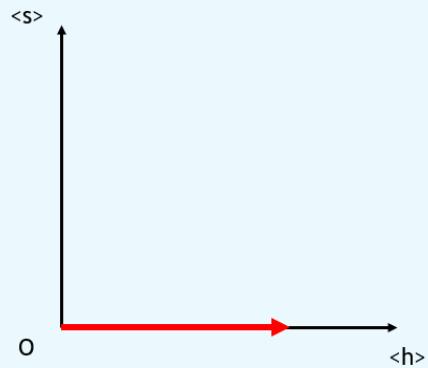


c.

The xSM

$$V_0(H, S) = -\mu^2(H^\dagger H) + \lambda(H^\dagger H)^2 + \frac{a_1}{2}(H^\dagger H)S + \frac{a_2}{2}(H^\dagger H)S^2 + \frac{b_2}{2}S^2 + \frac{b_3}{3}S^3 + \frac{b_4}{4}S^4,$$

$$S = x_0 + s$$

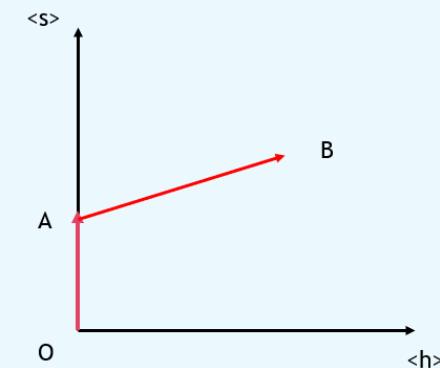
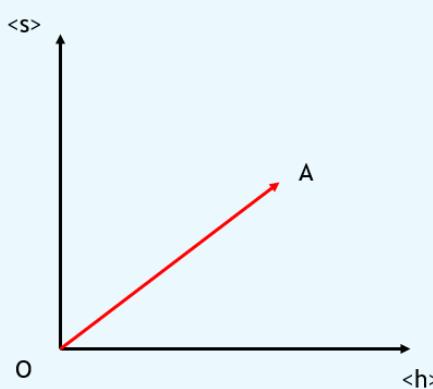
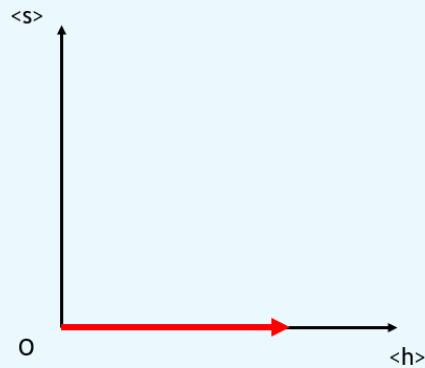


Key-item to generate a barrier in FOEWPT: a_2, a_1, b_3

The xSM

$$V_0(H, S) = -\mu^2(H^\dagger H) + \lambda(H^\dagger H)^2 + \frac{a_1}{2}(H^\dagger H)S + \frac{a_2}{2}(H^\dagger H)S^2 + \frac{b_2}{2}S^2 + \frac{b_3}{3}S^3 + \frac{b_4}{4}S^4,$$

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Key-item to generate a barrier in FOEWPT: a_2, a_1, b_3

The question is:

Can these terms be as large as we want?

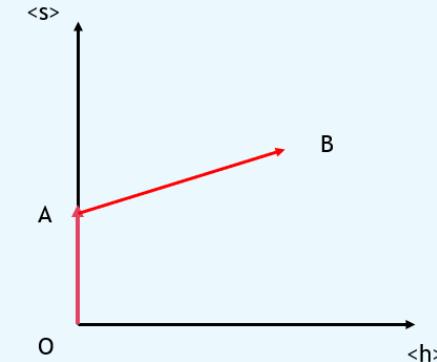
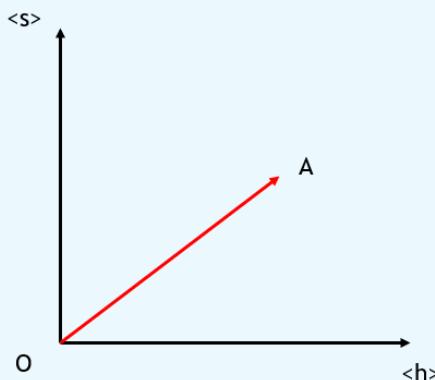
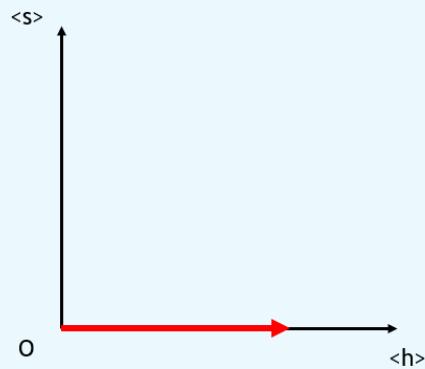
What's the consequence of adding these terms?

How to probe them?

The xSM

$$V_0(H, S) = -\mu^2(H^\dagger H) + \lambda(H^\dagger H)^2 + \frac{a_1}{2}(H^\dagger H)S + \frac{a_2}{2}(H^\dagger H)S^2 \\ + \frac{b_2}{2}S^2 + \frac{b_3}{3}S^3 + \frac{b_4}{4}S^4,$$

$$S = x_0 + s$$



Key-item to generate a barrier in FOEWPT: a_2, a_1, b_3

The question is:

One consequence: Scalar sector mixing:

Can these terms be as large as we want?

What's the consequence of adding these terms?

How to probe them?

$$\mathcal{M}^2 = \begin{pmatrix} -\frac{a_1 v_0^2}{4x_0} + x_0(b_3 + 2b_4 x_0) & \frac{v_0}{2}(a_1 + 2a_2 x_0) \\ \frac{v_0}{2}(a_1 + 2a_2 x_0) & 2\lambda v_0^2 \end{pmatrix}.$$

xSM Constraints: Vacuum Stability

$$V_0(H, S) = -\mu^2(H^\dagger H) + \lambda(H^\dagger H)^2 + \frac{a_1}{2}(H^\dagger H)S + \frac{a_2}{2}(H^\dagger H)S^2 \\ + \frac{b_2}{2}S^2 + \frac{b_3}{3}S^3 + \frac{b_4}{4}S^4,$$

- Vacuum (v_0, x_0) is a stable minimum.

$$\begin{vmatrix} \frac{\partial^2 V}{\partial v_0^2} & \frac{\partial^2 V}{\partial v_0 \partial x_0} \\ \frac{\partial^2 V}{\partial v_0 \partial x_0} & \frac{\partial^2 V}{\partial x_0^2} \end{vmatrix} > 0$$

- The minimum (v_0, x_0) is global minimum.
- The potential is bounded from below.

$$\begin{vmatrix} \lambda & \frac{a_2}{4} \\ \frac{a_2}{4} & \frac{b_4}{4} \end{vmatrix} > 0$$

xSM Constraints: Perturbation

$$V_0(H, S) = -\mu^2(H^\dagger H) + \lambda(H^\dagger H)^2 + \frac{a_1}{2}(H^\dagger H)S + \frac{a_2}{2}(H^\dagger H)S^2 \\ + \frac{b_2}{2}S^2 + \frac{b_3}{3}S^3 + \frac{b_4}{4}S^4,$$

Input parameters: Dim-1 and Dim-0 $a_1, b_3, b_4, \lambda, x_0$

EW effective theory: Normalisation Scale=10 TeV.

$$\frac{dX}{d \log \mu} = \frac{1}{(4\pi)^2} \beta^{(1)}(X), \quad 0 < 6\lambda, 6b_2, |a_2| < 4\pi$$

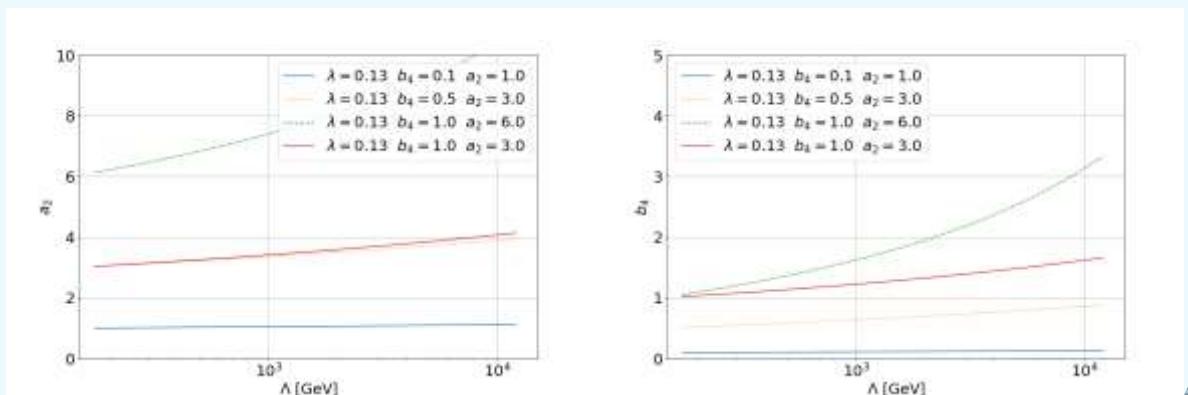
$$\beta^{(1)}(b_4) = 2a_2^2 + 18b_4^2$$

$$\beta^{(1)}(a_2) = 12a_2\lambda + 4a_2^2 + 6a_2b_4 - \frac{3}{2}a_2g_1^2 - \frac{9}{2}a_2g_2^2 + 6a_2|y_t|^2$$

$$\beta^{(1)}(a_1) = -\frac{3}{2}a_1g_1^2 - \frac{9}{2}a_1g_2^2 + 12a_1\lambda + 4a_1a_2 + 4a_2b_3$$

$$\beta^{(1)}(b_3) = +3a_1a_2 + 18b_3b_4$$

$$\beta^{(1)}(b_2) = a_1^2 + 4b_3^2 - 4a_2\mu + 6b_2b_4$$



xSM Constraints: EWPO

$$\Delta\mathcal{O} = (\cos^2 \theta - 1)\mathcal{O}^{\text{SM}}(m_{h_1}) + \sin^2 \theta \mathcal{O}^{\text{SM}}(m_{h_2}) = \sin^2 \theta [\mathcal{O}^{\text{SM}}(m_{h_2}) - \mathcal{O}^{\text{SM}}(m_{h_1})]$$

.

$$S - S_{SM} = 0.04 \pm 0.11$$

$$T - T_{SM} = 0.09 \pm 0.14$$

$$U - U_{SM} = -0.02 \pm 0.11$$

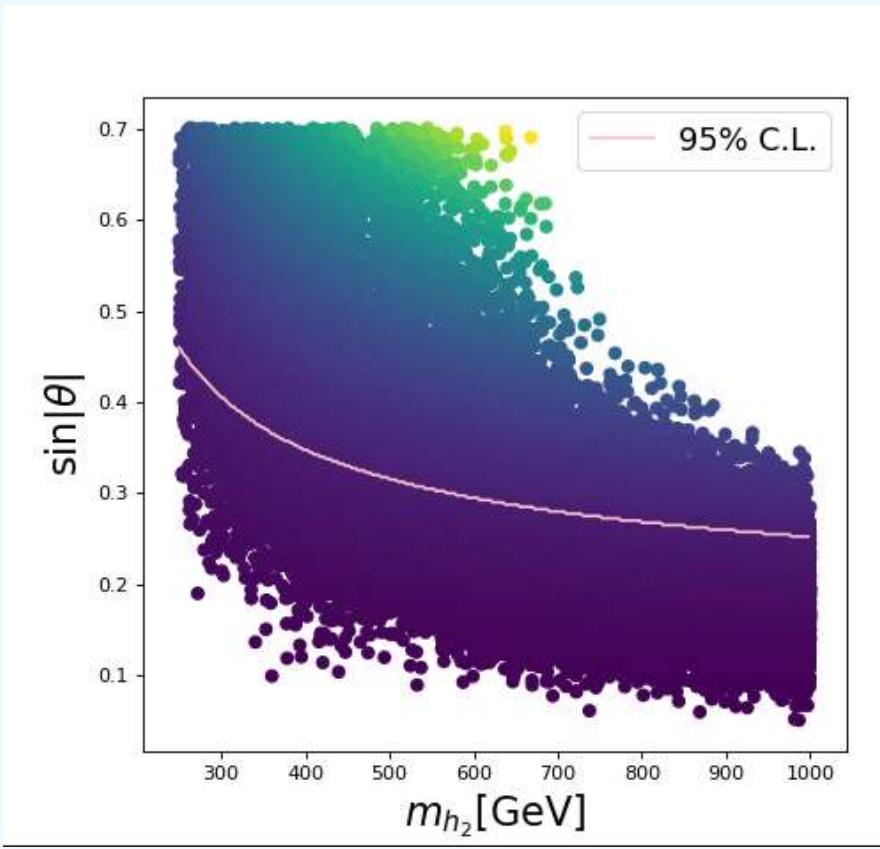
$$\rho_{ij} = \begin{pmatrix} 1 & 0.92 & -0.68 \\ 0.92 & 1 & -0.87 \\ -0.68 & -0.87 & 1 \end{pmatrix}.$$

$$\chi^2 = (X - \hat{X})_i (\sigma^2)_{ij}^{-1} (X - \hat{X})_j < 5.99$$

→ For 2 DoF, 95% C.L.

xSM Constraints: EW Precision Observables

$$\Delta\mathcal{O} = (\cos^2 \theta - 1)\mathcal{O}^{\text{SM}}(m_{h_1}) + \sin^2 \theta \mathcal{O}^{\text{SM}}(m_{h_2}) = \sin^2 \theta [\mathcal{O}^{\text{SM}}(m_{h_2}) - \mathcal{O}^{\text{SM}}(m_{h_1})]$$



YC, MJRM, LZ, WZ,
arXiv:2307.07615

Wenxing Zhang, SPCS 2023

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Eur.Phys.J.C 78 (2018) 8

TDLI, SJTU

xSM Constraints: Higgs Measurement

$$\Delta \mathcal{O} = (\cos^2 \theta - 1) \mathcal{O}^{\text{SM}}(m_{h_1}) + \sin^2 \theta \mathcal{O}^{\text{SM}}(m_{h_2}) = \sin^2 \theta [\mathcal{O}^{\text{SM}}(m_{h_2}) - \mathcal{O}^{\text{SM}}(m_{h_1})]$$

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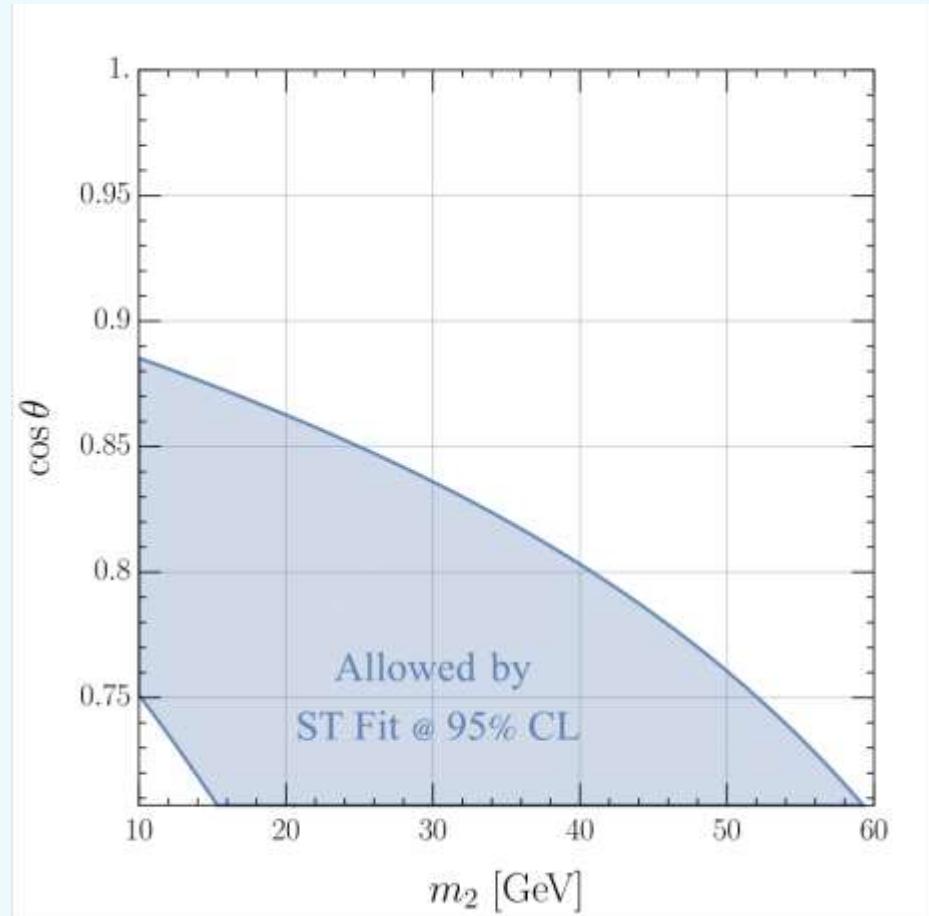
$$\begin{aligned}\Delta S &= 0.086 \pm 0.077, \\ \Delta T &= 0.177 \pm 0.070\end{aligned}$$

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$$\Delta\mathcal{O} = (\cos^2 \theta - 1)\mathcal{O}^{\text{SM}}(m_{h_1}) + \sin^2 \theta \mathcal{O}^{\text{SM}}(m_{h_2}) = \sin^2 \theta [\mathcal{O}^{\text{SM}}(m_{h_2}) - \mathcal{O}^{\text{SM}}(m_{h_1})]$$



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xSM Constraints: Higgs Measurement

New physics may induce deviation in Higgs couplings. Therefore it modifies the Higgs signal strength in Higgs measurement.

| Production mode | ggF+ $b\bar{b}H$ | VBF | WH | ZH | $t\bar{t}H$ | tH |
|---|------------------------|------------------------|------------------------|------------------------|------------------------|------------------------|
| $\sum_f \mu_{i \rightarrow h_1 \rightarrow ff}$ | $1.03^{+0.07}_{-0.07}$ | $1.10^{+0.13}_{-0.12}$ | $1.16^{+0.23}_{-0.22}$ | $0.96^{+0.22}_{-0.21}$ | $0.74^{+0.24}_{-0.24}$ | $6.61^{+4.24}_{-3.76}$ |

Nature 607, 52-59 (2022)

$$\mu_{pp \rightarrow h_1 \rightarrow XX} = \frac{\sigma_{pp \rightarrow h_1} BR(h_1 \rightarrow XX)}{\sigma_{pp \rightarrow h}^{SM} BR(h \rightarrow XX)_{SM}} \simeq \cos^4 \theta,$$

$$\chi^2 = \sum_{i,f} \frac{(\mu_{i \rightarrow h_1 \rightarrow f}^{xSM} - \mu_{i \rightarrow h_1 \rightarrow f}^{obs})^2}{\sigma_{\mu_{i \rightarrow h \rightarrow f}}^2}, \quad \Delta\chi^2 = \chi^2 - \chi^2_{min} < 3.841. \rightarrow \text{For 1 DoF, 95\% C.L.}$$



This set $\|\sin \theta\| < 0.193$.

Probe SFOEWPT at the LHC: Heavy Scalar Resonance

$$\mathcal{M}^2 = \begin{pmatrix} -\frac{a_1 v_0^2}{4x_0} + x_0 (b_3 + 2b_4 x_0) & \frac{v_0}{2} (a_1 + 2a_2 x_0) \\ \frac{v_0}{2} (a_1 + 2a_2 x_0) & 2\lambda v_0^2 \end{pmatrix}.$$

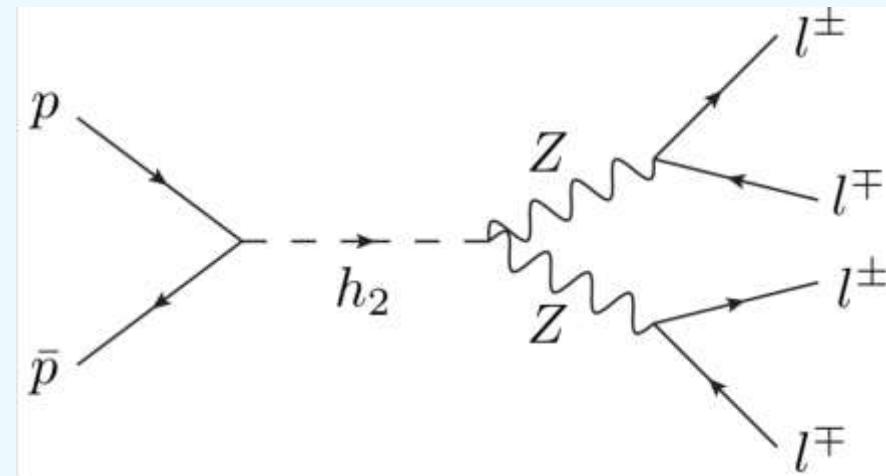
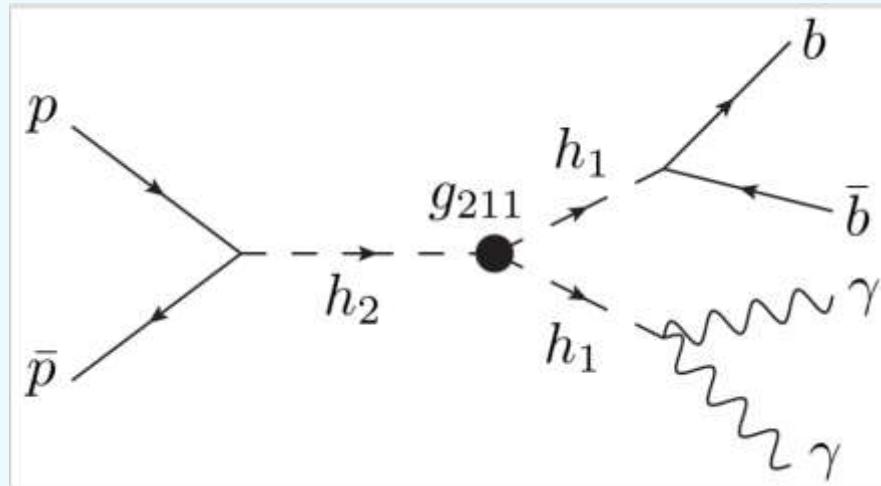
| Di-Higgs | Ref. |
|-------------------------|--|
| $4b$ | JHEP 01 (2019) 030, JHEP 08 (2018) 152 |
| $b b \nu \bar{\nu}$ | JHEP 04 (2019) 092, JHEP 01 (2018) 054 |
| $b b l \nu l \bar{\nu}$ | JHEP 01 (2018) 054 |
| WW^*WW^* | JHEP 05 (2019) 124 |
| $b b \tau \tau$ | Phys.Rev.Lett. 122 (2019) 8, 089901, Phys.Lett.B 778 (2018) 101-127 |
| $b b \gamma \gamma$ | JHEP 11 (2018) 040, JHEP 11 (2018) 040 |
| ... | ... |

| Di-Boson | Ref. |
|--------------|--|
| Semileptonic | Eur.Phys.J.C 80 (2020) 12, JHEP 03 (2018) 042 |
| Hadronic | Phys.Lett.B 777 (2018) 91-113, JHEP 09 (2016) 173 |
| Leptonic | Eur.Phys.J.C 78 (2018) 4, 293, Phys.Rev.D 98 (2018) 5 Eur.Phys.J.C 78 (2018) 1, 24 |
| ... | ... |

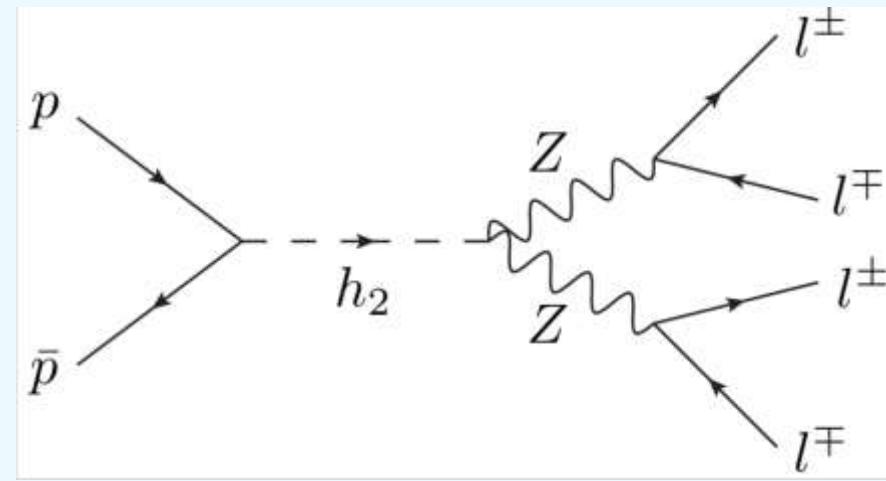
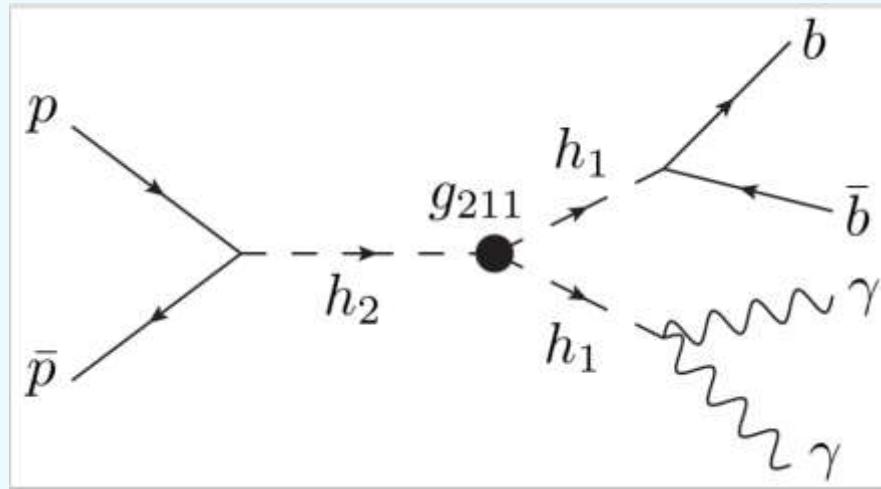
| Di-Fermion | Ref. |
|-------------------|--|
| $\tau \bar{\tau}$ | Phys.Rev.Lett. 125 (2020) 5, JHEP 01 (2018) 055 |
| $b \bar{b}$ | Phys.Rev.D 102 (2020) 3 |
| $t \bar{t}$ | JHEP 07 (2023) 203 |
| ... | ... |

All channels are effective in probing the xSM !

The first step: $b\bar{b}\gamma\gamma$ and $ZZ \rightarrow 4l$

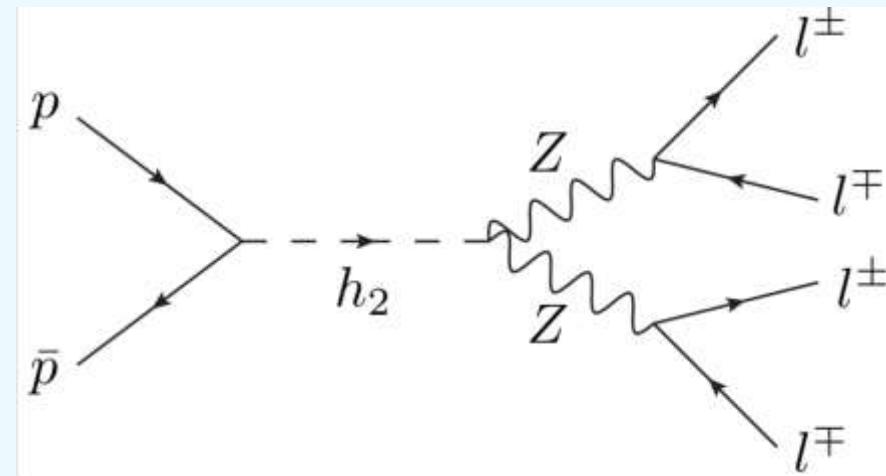
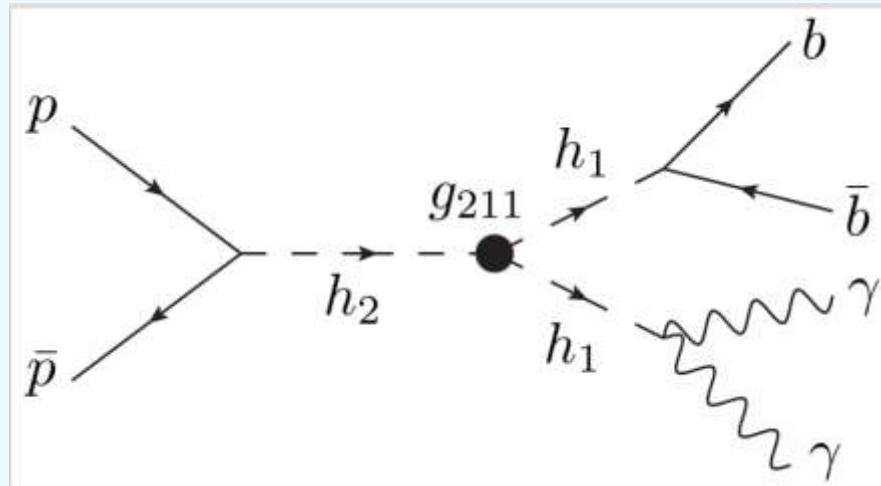


The first step: $b\bar{b}\gamma\gamma$ and $ZZ \rightarrow 4l$



$$\begin{aligned} g_{211} = & \frac{1}{4} [(a_1 + 2a_2 x_0) \cos^3 \theta + 4v_0 (a_2 - 3\lambda) \cos^2 \theta \sin \theta \\ & - 2(a_1 + 2a_2 x_0 - 2b_3 - 6b_4 x_0) \cos \theta \sin^2 \theta - 2a_2 v_0 \sin^3 \theta]. \end{aligned}$$

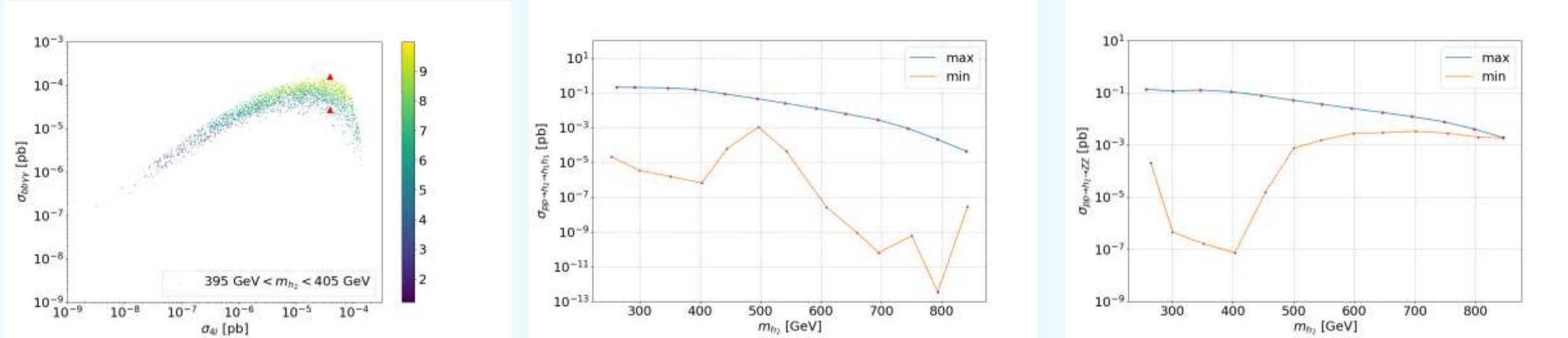
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$$\sigma_{bb\gamma\gamma} = \sigma_{pp \rightarrow h_2} \times BR(h_2 \rightarrow h_1 h_1) \times BR(h_1 \rightarrow b\bar{b}) \times BR(h_1 \rightarrow \gamma\gamma), \\ \sigma_{4\ell} = \sigma_{pp \rightarrow h_2} \times BR(h_2 \rightarrow ZZ) \times BR(ZZ \rightarrow 4\ell)$$

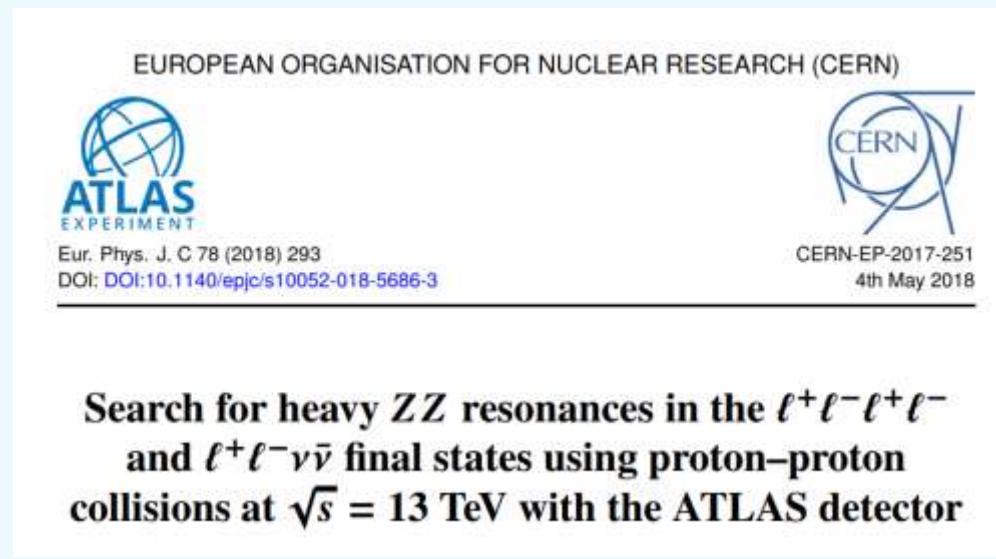
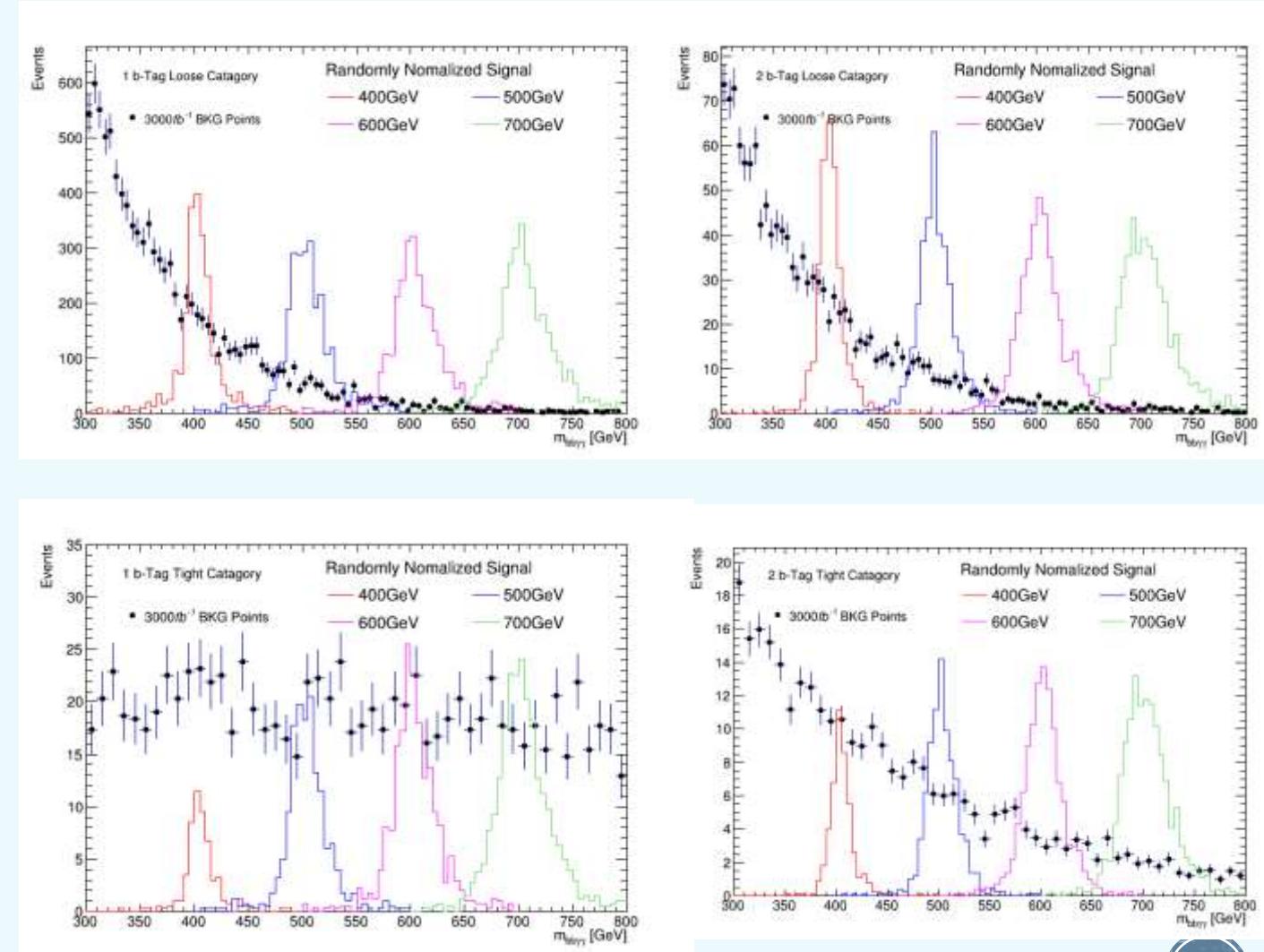
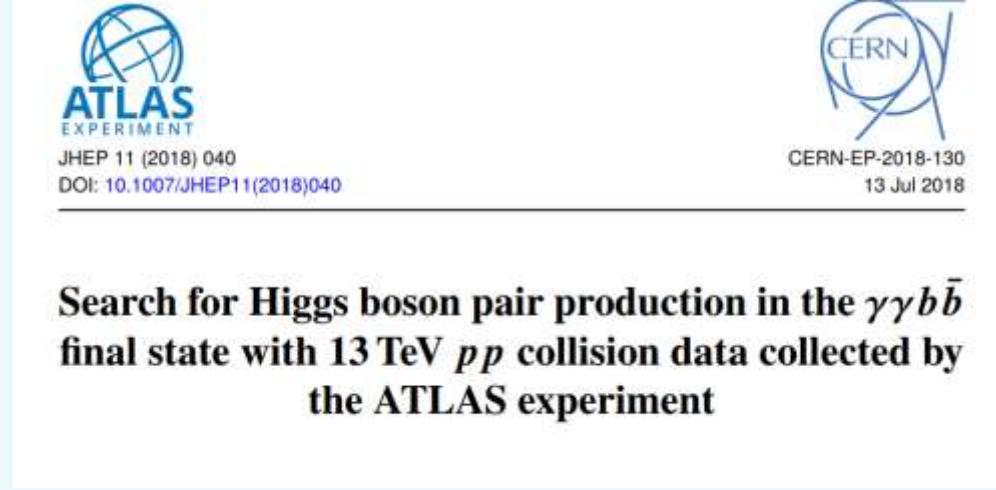
The first step: $b\bar{b}\gamma\gamma$ and $ZZ \rightarrow 4l$



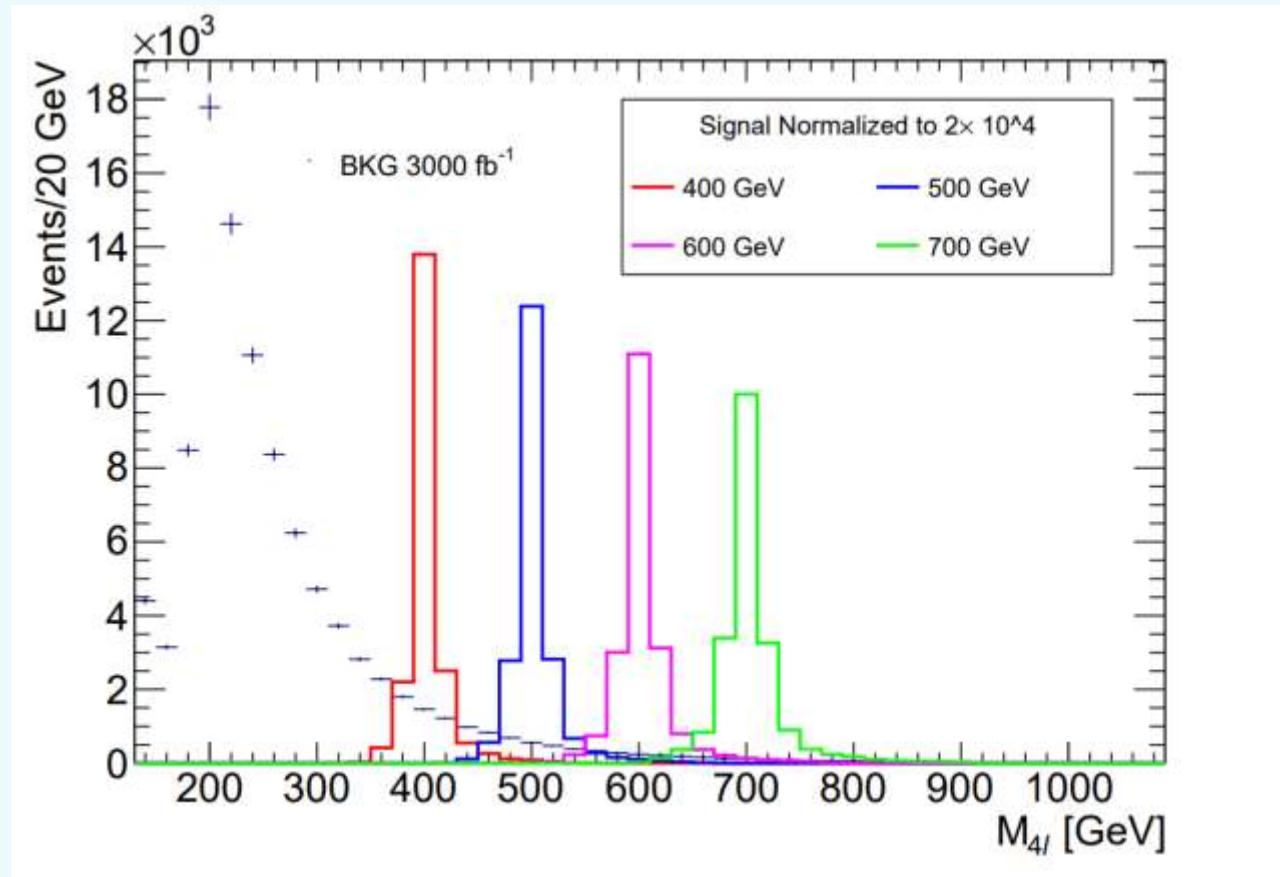
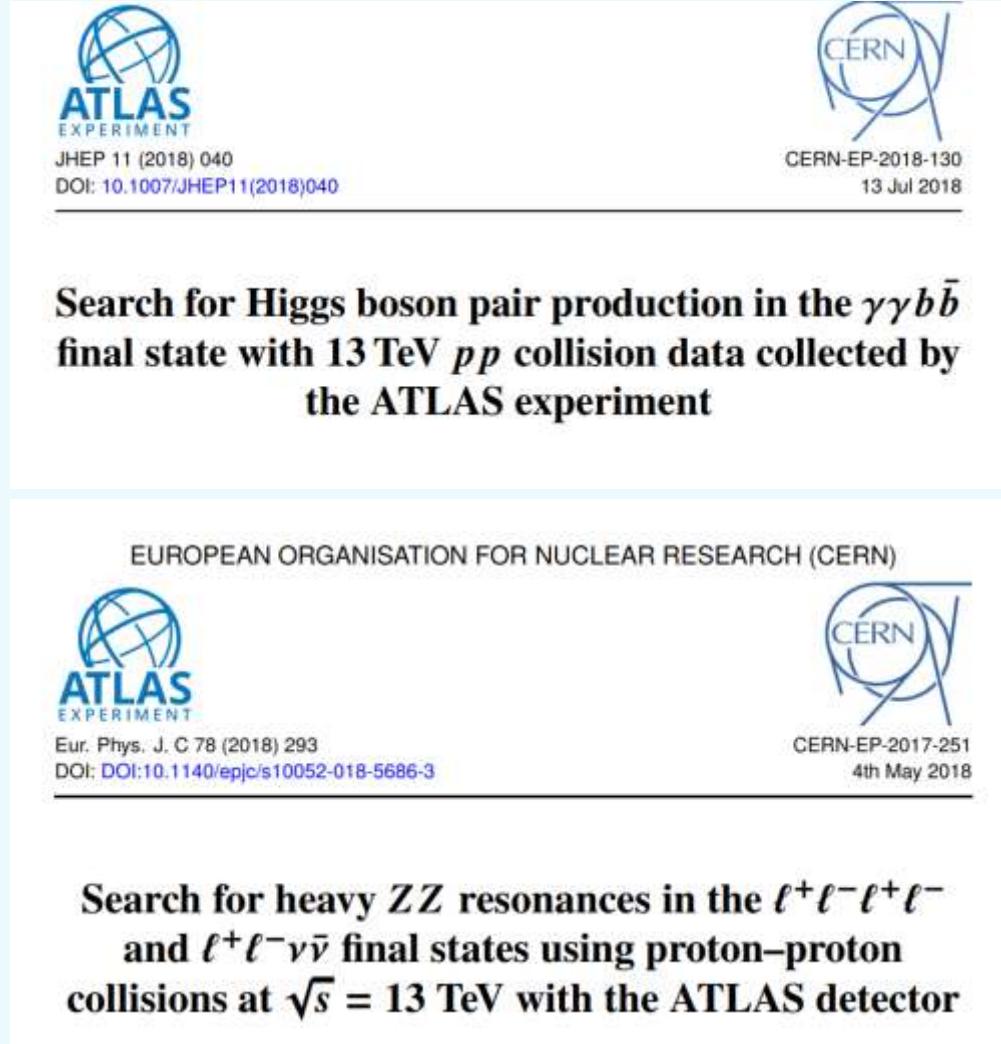
$$\begin{aligned}\sigma_{bb\gamma\gamma} &= \sigma_{pp \rightarrow h_2} \times BR(h_2 \rightarrow h_1 h_1) \times BR(h_1 \rightarrow b\bar{b}) \times BR(h_1 \rightarrow \gamma\gamma), \\ \sigma_{4\ell} &= \sigma_{pp \rightarrow h_2} \times BR(h_2 \rightarrow ZZ) \times BR(ZZ \rightarrow 4\ell)\end{aligned}$$

The problem is: How to combine them together?
Will the combined bound be stronger?

Standard of combination of multiple channels

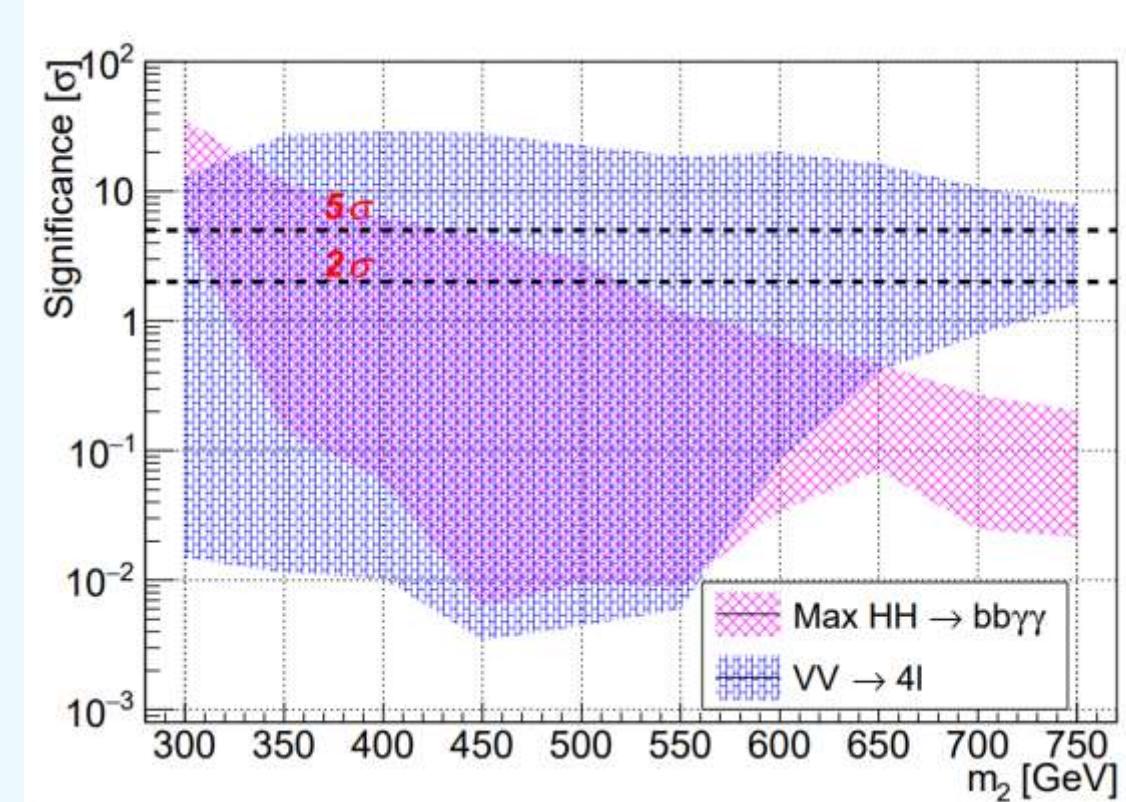
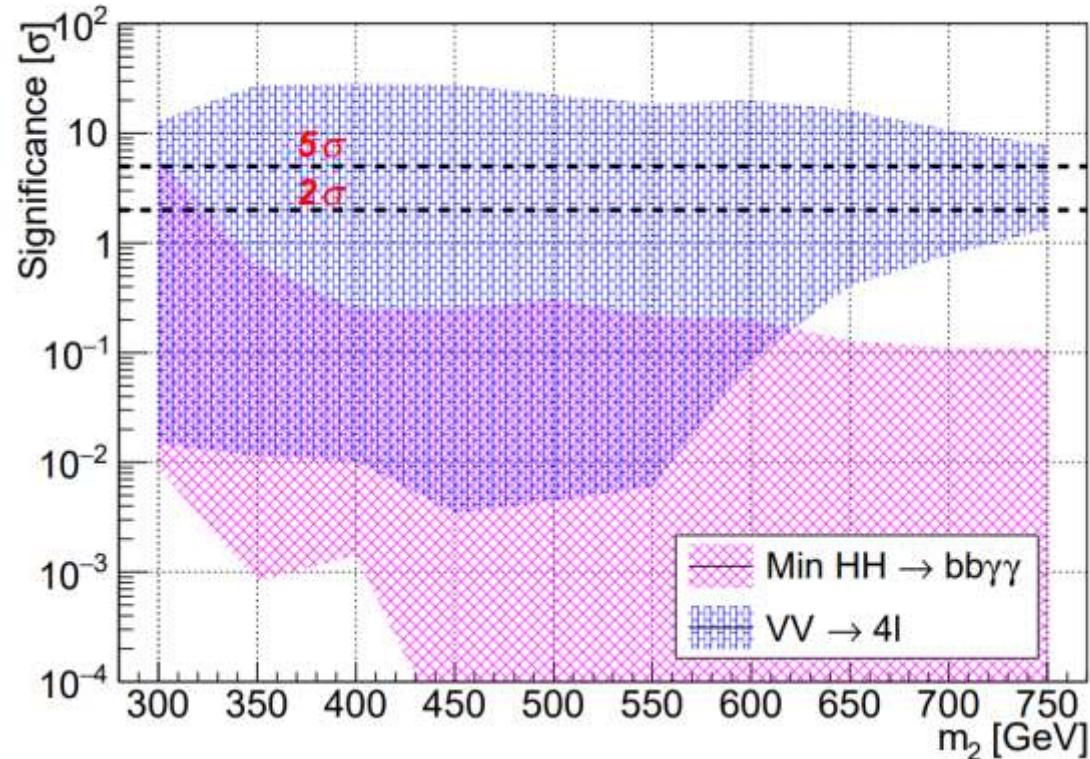


Standard of combination of multiple channels

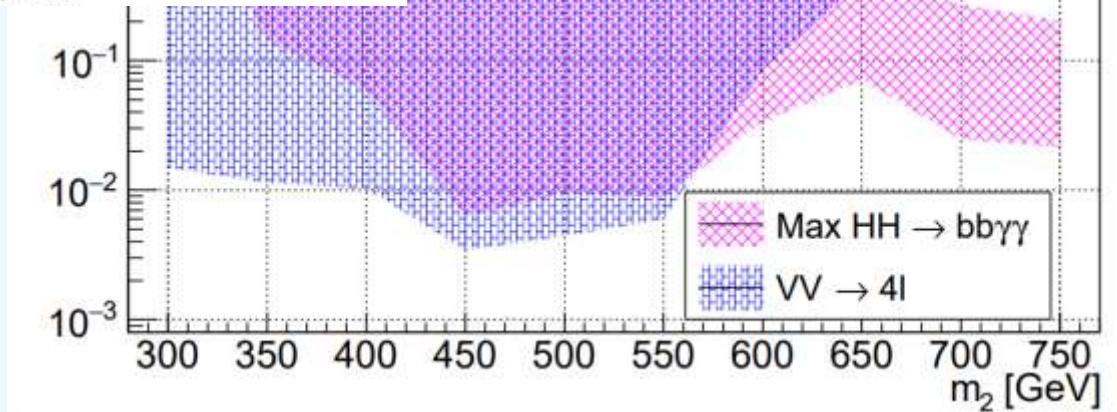
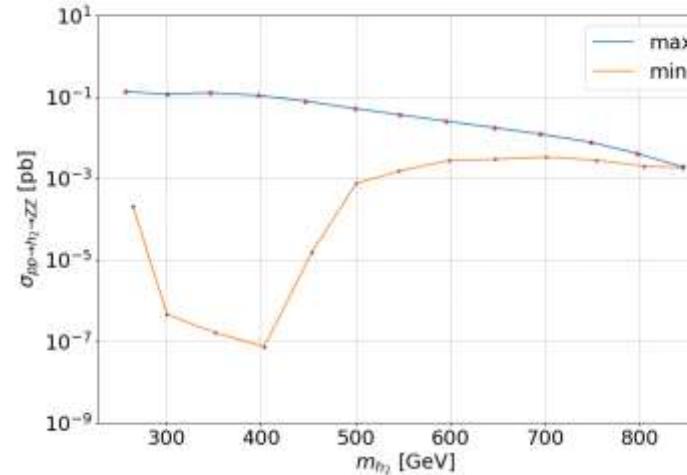
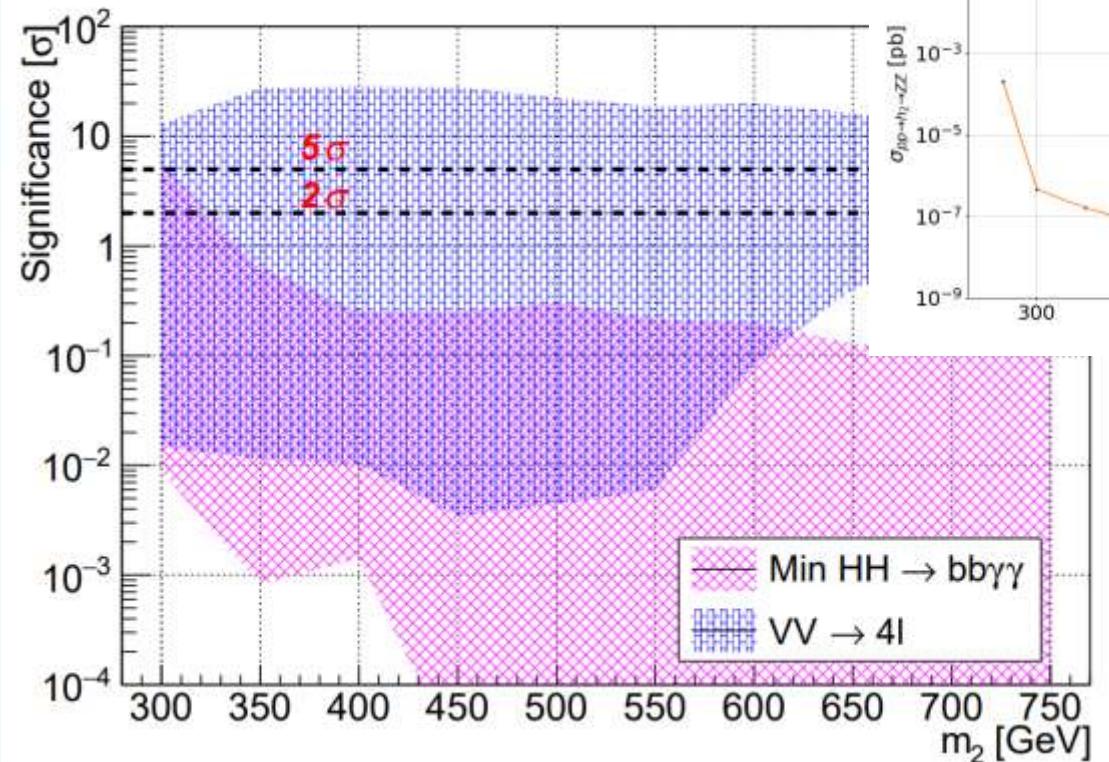


Experiment: Distributions and Efficiency
Simulation: Upper limit cross sections.

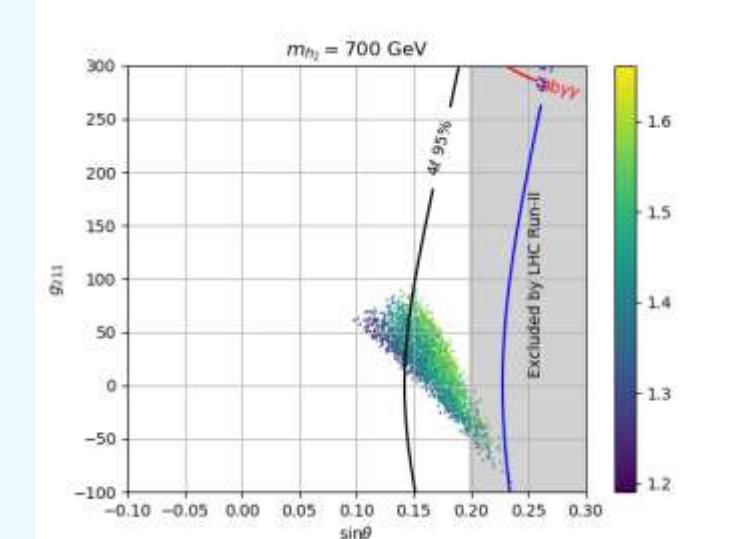
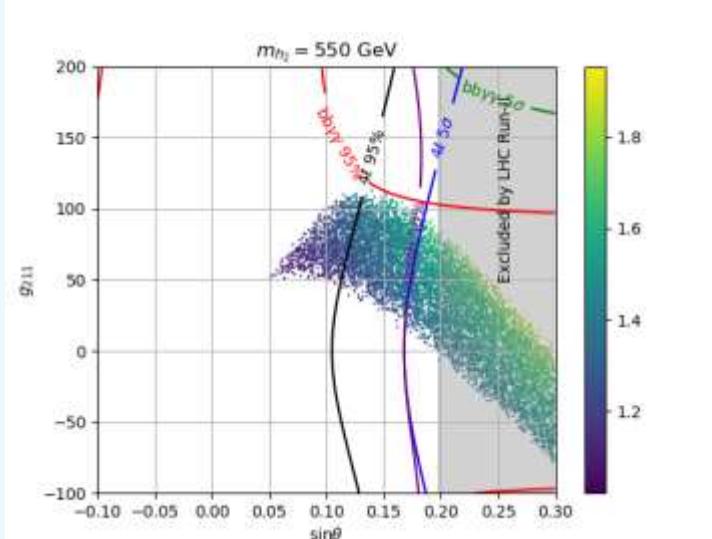
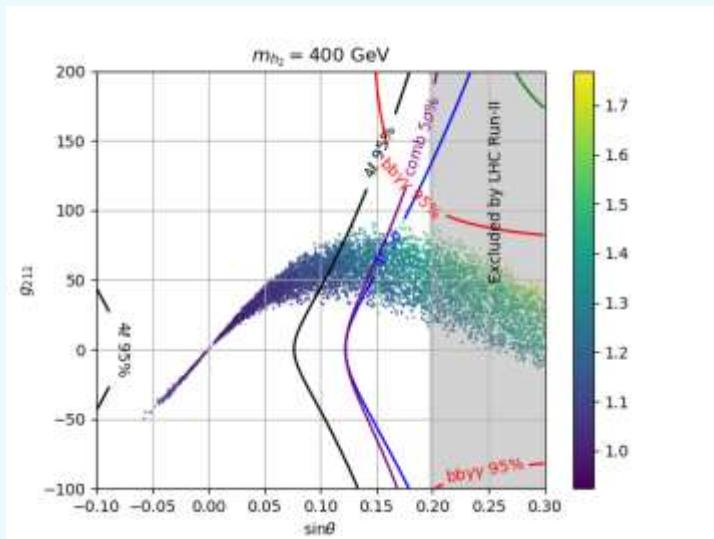
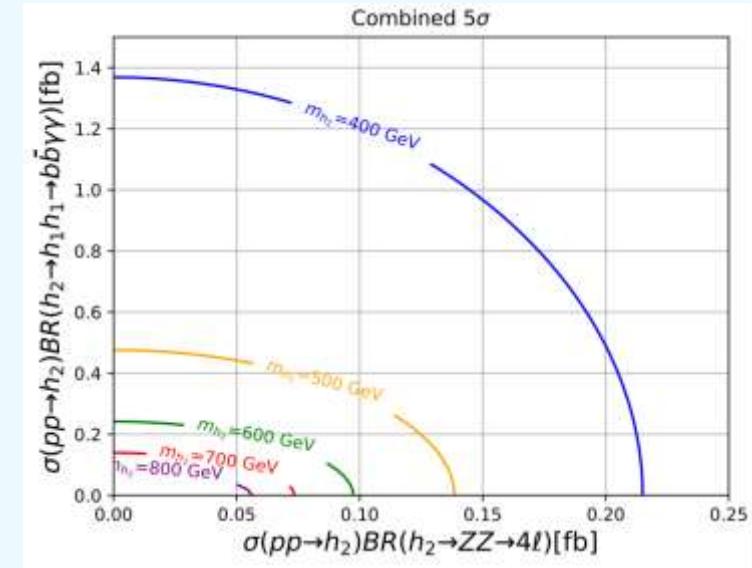
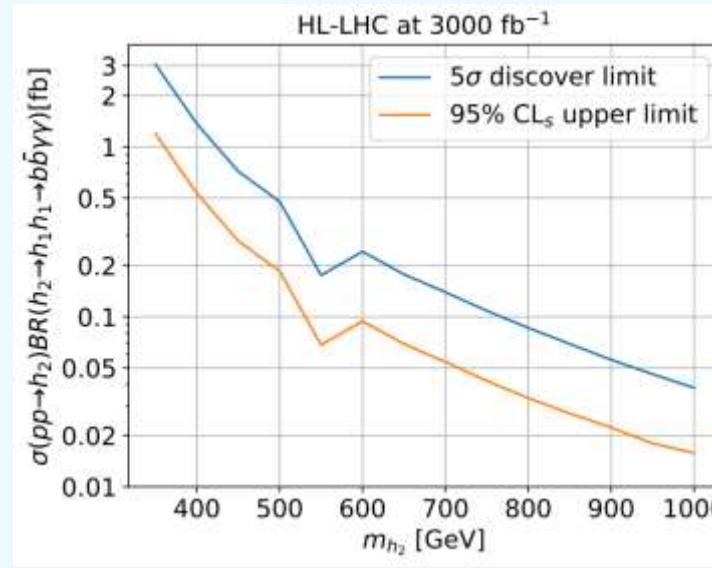
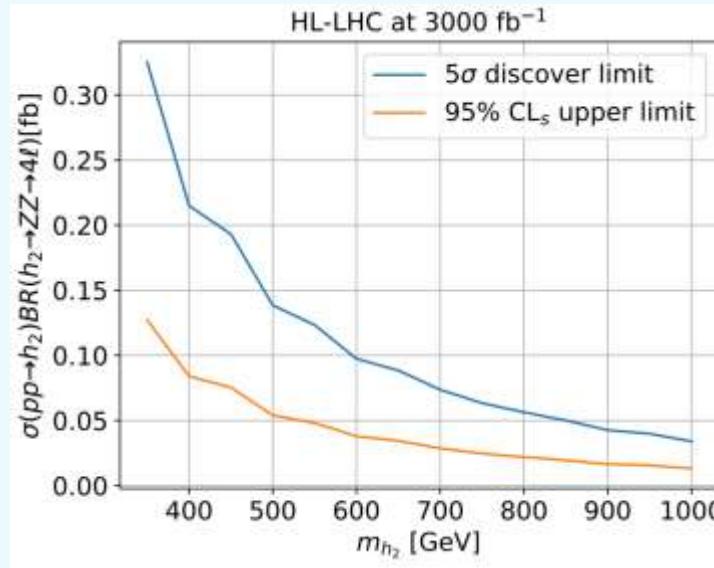
Results: The combined exclusion bound



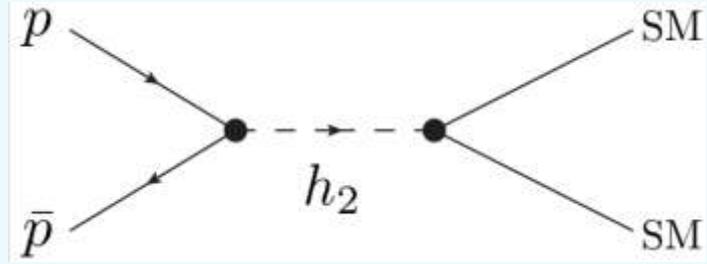
Results: The combined exclusion bound



Combination of channels : $b\bar{b}\gamma\gamma$ and $ZZ \rightarrow 4l$



Open Questions: Test the sign of the mixing angle ?

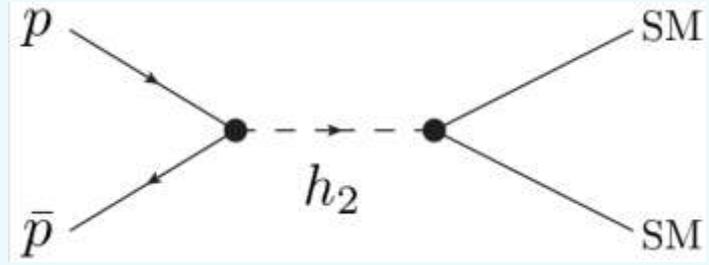


$$h_1 = h \cos \theta + s \sin \theta$$

$$h_2 = s \cos \theta - h \sin \theta$$

Higgs measurement only constrain $\cos^2 \theta$,
but not the sign of θ .

Open Questions: Test the sign of the mixing angle ?

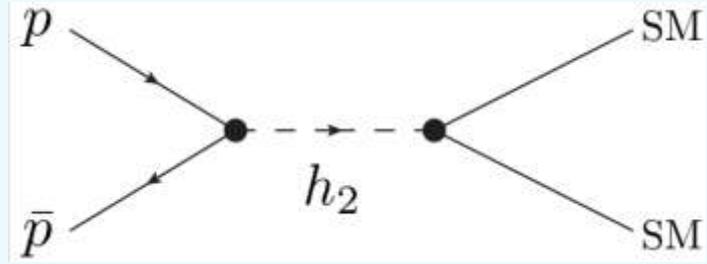


$$h_1 = h \cos \theta + s \sin \theta$$

$$h_2 = s \cos \theta - h \sin \theta$$

What happened in the xSM ?

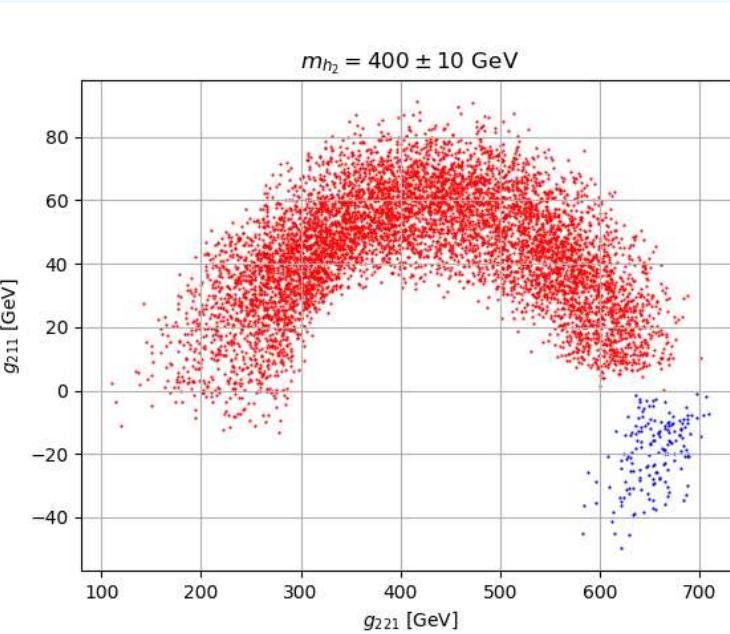
Open Questions: Test the sign of the mixing angle ?



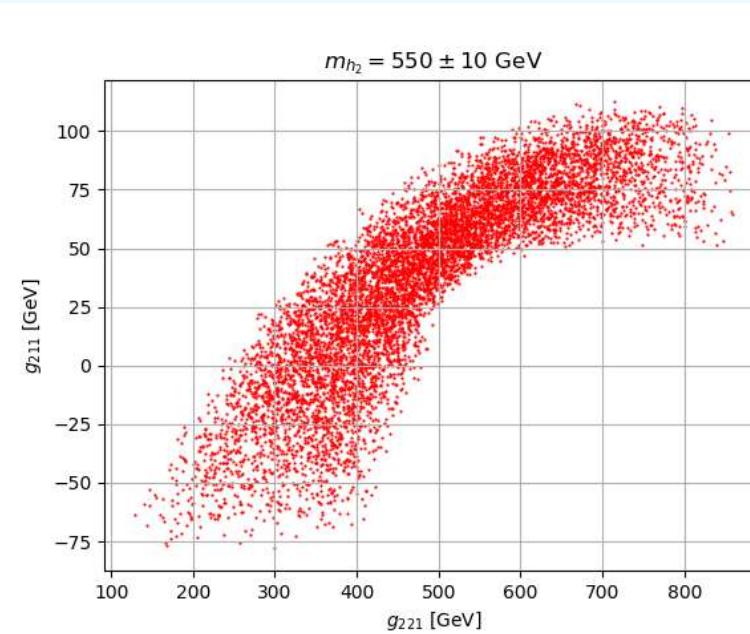
$$h_1 = h \cos \theta + s \sin \theta$$

$$h_2 = s \cos \theta - h \sin \theta$$

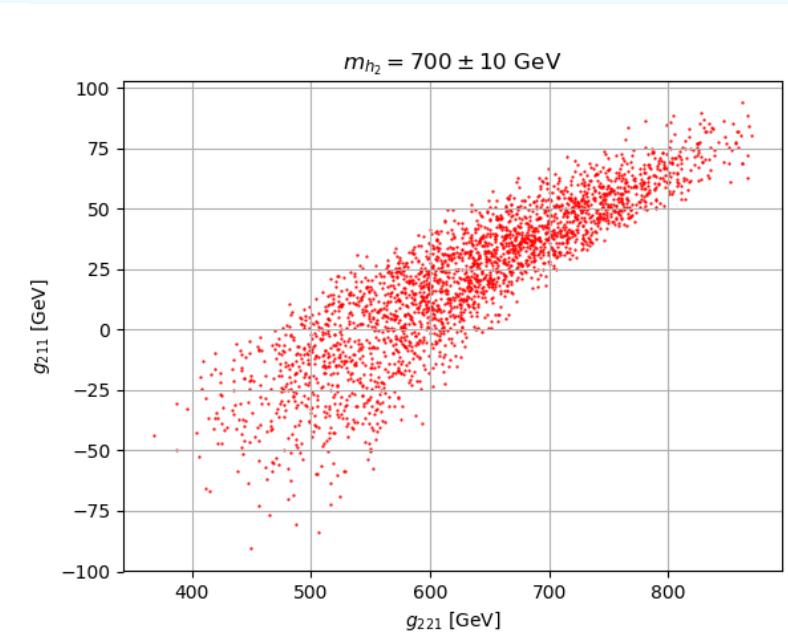
$m_{h_2} = 400 \pm 10 \text{ GeV}$



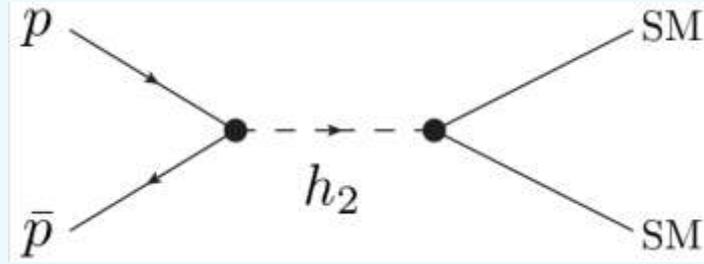
$m_{h_2} = 550 \pm 10 \text{ GeV}$



$m_{h_2} = 700 \pm 10 \text{ GeV}$



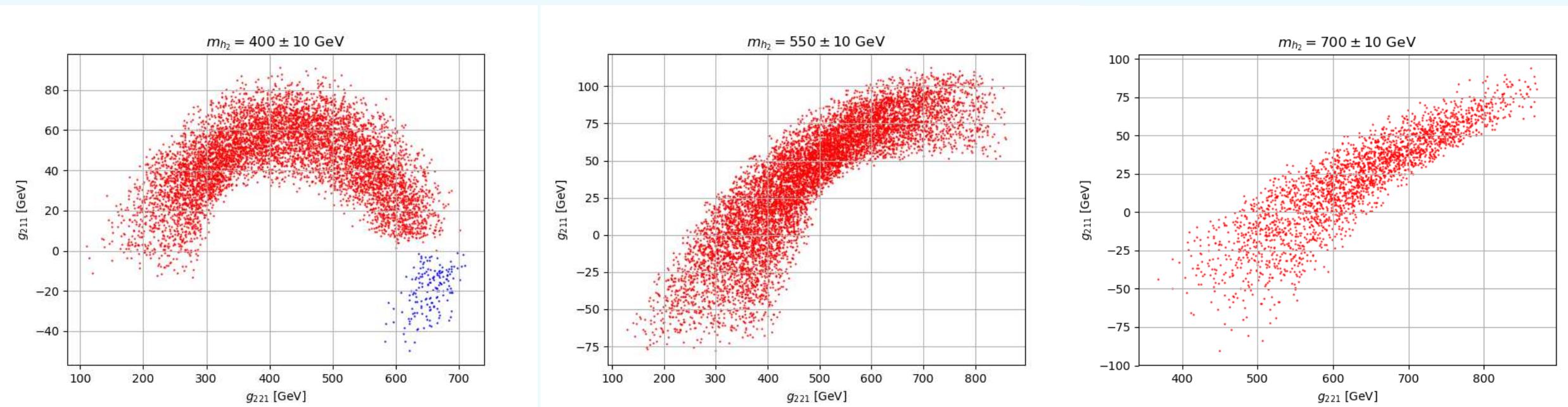
Open Questions: Test the sign of the mixing angle ?



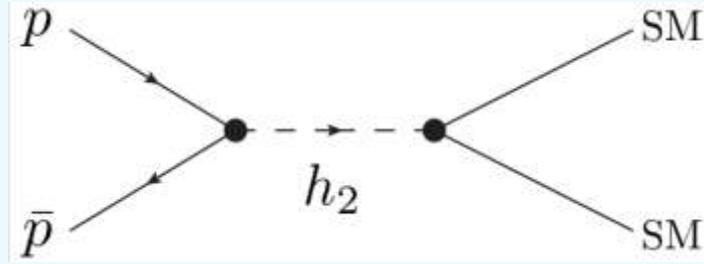
$$h_1 = h \cos \theta + s \sin \theta$$

$$h_2 = s \cos \theta - h \sin \theta$$

$$\sin 2\theta = \frac{(a_1 + 2a_2 x_0)v_0}{m_1^2 - m_2^2}$$



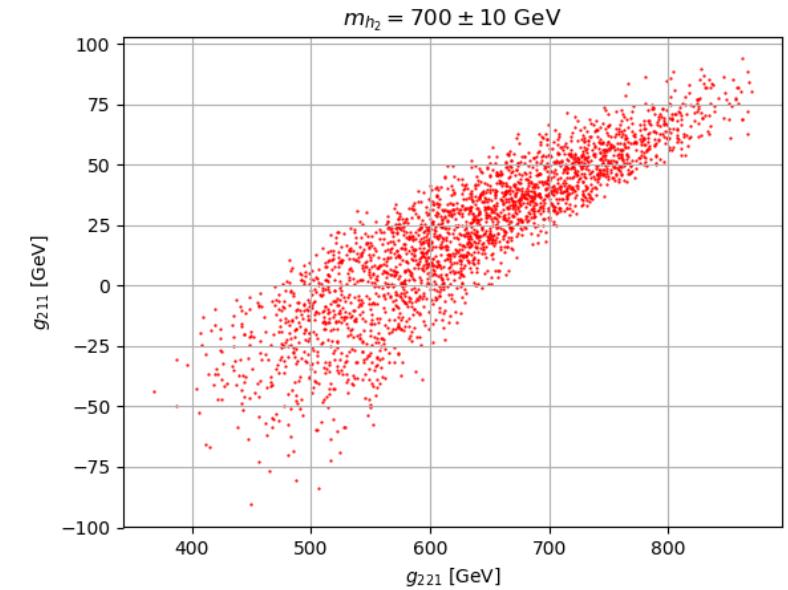
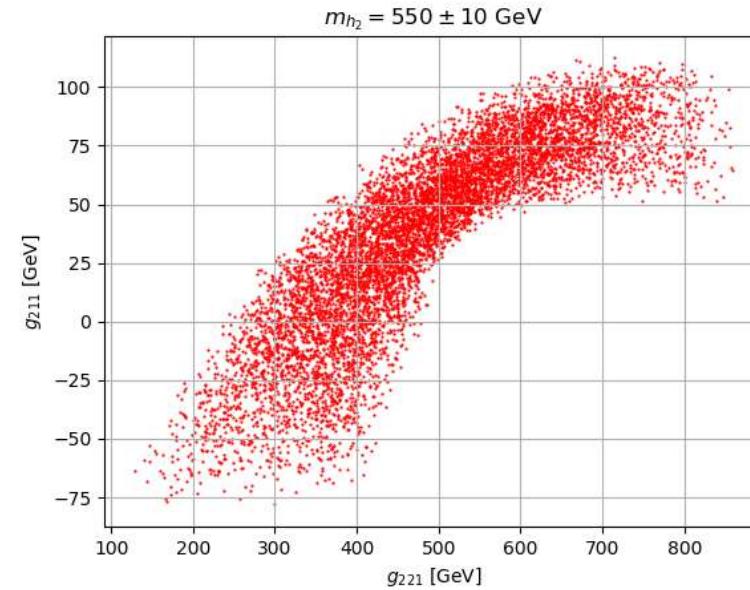
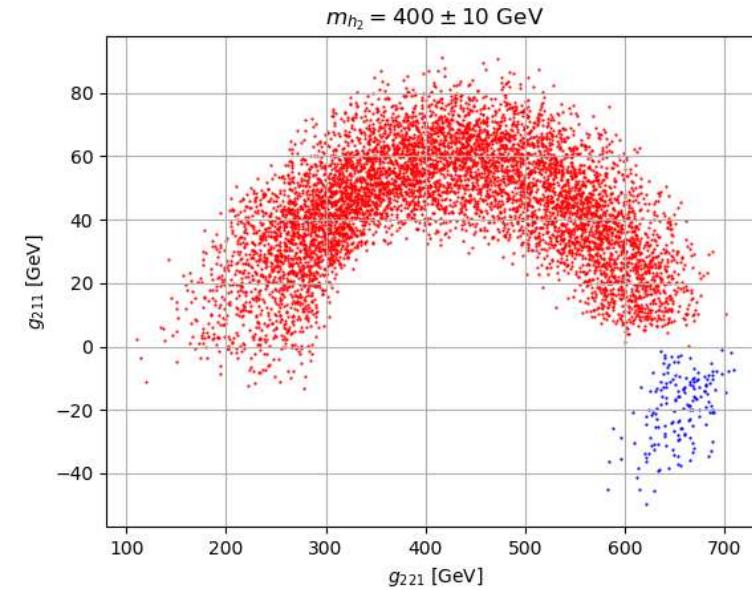
Open Questions: Test the sign of the mixing angle ?



$$h_1 = h \cos \theta + s \sin \theta$$

$$h_2 = s \cos \theta - h \sin \theta$$

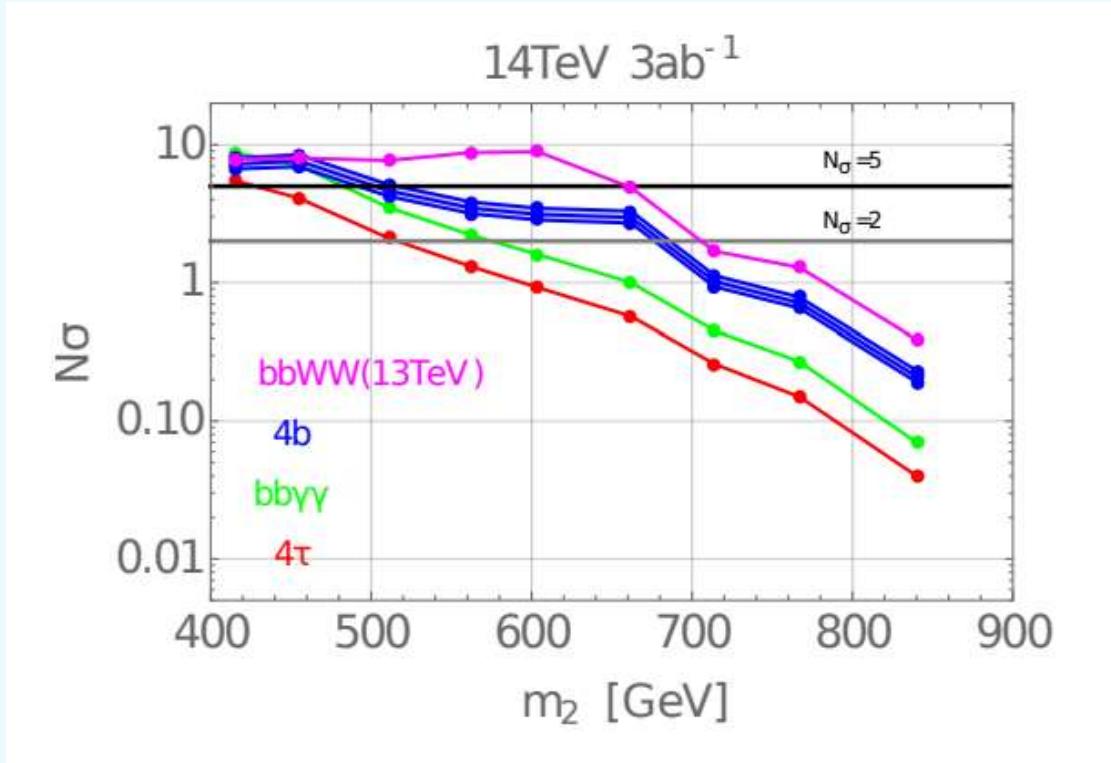
$$g_{211} = \frac{1}{4} [(a_1 + 2a_2 x_0) \cos^3 \theta + 4v_0 (a_2 - 3\lambda) \cos^2 \theta \sin \theta \\ - 2 (a_1 + 2a_2 x_0 - 2b_3 - 6b_4 x_0) \cos \theta \sin^2 \theta - 2a_2 v_0 \sin^3 \theta].$$



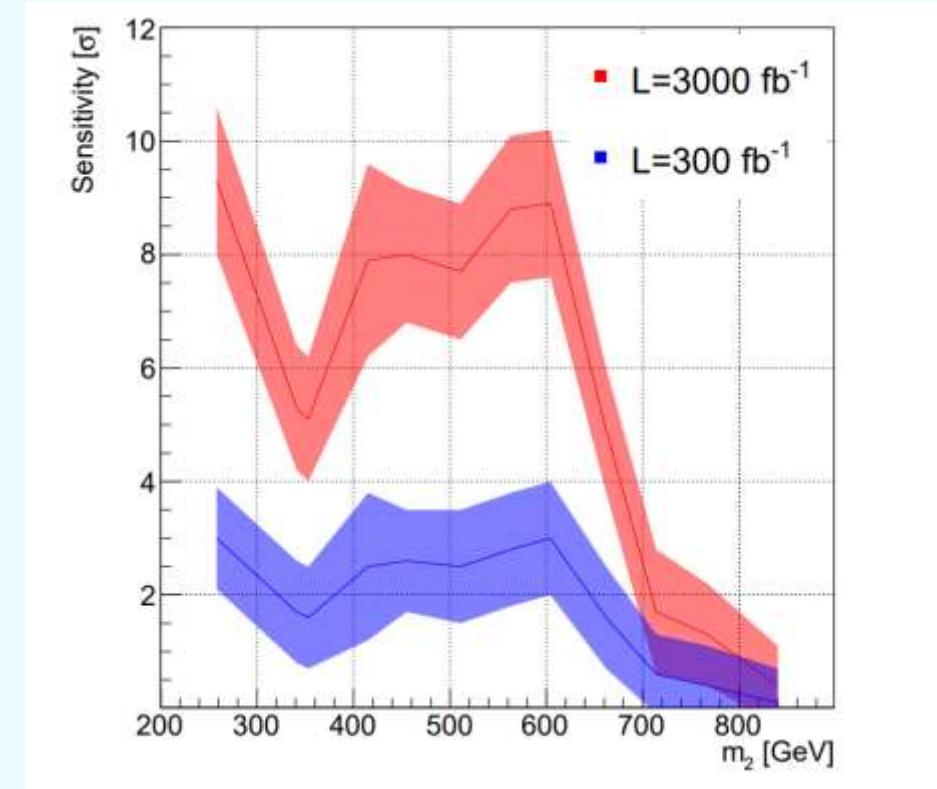
Summary

- We study the SFOEWPT in xSM and searches for heavy resonant di-Higgs production.
- We introduce the current constraints on this model from EWPO, Higgs measurement, vacuum stability...
- We introduce a new scheme to combine the current LHC di-Higgs channels and di-boson channels and show $bb\gamma\gamma$ and $4l$ detection ability.
- SFOEWPT is hard to be probed up to 5σ for $m_{h_2} > 700$ GeV.
- Combination of $bb\gamma\gamma$ and $4l$ can be powerful in low mass region.
- An interesting open question: SFOEWPT prefer positive mixing angle. How to check the sign of the mixing angle in the future?

Review: Single Channel Searches



Phys.Rev.D 100 (2019) 7, 075035
HL, MJRM, SW



Phys.Rev.D 96 (2017) 3, 035007
TH, JMN, LP, MJRM, AS