

Non-Abelian kinetic mixing: transfer CP violation with dark photon

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2023年9月23日

Electroweak baryogenesis

We want to explain baryon asymmetry in our universe (BAU)

$$Y_B \equiv \frac{n_b}{s} = (8.50 \pm 0.11) \times 10^{-11}$$

Sakharov conditions:

- | | | |
|--------------------------------------|----------------------------|---|
| • Baryon number violation | electroweak sphalerons | ✓ |
| • C and CP violation | complex phases | ✗ |
| • Departure from thermal equilibrium | 1st order phase transition | ✗ |

Electroweak baryogenesis

EWPT: 1st order phase transition

The most economic way: introducing additional scalar(s)

singlet

S. Profumo, M. J. Ramsey-Musolf, G. Shaughnessy,
JHEP 08 (2007) 010

doublet

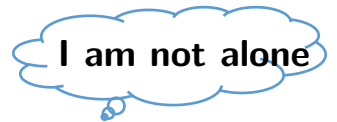
J. M. Cline, P. Lemieux, Phys. Rev. D 55 (1997) 3873

triplet

H. H. Patel, M. J. Ramsey-Musolf, Phys. Rev. D 88 (2013) 035013

leptoquark

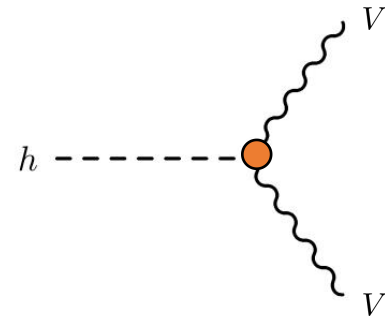
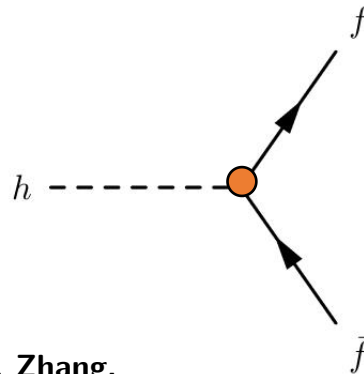
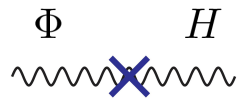
B. Fu, S. F. King, JCAP 05 (2023) 055



Electroweak baryogenesis

CPV: complex phases

anywhere in the SM sector, but mostly studied in

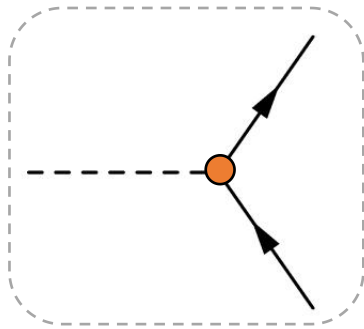


S. Inoue, M. J. Ramsey-Musolf, Y. Zhang,
Phys.Rev.D 89 (2014) 115023

Electroweak baryogenesis

CPV: complex phases

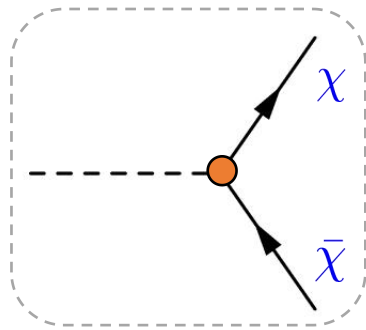
less studied in the extended sector



Electroweak baryogenesis

CPV: complex phases

less studied in the extended sector



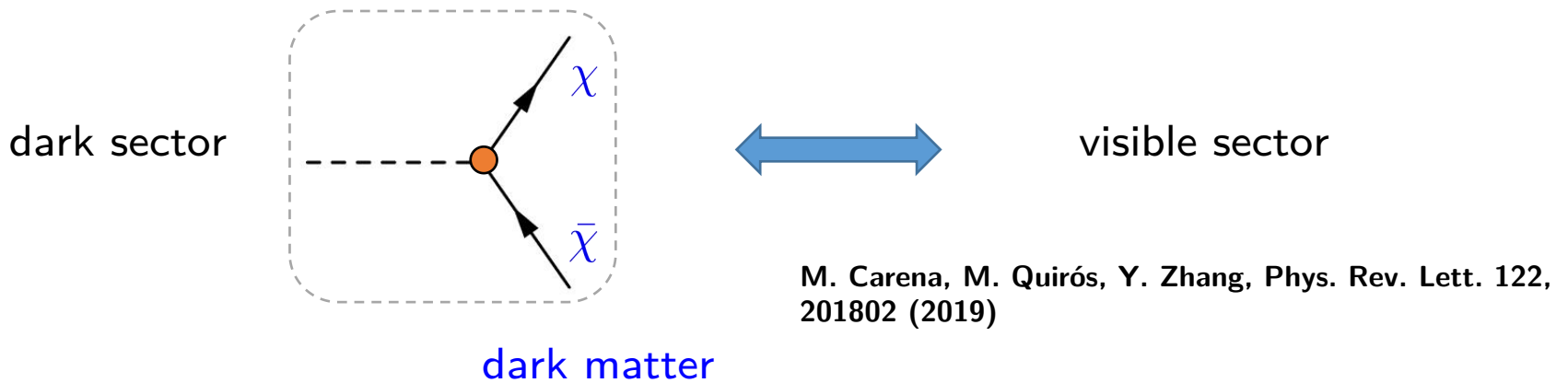
dark matter

M. Carena, M. Quirós, Y. Zhang, Phys. Rev. Lett. 122, 201802 (2019)

Electroweak baryogenesis

CPV: complex phases

less studied in the extended sector

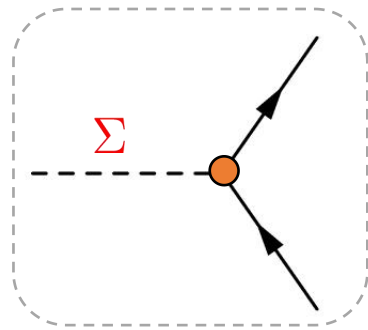


challenge: transfer CP violation from the *dark* sector to the *visible* sector

Electroweak baryogenesis

CPV: complex phases

less studied in the extended sector



real triplet scalar



SM sector

Real triplet scalar

Real triplet scalar (1, 3, 0):

$$\Sigma = \frac{1}{2} \begin{pmatrix} \Sigma^0 & \sqrt{2}\Sigma^+ \\ \sqrt{2}\Sigma^- & -\Sigma^0 \end{pmatrix}$$

Real triplet scalar

Real triplet scalar (1, 3, 0):

$$\Sigma = \frac{1}{2} \begin{pmatrix} \Sigma^0 & \sqrt{2}\Sigma^+ \\ \sqrt{2}\Sigma^- & -\Sigma^0 \end{pmatrix}$$

- dark matter candidate

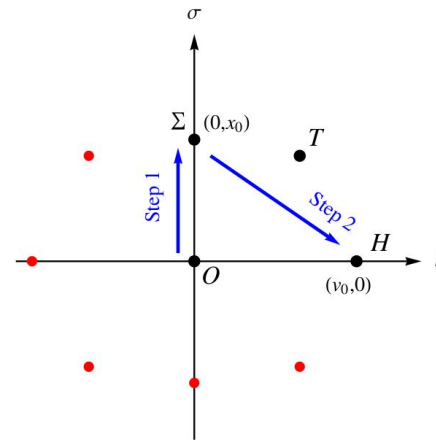
$$\langle \Sigma^0 \rangle = 0$$

M. Cirelli, N. Fornengo and A. Strumia, NPB 753, 178 (2006)
P. Fileviez Pérez, H. H. Patel, M. J. Ramsey-Musolf, K. Wang,
Phys. Rev. D 79 (2009) 055024

- 1st order phase transition

$$\langle \Sigma^0 \rangle = x_0 \rightarrow 0$$

H. H. Patel, M. J. Ramsey-Musolf, Phys. Rev. D 88
(2013) 035013



Real triplet scalar

Real triplet scalar (1, 3, 0):

$$\Sigma = \frac{1}{2} \begin{pmatrix} \Sigma^0 & \sqrt{2}\Sigma^+ \\ \sqrt{2}\Sigma^- & -\Sigma^0 \end{pmatrix}$$

- neutrino masses?

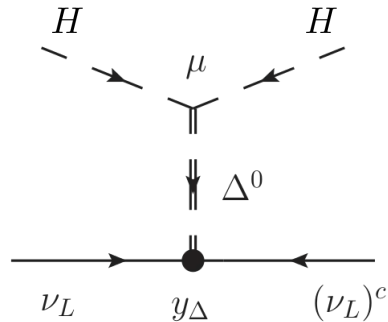
Real triplet scalar

Real triplet scalar (1, 3, 0):

$$\Sigma = \frac{1}{2} \begin{pmatrix} \Sigma^0 & \sqrt{2}\Sigma^+ \\ \sqrt{2}\Sigma^- & -\Sigma^0 \end{pmatrix}$$

- neutrino masses?

In case of a complex triplet scalar (1, 3, 1)



$$\Delta = \begin{pmatrix} \frac{\Delta^+}{\sqrt{2}} & \Delta^{++} \\ \Delta^0 & -\frac{\Delta^+}{\sqrt{2}} \end{pmatrix}$$

$$\mathcal{L} \supset - (Y_\Delta)_{ij} \overline{L}_i^C i\sigma^2 \Delta L_j + \text{h.c.}$$

$$\Delta^0 \rightarrow \langle \Delta^0 \rangle \quad \text{hypercharge: } -1/2 - 1/2 + 1 = 0$$

neutrino mass in type-II seesaw mechanism

Real triplet scalar

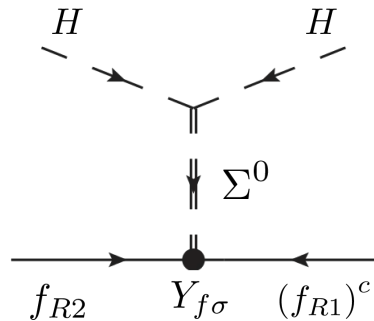
Real triplet scalar (1, 3, 0):

$$\Sigma = \frac{1}{2} \begin{pmatrix} \Sigma^0 & \sqrt{2}\Sigma^+ \\ \sqrt{2}\Sigma^- & -\Sigma^0 \end{pmatrix}$$

- neutrino masses?

$$4 \text{Tr} (\bar{f}_{Ri}^c Y_{f\sigma} \Sigma f_{Rj}) = i Y_{f\sigma} \bar{f}_{Li}^a \Sigma^b f_{Rj}^c \epsilon^{abc}$$

$$Y_{f\sigma 12} \left(\overline{(f_{R1}^+)^c} f_{R2}^+ - \overline{(f_{R1}^-)^c} f_{R2}^- \right) (v_\Sigma + \Sigma^0)$$



$$\Sigma^0 \rightarrow \langle \Sigma^0 \rangle \quad \text{hypercharge: } -1/2 + 1/2 + 0 = 0$$

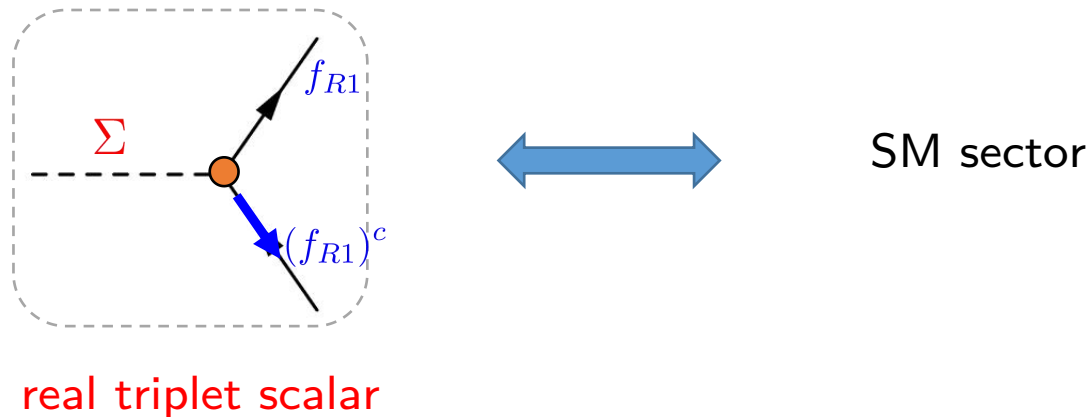
neutrino mass in **type-III** seesaw mechanism

Y. Cheng, X.-G. He, M. J. Ramsey-Musolf, J. Sun, Phys.Rev.D 105 (2022) 095010

Electroweak baryogenesis

CPV: complex phases

less studied in the extended sector



task : **finding a suitable mechanism** to transfer CP violation from the extended sector to the SM sector

Dark photon as a simple extension

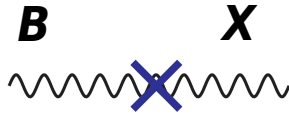
mass	$\approx 2.2 \text{ MeV}/c^2$	$\approx 1.28 \text{ GeV}/c^2$	$\approx 173.1 \text{ GeV}/c^2$	0	$\approx 125.09 \text{ GeV}/c^2$
charge	2/3	2/3	2/3	0	0
spin	1/2	1/2	1/2	1	0
	u up	c charm	t top	g gluon	H Higgs
QUARKS	d down	s strange	b bottom	γ photon	X
	$\approx 0.511 \text{ MeV}/c^2$	$\approx 105.66 \text{ MeV}/c^2$	$\approx 1.7768 \text{ GeV}/c^2$	$\approx 91.19 \text{ GeV}/c^2$	
	-1	-1	-1	0	
	1/2	1/2	1/2	1	
	e electron	μ muon	τ tau	Z Z boson	
LEPTONS	$< 2.2 \text{ eV}/c^2$	$< 1.7 \text{ MeV}/c^2$	$< 15.5 \text{ MeV}/c^2$	$\approx 80.39 \text{ GeV}/c^2$	
	0	0	0	± 1	
	1/2	1/2	1/2	1	
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson	

strong weak EM
 $SU(3)_C \otimes SU(2)_L \otimes U(1)_Y \otimes U(1)_X$
 g W/Z γ X

Dark photon as a simple extension

- kinetic mixing

Abelian case:



$$\mathcal{L} \supset -\frac{1}{4}B_{\mu\nu}B^{\mu\nu} - \frac{1}{4}X_{\mu\nu}X^{\mu\nu} - \frac{\sigma}{2}X_{\mu\nu}B^{\mu\nu}$$

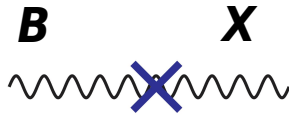
B. Holdom, Phys. Lett. B166, 196 (1986)
R. Foot, X.-G. He Phys.Lett. B267 (1991) 509

- Where does σ comes from?

Dark photon as a simple extension

- kinetic mixing

Abelian case:



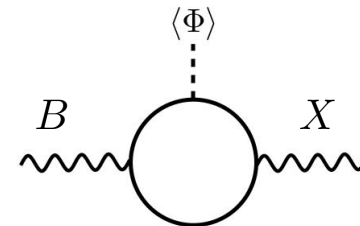
$$\mathcal{L} \supset -\frac{1}{4}B_{\mu\nu}B^{\mu\nu} - \frac{1}{4}X_{\mu\nu}X^{\mu\nu} - \frac{\sigma}{2}X_{\mu\nu}B^{\mu\nu}$$

If $U(1)_x$ is fundamental, σ exists in the UV

If $U(1)_x$ is from other symmetry breaking

B. Holdom, Phys. Lett. B166, 196 (1986)
 R. Foot, X.-G. He Phys.Lett. B267 (1991) 509

- Where does σ comes from?

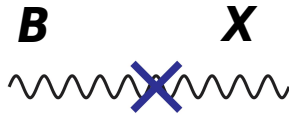


$$\sigma \sim (16\pi^2)^{-1} g_Y g_X$$

Dark photon as a simple extension

- kinetic mixing

Abelian case:



$$\mathcal{L} \supset -\frac{1}{4}B_{\mu\nu}B^{\mu\nu} - \frac{1}{4}X_{\mu\nu}X^{\mu\nu} - \frac{\sigma}{2}X_{\mu\nu}B^{\mu\nu}$$



$$\mathcal{L} \supset -\frac{1}{4}\hat{B}_{\mu\nu}\hat{B}^{\mu\nu} - \frac{1}{4}\hat{X}_{\mu\nu}\hat{X}^{\mu\nu}$$

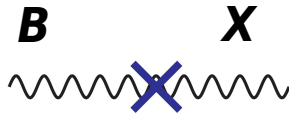
B. Holdom, Phys. Lett. B166, 196 (1986)
R. Foot, X.-G. He Phys.Lett. B267 (1991) 509

- Where does σ go?

Dark photon as a simple extension

- kinetic mixing

Abelian case:



$$\mathcal{L} \supset -\frac{1}{4}B_{\mu\nu}B^{\mu\nu} - \frac{1}{4}X_{\mu\nu}X^{\mu\nu} - \frac{\sigma}{2}X_{\mu\nu}B^{\mu\nu}$$



$$\mathcal{L} \supset -\frac{1}{4}\hat{B}_{\mu\nu}\hat{B}^{\mu\nu} - \frac{1}{4}\hat{X}_{\mu\nu}\hat{X}^{\mu\nu}$$

B. Holdom, Phys. Lett. B166, 196 (1986)
 R. Foot, X.-G. He Phys.Lett. B267 (1991) 509

- Where does σ go?

other terms in the Lagrangian

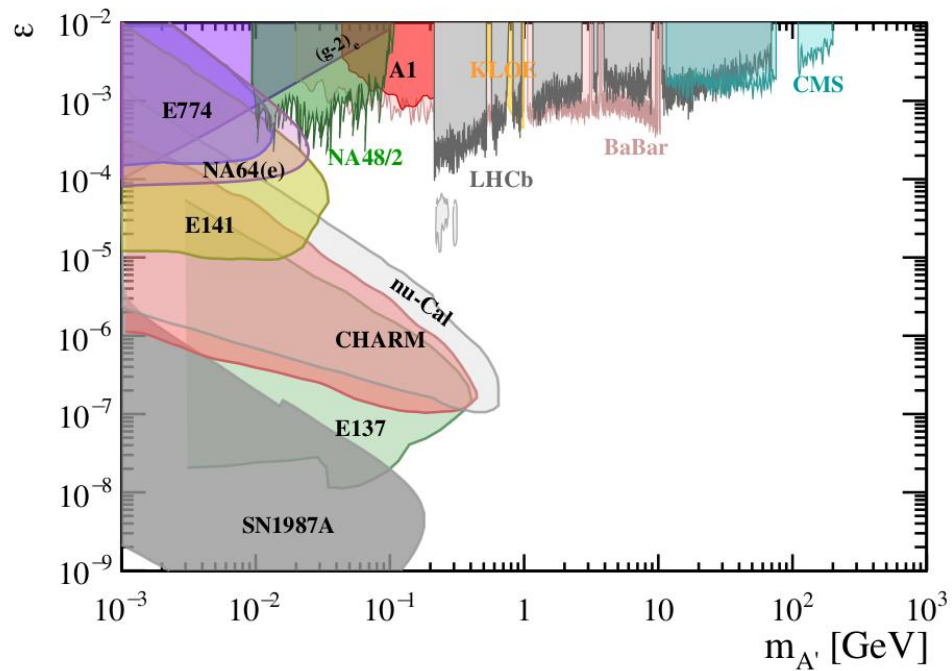
$$\mathcal{L} \supset j_B^\mu B_\mu + j_X^\mu X_\mu$$

Special attention should be paid
 if dark photon is exactly massless

J.-X. Pan, M. He, X.-G. He, **GL**,
 Nucl.Phys.B 953 (2020) 114968

Dark photon as a simple extension

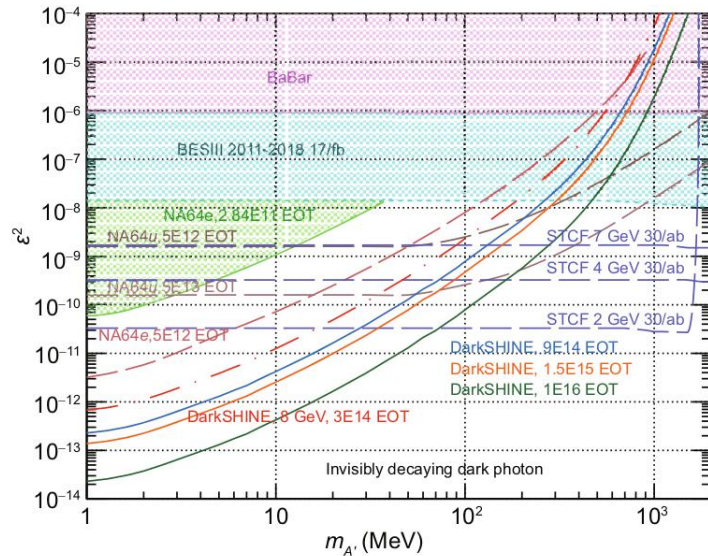
- various constraints and (projected) searches



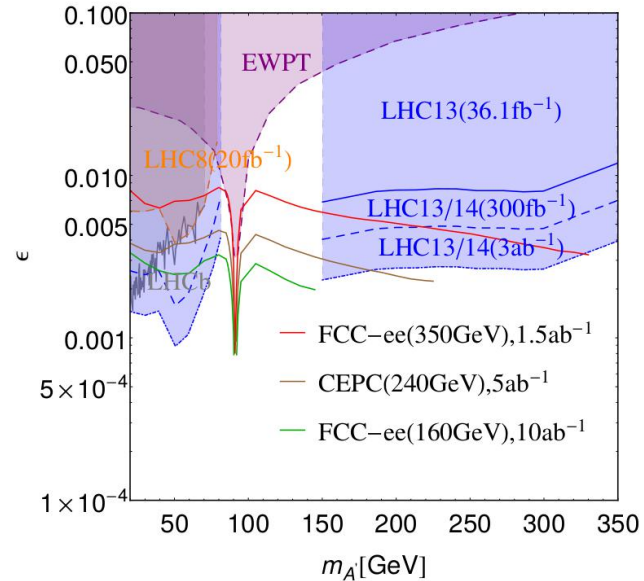
M. Fabbrichesi, E. Gabrielli, G. Lanfranchi, 2005.01515

Dark photon as a simple extension

- various constraints and (projected) searches



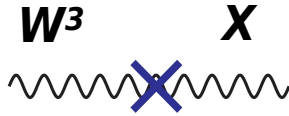
DarkSHINE experiment, Sci.China
Phys.Mech.Astron. 66 (2023) 1, 211062



M. He, X.-G. He, C.-K. Huang, **GL**,
JHEP 03 (2018) 139

Non-Abelian kinetic mixing

- Effective field theory



$$\mathcal{L} \supset -\frac{1}{4} X_{\mu\nu} X^{\mu\nu} - \frac{\beta}{\Lambda} \text{Tr} [W_{\mu\nu} \Sigma] X^{\mu\nu}$$

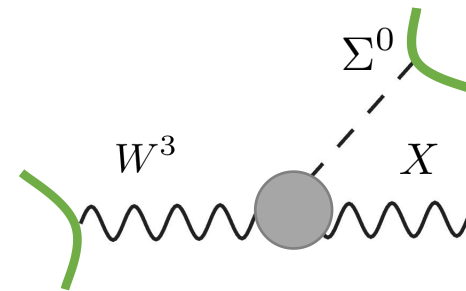
C. A. Argüelles, X.-G. He, G. Ovanessian,
T. Peng, M. J. Ramsey-Musolf,
Phys.Lett. B770 (2017) 101

$$W_{\mu\nu} = W_{\mu\nu}^a \tau^a / 2 \quad \Sigma = \frac{1}{2} \begin{pmatrix} \Sigma^0 & \sqrt{2}\Sigma^+ \\ \sqrt{2}\Sigma^- & -\Sigma^0 \end{pmatrix}$$

- X interacts with the SM only through the non-Abelian kinetic mixing

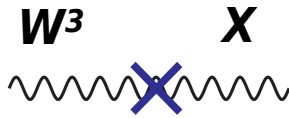
$$\langle \Sigma^0 \rangle = v_\Sigma$$

- Σ can also interact with th SM through the mixing $\Sigma - H$



Non-Abelian kinetic mixing

- Effective field theory



$$\mathcal{L} \supset -\frac{1}{4} X_{\mu\nu} X^{\mu\nu} - \frac{\beta}{\Lambda} \text{Tr} [W_{\mu\nu} \Sigma] X^{\mu\nu} - \frac{\tilde{\beta}}{\Lambda} \text{Tr} [W_{\mu\nu} \Sigma] \tilde{X}^{\mu\nu}$$

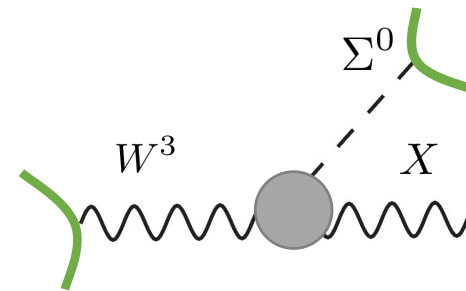
K. Fuyuto, X.-G. He, **GL**, M. J. Ramsey-Musolf, Phys.Rev.D 101 (2020) 075016

$$W_{\mu\nu} = W_{\mu\nu}^a \tau^a / 2 \quad \Sigma = \frac{1}{2} \begin{pmatrix} \Sigma^0 & \sqrt{2}\Sigma^+ \\ \sqrt{2}\Sigma^- & -\Sigma^0 \end{pmatrix}$$

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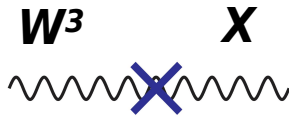
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Non-Abelian kinetic mixing

- Effective field theory



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K. Fuyuto, X.-G. He, **GL**, M. J. Ramsey-Musolf, Phys.Rev.D 101 (2020) 075016

$$W_{\mu\nu} = W_{\mu\nu}^a \tau^a / 2 \quad \Sigma = \frac{1}{2} \begin{pmatrix} \Sigma^0 & \sqrt{2}\Sigma^+ \\ \sqrt{2}\Sigma^- & -\Sigma^0 \end{pmatrix}$$

$$-\frac{\beta}{\Lambda} \text{Tr} [W_{\mu\nu} \Sigma] X^{\mu\nu} - \frac{\tilde{\beta}}{\Lambda} \text{Tr} [W_{\mu\nu} \Sigma] \tilde{X}^{\mu\nu}$$

$$W_{\mu\nu}^3 = \partial_\mu W_\nu^3 - \partial_\nu W_\mu^3 + g\epsilon^{3bc} W_\mu^b W_\nu^c$$

vev

Σ^0

vev (Σ^0)

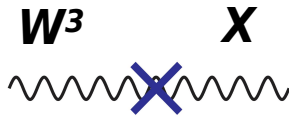
X - W^3 mixing

CPV $\Sigma^0 W^3 X$ int.

CPV $X(\Sigma^0) W^+ W^-$ int.

Non-Abelian kinetic mixing

- Effective field theory



$$\mathcal{L} \supset -\frac{1}{4} X_{\mu\nu} X^{\mu\nu} - \frac{\beta}{\Lambda} \text{Tr} [W_{\mu\nu} \Sigma] X^{\mu\nu} - \frac{\tilde{\beta}}{\Lambda} \text{Tr} [W_{\mu\nu} \Sigma] \tilde{X}^{\mu\nu}$$

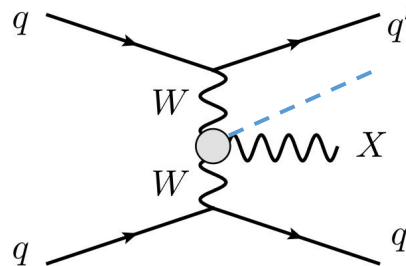
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$$W_{\mu\nu} = W_{\mu\nu}^a \tau^a / 2 \quad \Sigma = \frac{1}{2} \begin{pmatrix} \Sigma^0 & \sqrt{2}\Sigma^+ \\ \sqrt{2}\Sigma^- & -\Sigma^0 \end{pmatrix}$$

Observable:

CPV asymmetry at colliders

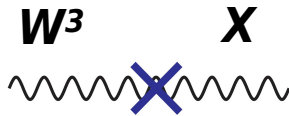
CPV $X(\Sigma^0)W^+W^-$ int.



azimuthal angle distribution: sensitivity is insufficient

Non-Abelian kinetic mixing

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K. Fuyuto, X.-G. He, **GL**, M. J. Ramsey-Musolf, Phys.Rev.D 101 (2020) 075016

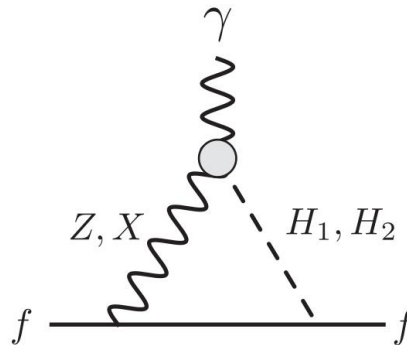
$$W_{\mu\nu} = W_{\mu\nu}^a \tau^a / 2 \quad \Sigma = \frac{1}{2} \begin{pmatrix} \Sigma^0 & \sqrt{2}\Sigma^+ \\ \sqrt{2}\Sigma^- & -\Sigma^0 \end{pmatrix}$$

Observable:

electric dipole moments

$$\mathcal{L}^{\text{EDM}} = -\frac{i}{2} d_f \bar{f} \sigma^{\mu\nu} \gamma_5 f F_{\mu\nu}$$

CPV $\Sigma^0 W^3 X$ int.

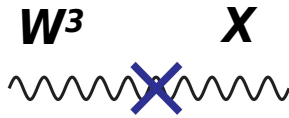


$$\begin{pmatrix} H_1 \\ H_2 \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} h \\ \Sigma^0 \end{pmatrix}$$

$$-\frac{\tilde{\beta}}{2\Lambda} s_W A_{\mu\nu} (c_\theta H_2 + s_\theta H_1) (c_\xi \tilde{X}^{\mu\nu} - s_\xi \tilde{Z}^{\mu\nu})$$

Non-Abelian kinetic mixing

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$$\mathcal{L} \supset -\frac{1}{4} X_{\mu\nu} X^{\mu\nu} - \frac{\beta}{\Lambda} \text{Tr} [W_{\mu\nu} \Sigma] X^{\mu\nu} - \frac{\tilde{\beta}}{\Lambda} \text{Tr} [W_{\mu\nu} \Sigma] \tilde{X}^{\mu\nu}$$

K. Fuyuto, X.-G. He, **GL**, M. J. Ramsey-Musolf, Phys.Rev.D 101 (2020) 075016

Observable:

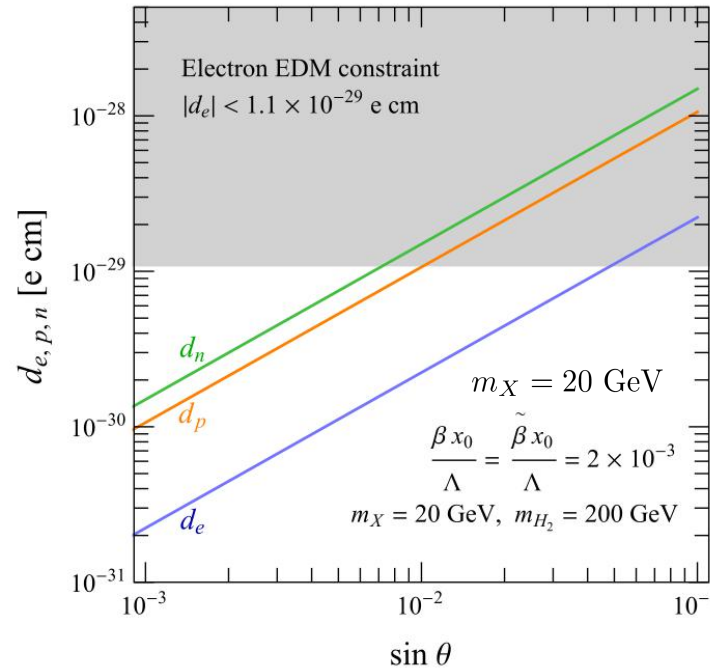
electric dipole moments

$$d_f = \frac{e}{8\pi^2} \frac{m_f}{v} c_\theta s_\theta \left[C_Z V_Z^f f(r_{ZH_1}, r_{ZH_2}) + C_X V_X^f f(r_{XH_1}, r_{XH_2}) \right]$$

$$C_Z = \frac{\tilde{\beta}}{\Lambda} s_W s_\xi, \quad C_X = \frac{\tilde{\beta}}{\Lambda} s_W c_\xi$$

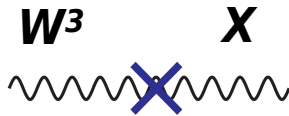
$$V_X = (c_\xi \alpha_{ZX} - s_\xi) v_Z + Q_f \alpha_{AX} c_\xi s_W c_W$$

$$A_X = (c_\xi \alpha_{ZX} - s_\xi) a_Z$$



Non-Abelian kinetic mixing

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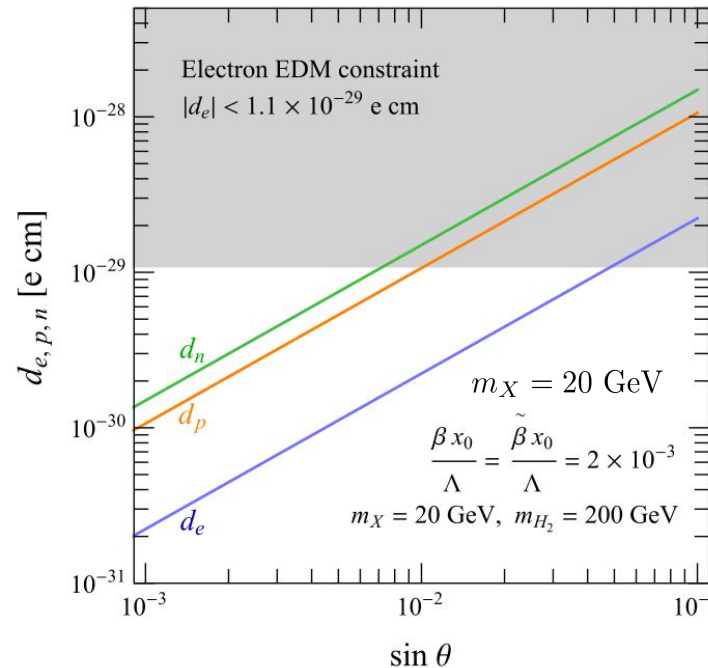
Observable:

electric dipole moments

Feature:

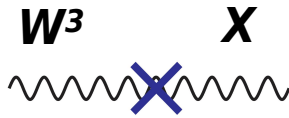
new CPV source is associated to the **light** and weakly coupled new physics

Snowmass 2203.08103



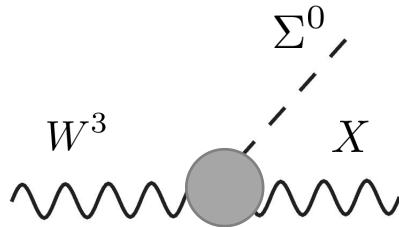
Non-Abelian kinetic mixing

- UV completion



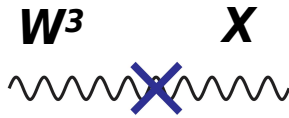
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$$W_{\mu\nu} = W_{\mu\nu}^a \tau^a / 2 \quad \Sigma = \frac{1}{2} \begin{pmatrix} \Sigma^0 & \sqrt{2}\Sigma^+ \\ \sqrt{2}\Sigma^- & -\Sigma^0 \end{pmatrix}$$



Non-Abelian kinetic mixing

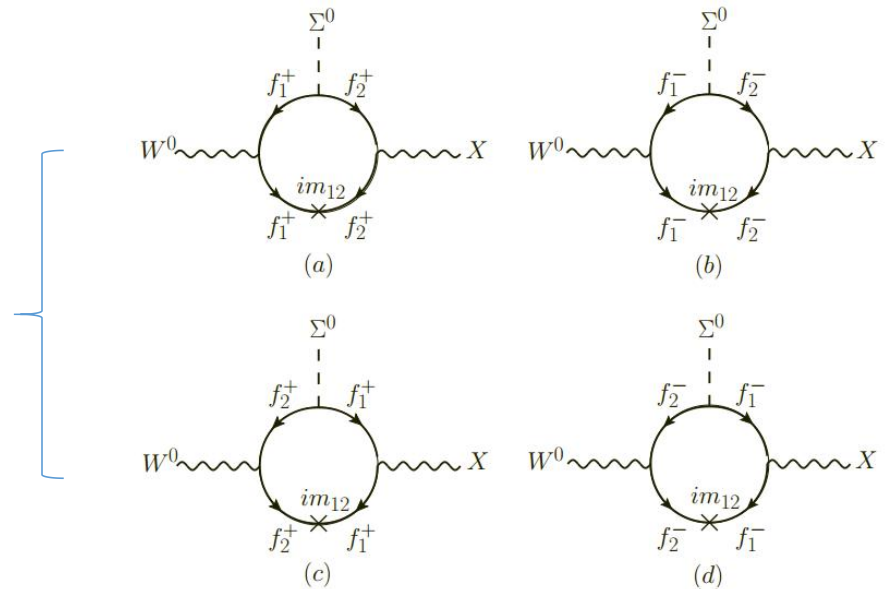
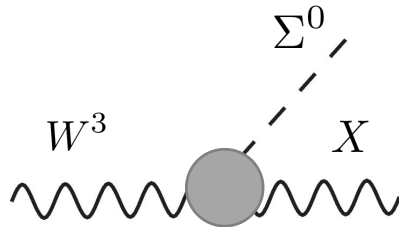
- UV completion



$$\mathcal{L} \supset -\frac{1}{4} X_{\mu\nu} X^{\mu\nu} - \frac{\beta}{\Lambda} \text{Tr} [W_{\mu\nu} \Sigma] X^{\mu\nu} - \frac{\tilde{\beta}}{\Lambda} \text{Tr} [W_{\mu\nu} \Sigma] \tilde{X}^{\mu\nu}$$

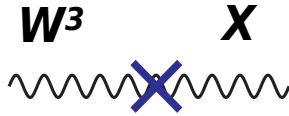
Y. Cheng, X.-G. He, M. J. Ramsey-Musolf, J. Sun, Phys.Rev.D 105 (2022) 095010

$$W_{\mu\nu} = W_{\mu\nu}^a \tau^a / 2 \quad \Sigma = \frac{1}{2} \begin{pmatrix} \Sigma^0 & \sqrt{2}\Sigma^+ \\ \sqrt{2}\Sigma^- & -\Sigma^0 \end{pmatrix}$$



Non-Abelian kinetic mixing

- UV completion



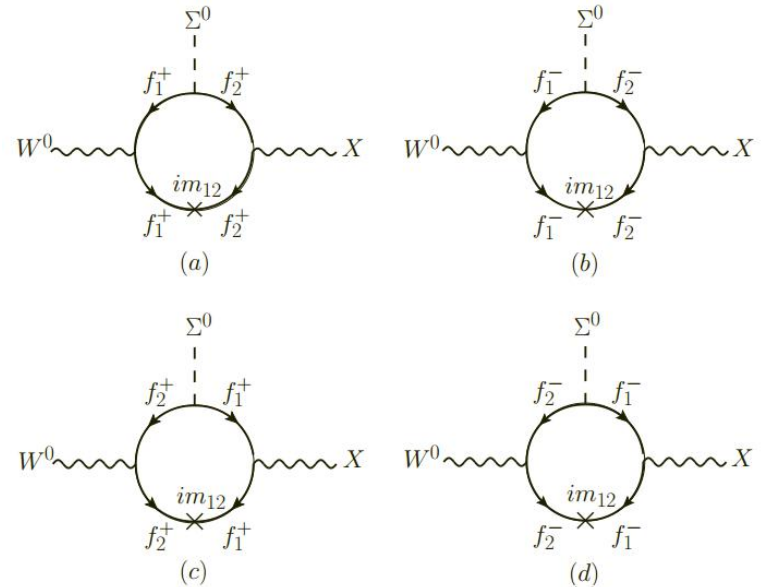
$$\mathcal{L} \supset -\frac{1}{4} X_{\mu\nu} X^{\mu\nu} - \frac{\beta}{\Lambda} \text{Tr} [W_{\mu\nu} \Sigma] X^{\mu\nu} - \frac{\tilde{\beta}}{\Lambda} \text{Tr} [W_{\mu\nu} \Sigma] \tilde{X}^{\mu\nu}$$

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$$W_{\mu\nu} = W_{\mu\nu}^a \tau^a / 2 \quad \Sigma = \frac{1}{2} \begin{pmatrix} \Sigma^0 & \sqrt{2}\Sigma^+ \\ \sqrt{2}\Sigma^- & -\Sigma^0 \end{pmatrix}$$

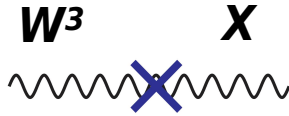
$$\frac{\tilde{\beta}_X}{\Lambda} = \frac{1}{2\pi^2} gg_X x_f \text{Im} (m_{12} Y_{f\sigma}^*) \times [f(m_1, m_2, p_W, p_X) + f(m_2, m_1, p_W, p_X)]$$

$$\frac{\beta_X}{\Lambda} = \frac{1}{2\pi^2} gg_X x_f \text{Re} (m_{12} Y_{f\sigma}^*) \times [f(m_1, m_2, p_W, p_X) + f(m_2, m_1, p_W, p_X)]$$



Non-Abelian kinetic mixing

- UV completion



$$\mathcal{L} \supset -\frac{1}{4} X_{\mu\nu} X^{\mu\nu} - \frac{\beta}{\Lambda} \text{Tr} [W_{\mu\nu} \Sigma] X^{\mu\nu} - \frac{\tilde{\beta}}{\Lambda} \text{Tr} [W_{\mu\nu} \Sigma] \tilde{X}^{\mu\nu}$$

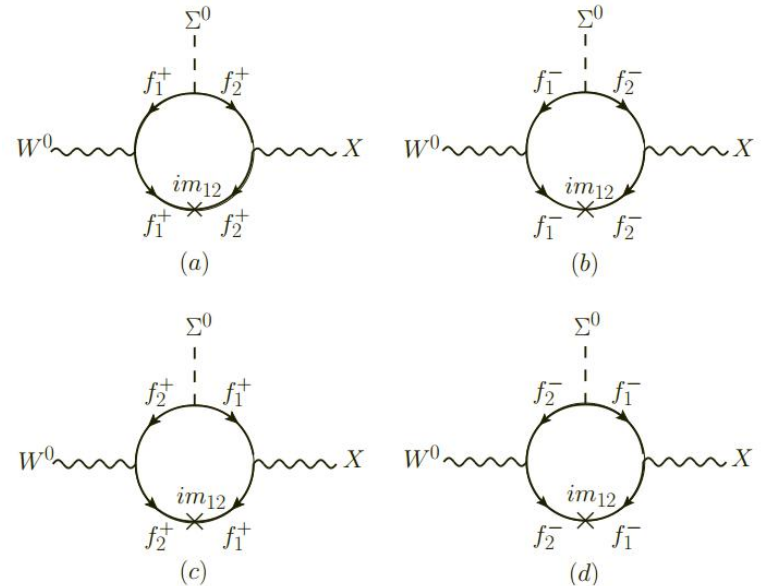
Y. Cheng, X.-G. He, M. J. Ramsey-Musolf, J. Sun, Phys.Rev.D 105 (2022) 095010

$$W_{\mu\nu} = W_{\mu\nu}^a \tau^a / 2 \quad \Sigma = \frac{1}{2} \begin{pmatrix} \Sigma^0 & \sqrt{2}\Sigma^+ \\ \sqrt{2}\Sigma^- & -\Sigma^0 \end{pmatrix}$$

$$\begin{aligned} & -\bar{L}_L Y_e \tilde{H} E_R - \bar{L}_L Y_{fL3} \tilde{H} f_{R3} - \bar{f}_{R1}^c Y_{fs1} S_X f_{R1} \\ & - \bar{f}_{R2}^c Y_{fs2} S_X^\dagger f_{R2} - \bar{f}_{R1}^c m_{12} f_{R2} - \bar{f}_{R3}^c m_{33} f_{R3} \\ & - \bar{Q}_L Y_u H U_R - \bar{Q}_L Y_d \tilde{H} D_R. \end{aligned}$$

Neutrino masses:

$$\begin{aligned} \mathcal{L}_m = & -\frac{1}{2} (\bar{\nu}_L, \bar{\nu}_R^c) \begin{pmatrix} 0 & M_D \\ M_D^T & M_R \end{pmatrix} \begin{pmatrix} \nu_L^c \\ \nu_R \end{pmatrix} \\ & - (\bar{E}_L, \bar{f}_L) \begin{pmatrix} m_e & \sqrt{2}M_D \\ 0 & M_R \end{pmatrix} \begin{pmatrix} E_R \\ f_R \end{pmatrix} \end{aligned}$$



Summary

- Real triplet scalar enables a strong 1st order phase transition
- The CPV interaction between real triplet scalar and triplet leptons can explain neutrino masses
- Non-Abelian kinetic mixing assisted with dark photon can transfer CP violation from the extended sector to the SM sector

