

Gemini dark  
matter

Yu-Cheng QIU

Introduction

Model

Production

Dark radiation

Summary and  
Discussion

## Gemini dark matter

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# I. Introduction

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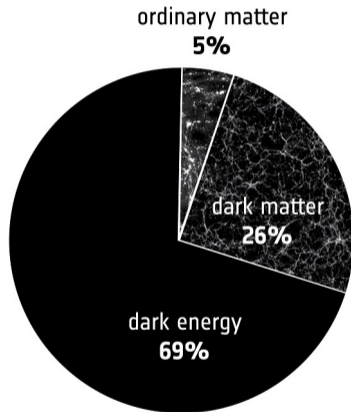


Figure: Copyright: ESA.

- Hubble Tension
- Cosmic Birefringence
- $S_8/\sigma_8$  Tension
  - less dark matter
  - decaying dark matter

- $CDM \rightarrow WDM + \dots$
- The kinetic energy

$$\epsilon \equiv \frac{1}{2} \frac{m_{\text{CDM}}^2 - m_{\text{WDM}}^2}{m_{\text{CDM}}^2}$$

- The lifetime of CDM,  $\tau$ .

Available parameter space:

$$\epsilon \sim \mathcal{O}(0.01) - \mathcal{O}(0.1)$$

$$\tau_8 \sim \mathcal{O}(10^{18}) \text{ s}$$

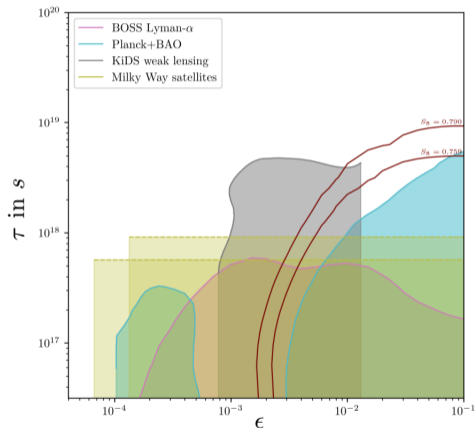


Figure: From 2403.15543 (Fuß, Garny & Ibarra)

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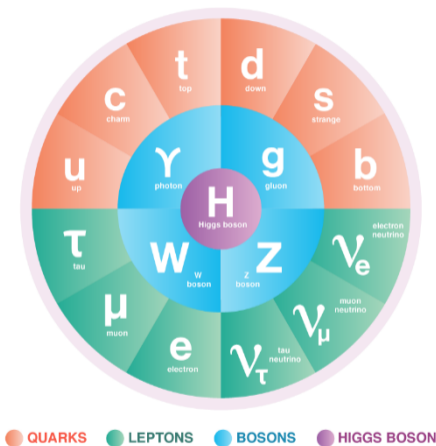
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- Strong CP problem
- Naturalness problem
- Yukawa hierarchy (Why Yukawa couplings are hierarchical?)
  - Landscape (statistical)
  - Clockwork
  - Flavon

Figure: Artwork by Sandbox Studio, Chicago.

Take charged lepton for example,  $m_\tau \gg m_\mu \gg m_e$ .

FN mechanism considers a chiral  $U(1)_{\text{FN}}$ . (Froggatt and Nielsen (1979))

$U(1)_F$  charge:

$$n_{\bar{\ell}_L} = (1, 0.5, 0), \quad n_{e_R} = (4, 1, 0), \quad n_\Phi = -1, \quad n_H = 0.$$

Yukawa operator ' $\bar{\ell} \mathcal{H} e$ ' is not allowed, only

$$-\mathcal{L} \supset g_{ij} \left( \frac{\Phi}{\Lambda} \right)^{n_{ij}} \bar{\ell}_L^i \mathcal{H} e_R^j, \quad n_{ij} = n_{\bar{\ell}_L}^i + n_{e_R}^j, \quad g_{ij} \sim \mathcal{O}(1).$$

$\Phi$  SSB :  $\langle \Phi \rangle / \Lambda \equiv \lambda < 1$  and

$$y_{ij} \equiv g_{ij} \lambda^{n_{ij}} \sim \begin{pmatrix} \lambda^5 & \lambda^2 & \lambda \\ \lambda^{4.5} & \lambda^{1.2} & \lambda^{0.5} \\ \lambda^4 & \lambda & 1 \end{pmatrix} \implies m_\tau \gg m_\mu \gg m_e$$

- DDM that resolves  $S_8$  requires  $\epsilon \sim \mathcal{O}(0.01)$  and  $\tau_8 \sim \mathcal{O}(10^{18})$  s:
  - (i) DM visible decay is constrained by Indirect detection;
  - (ii) Almost degenerate spectrum is rare (without supersymmetry).





Interestingly:

- FN mechanism predicts flavon,  $\Phi$ .  
It couples with fermions:  $g_\Psi \Phi \bar{\Psi} \Psi$ ,  $g_\Psi \sim \mathcal{O}(m_\Psi/\Lambda)$ .  
 $\Phi$  couples to flavor-changing-currents.  
Suppressed decay channel!
- FN mass matrices are almost rank 1.  
Degenerate spectrum can be produced!





Interestingly:

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A decaying dark matter model under the FN mechanism!

## II. Gemini dark matter model

Dark sector lagrangian with chiral  $U(1)_{\text{FN}}$ :

$$\mathcal{L} = i\bar{\chi}_j \bar{\sigma}^\mu \partial_\mu \chi_j - \frac{\beta_{jk}}{2} \frac{\Phi^{n_j+n_k}}{\Lambda^{n_j+n_k-1}} \chi_j \chi_k + \text{h.c.}$$

- $U(1)_{\text{FN}}$  charge:  $\chi_j (n_j)$  and  $\Phi (-1)$ .
- $\Phi$  SSB :  $\Phi = (\langle \Phi \rangle + \phi) e^{ia/f_a}$  and  $\{\phi, a\}$  are flavons.

$$\left(\frac{\Phi}{\Lambda}\right)^n = \lambda^n e^{in\frac{a}{f_a}} \left(1 + n\frac{\phi}{f_a} + \dots\right).$$

- Perform phase rotation  $\chi_j \rightarrow e^{-in_j a/f_a} \chi_j$  to adjust the field space coordinates.
- The lagrangian becomes

$$\mathcal{L} = -\bar{\chi}_j \bar{\sigma}^\mu \partial_\mu \chi_j - \frac{1}{2} m_k \chi_k \chi_k - g_{jk}^\phi \phi \chi_j \chi_k - g_{jk}^a a \chi_j \chi_k + \text{h.c.}$$

The mismatch between **mass-** and **interaction-**eigenstate gives the off-diagonal interactions between flavon and fermions.

$$\mathcal{L} = -\bar{\chi}_j \bar{\sigma}^\mu \partial_\mu \chi_j - \frac{1}{2} m_k \chi_k \chi_k - g_{jk}^\phi \phi \chi_j \chi_k - g_{jk}^a a \chi_j \chi_k + \text{h.c.}$$

$$D = \text{diag}(m_1, m_2, \dots) = U^\top M U$$

$$g^\phi = \frac{1}{2} \text{sym} \left( U^\top \frac{1}{f_a} \frac{\partial(\lambda M)}{\partial \lambda} U \right)$$

$$g^a = \text{sym} \left( \frac{N D}{f_a} \right)$$

$$M_{jk} = \frac{1}{\sqrt{2}} f_a \beta_{jk} \lambda^{n_j + n_k - 1}$$

$$N_{jk} = (U^\dagger)_{ji} n_i U_{ik}$$

$$[\text{sym}(\dots)]_{jk} = (\dots)_{jk} + (\dots)_{kj} - (\dots)_{jj} \delta_{jk}$$

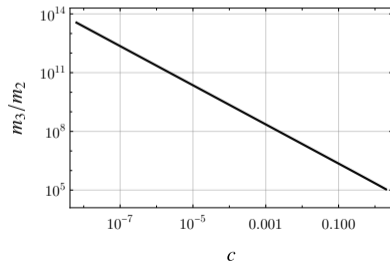
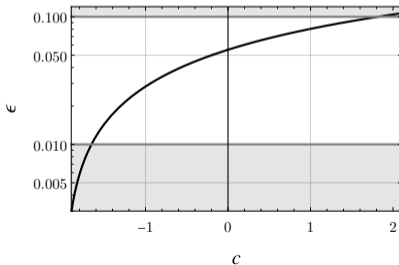
Parametrize couplings as

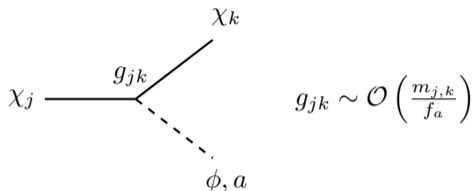
$$g_{jk}^\phi = \frac{1}{f_a} (m_j - m_k + m_j \delta_{jk}) \mathcal{A}_{jk}$$

$$g_{jk}^a = \frac{1}{f_a} (m_j - m_k + m_j \delta_{jk}) \mathcal{B}_{jk}$$

- In the limit of  $\beta_{jk} \rightarrow 1$ ,  $\text{rank}(M) = 1$ .  
 $\implies$  To have a (nearly) degenerate spectrum, one needs at least 3 generations.
- Gemini dark matter:  $\{\chi_1, \chi_2, \chi_3\}$ , with  $m_1 \lesssim m_2 \ll m_3$ .

Take for example,  $n_1 = 4.5 + n_3$ ,  $n_2 = 2.5 + n_3$ , and  $\beta = \begin{pmatrix} 1 & 1 & 1+c \\ 1 & 1 & 1 \\ 1+c & 1 & 1 \end{pmatrix}$ .





$\chi_{1/2}$  are light enough to be stable. So they are DM.

$m_a$  is from explicit breaking of  $U(1)_{FN}$ .

We choose  $m_a = 10^{-6}$  eV to avoid overproduction from misalignment.

$\phi$  is associated with SSB scale, which is heavy. Take  $m_\phi = 10^9$  GeV.

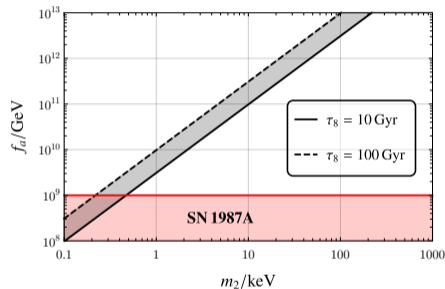
So kinematically,

$$\chi_2 \rightarrow \chi_1 + a, \quad \chi_3 \rightarrow \chi_{1/2} + a, \quad \phi \rightarrow \chi_j + \chi_k$$

The decay  $\chi_2 \rightarrow \chi_1 + a$  explains the  $S_8/\sigma_8$  tension.

- ①  $m_1$  and  $m_2$  are linked by  $\epsilon \simeq 0.05$ .
- ②  $m_{1/2}$  and  $f_a$  are linked by  $\tau_8 \sim \mathcal{O}(10^{18})$  s:

$$m_{1/2} \approx 37 \times \left( \frac{f_a^2}{\tau_8} \right)^{1/3}$$



We call  $\chi_1$  and  $\chi_2$  the twins and  $\chi_3$  as the mother particle.

Free parameters are  $\{f_a, m_3\}$ .

The Gemini DM production has three stages:

- ①  $T \gtrsim m_\phi$ ,  $\phi$  stays in the thermal bath;
- ②  $\chi_3$  freeze in from  $\phi$  decay,  $\phi \rightarrow \chi_3 + \chi_3$ ;

$$Y_3^{\text{f.i.}} \approx 0.3 \times \frac{T_0^3 M_{\text{Pl}}}{s_0 m_\phi} \frac{m_3^2}{f_a^2}$$

- ③  $\chi_{1/2}$  production from  $\chi_3$  decay,  $\chi_3 \rightarrow \chi_{1/2} + a$ . So  $Y_1 + Y_2 \approx Y_3^{\text{f.i.}}$ ,

$$\Omega_{\text{DM}} h^2 = \frac{(\rho_1 + \rho_2) h^2}{3 M_{\text{Pl}}^2 H_0^2} \approx \frac{m_{1/2} Y_3^{\text{f.i.}} s_0 h^2}{3 M_{\text{Pl}}^2 H_0^2} \approx 4 \times \frac{h^2 T_0^3 m_3^2}{H_0^2 M_{\text{Pl}} m_\phi (\tau_8 f_a^4)^{1/3}}$$

Due to the (almost) degeneracy,  $\chi_1$  and  $\chi_2$  are produce together with almost same amount. Thus the name 'Gemini'.



To have the correct DM relic abundance,

$$\Omega_{\text{DM}} h^2 \approx 0.12 \times \left( \frac{m_3}{1.1 \times 10^4 \text{ GeV}} \right)^2 \left( \frac{f_a}{2 \times 10^{10} \text{ GeV}} \right)^{-4/3}$$

Where we have take  $\tau_8 = 10 \text{ Gyr}$  and  $H_0/h = 2.1 \times 10^{-42} \text{ GeV}$ .

For  $f_a = 10^{11}$  GeV,  $m_{1/2} \simeq 10$  keV. (Is it warm?)

For  $f_a = 10^{11}$  GeV,  $m_{1/2} \simeq 10$  keV. (Is it warm?)

Suppose the instantaneous decay of  $\chi_3 \rightarrow \chi_{1/2} + a$ , happens at

$$T_3 \simeq 10^{-3} \times \frac{\sqrt{m_3^3 M_{\text{Pl}}}}{f_a}.$$

The twins  $\chi_{1/2}$  obtain the average momentum  $\langle p \rangle_3 \approx m_3/2$ , which is redshifted to today. The free-streaming scale of the Gemini DM is

$$\lambda_{\text{fs}} \approx \frac{\langle v \rangle_0}{H_0} \approx \frac{\langle p \rangle_0}{H_0 m_{1/2}} \simeq 4.1 \times 10^{-3} \text{ Mpc}/h.$$

Clearly,  $\lambda_{\text{fs}} \ll \mathcal{O}(1) \text{ Mpc}/h$ , the scale of Ly- $\alpha$  constraint.

It is cold.

$a$  is light enough to be relativistic. So they contribute to  $\Delta N_{\text{eff}}$ .

$$\Delta N_{\text{eff}} = \frac{8}{7} \left( \frac{11}{4} \right)^{4/3} \frac{\rho_a^{\text{th}} + \Delta \rho_a}{\rho_\gamma} \Big|_{\text{rec}}$$

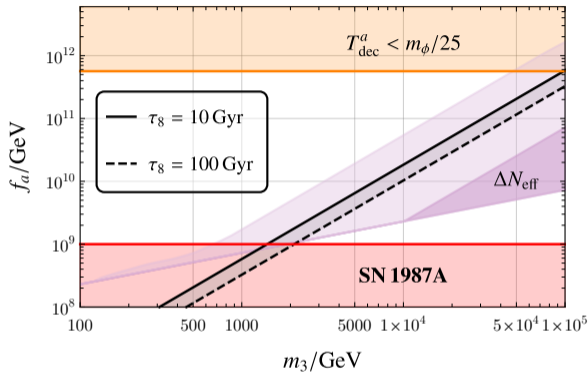
There are two possible production channels of such radiation:

- ① thermal freeze out,  $\rho_a^{\text{th}} \implies \Delta N_{\text{eff}} \geq 0.028$ ;
- ② parturition process  $\chi_3 \rightarrow \chi_{1/2} + a$ ,  $\Delta \rho_a$ .

SM prediction  $(N_{\text{eff}})_{\text{SM}} \approx 3.044$ .

Planck collaboration gives  $(N_{\text{eff}})_{\text{P18}} = 2.88^{+0.44}_{-0.42}$ .

$$\Delta N_{\text{eff}} = (N_{\text{eff}})_{\text{P18}} - (N_{\text{eff}})_{\text{SM}} \leq 0.276$$



**Figure:** Benchmark model:  $m_a = 10^{-6} \text{ eV}$ ,  $m_\phi = 10^9 \text{ GeV}$  and  $\epsilon = 0.05$ .  is the range where  $\Delta N_{\text{eff}} > 0.276$  and  is where  $\Delta N_{\text{eff}} > 0.04$ . The sensitivity of future CMB-S4 could reach  $\Delta N_{\text{eff}} \sim 0.02$ .  indicates where radiation from  $\phi \rightarrow a + a$  cannot be thermalized.

# III. Summary and discussion

- We propose the Gemini dark matter model to explain the  $S_8/\sigma_8$  tension.
  - The dark matter couple to the flavon that explains the Yukawa hierarchy.
  - Flavon provides the decay channel for  $S_8/\sigma_8$  and DM production channel.
- The cry of the twins during parturition (dark radiation) is predicted and can be probed in the future CMB-S4.

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- Gemini DM could be the sterile neutrino.
- Light flavon indicates fifth force.
- Extremely light flavon( $a$ ) can be used to explain the cosmic birefringence.



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# Thank you!

Consider  $n_1 = 4.5 + n_3$ ,  $n_2 = 2.5 + n_3$  and  $\beta = \begin{pmatrix} 1 & 1 & 1+c \\ 1 & 1 & 1 \\ 1+c & 1 & 1 \end{pmatrix}$ .

Only  $c$  will affect the mixing patterns. Parametrize the coupling as

$$g_{jk}^\phi = \frac{1}{f_a} (m_j - m_k + m_j \delta_{jk}) \mathcal{A}_{jk}$$

$$g_{jk}^a = \frac{1}{f_a} (m_j - m_k + m_j \delta_{jk}) \mathcal{B}_{jk}.$$

$(ij)$	$ \mathcal{A}_{ij} ^2$	$ \mathcal{B}_{ij} ^2$
(11)	$6.64_{-0.47}^{+0.49} \times 10^3$	$48.6_{-0.4}^{+0.4}$
(22)	$6.76_{-0.48}^{+0.48} \times 10^3$	$49.4_{-0.4}^{+0.3}$
(33)	$1.57 \times 10^3 \pm 10^{-3}$	$12.3 \pm 10^{-5}$
(21)	$1.37 \times 10^2 \pm 10^{-1}$	$0.999_{-0.002}^{+0.001}$
(31)	$5.77_{-0.88}^{+0.95} \times 10^{-2}$	$4.21_{-0.65}^{+0.70} \times 10^{-4}$
(32)	$6.79_{-0.99}^{+1.11} \times 10^{-2}$	$4.98_{-0.75}^{+0.79} \times 10^{-4}$

Statistics of matrix elements  $|\mathcal{A}_{ij}|^2$  and  $|\mathcal{B}_{ij}|^2$  with  $\epsilon \in (0.01, 0.1)$ , and randomly sampled  $c$  under uniform distribution.

Central values are averages. The upper and the lower uncertainties indicate the maximum and the minimum.

$\phi$  coupled to SM in the form  $\lambda^n \frac{\phi}{f_a} \bar{Q} \mathcal{H} q$ , which leads to

$$\phi + \mathcal{H} \rightarrow \bar{Q} + q, \quad \phi + Q \rightarrow \mathcal{H} + q, \quad \phi + q \rightarrow \mathcal{H} + Q.$$

The amplitudes are  $|\mathcal{M}|^2 = \frac{\lambda^2}{f_a^2} (2p_Q p_q)$ . (take  $n = 1$  for leading contribution)  
 The Boltzmann equation for  $\phi$  is

$$\begin{aligned} \dot{n}_\phi + 3Hn_\phi &= -\tilde{\Gamma}_\phi (n_\phi - n_\phi^{\text{eq}}) \\ \tilde{\Gamma}_\phi &= \langle \sigma_{\mathcal{H}V} \rangle n_{\mathcal{H}}^{\text{eq}} + \langle \sigma_{QV} \rangle n_Q^{\text{eq}} + \langle \sigma_{qV} \rangle n_q^{\text{eq}} \end{aligned}$$

Decoupling temperatures are

$$3H(T_{\text{dec}}^a) = \tilde{\Gamma}_a(T_{\text{dec}}^a), \quad 3H(T_{\text{dec}}^\phi) = \tilde{\Gamma}_\phi(T_{\text{dec}}^\phi)$$

Take  $\{\mathcal{H}, Q, q\}$  massless.

$$\begin{aligned}
 \tilde{\Gamma}_\phi &= \langle \sigma_{\mathcal{H}V} \rangle n_{\mathcal{H}}^{\text{eq}} + \langle \sigma_{QV} \rangle n_Q^{\text{eq}} + \langle \sigma_{qV} \rangle n_q^{\text{eq}} \\
 &\approx \frac{1}{n_\phi^{\text{eq}}} \int \prod_j \frac{g_j d^3 p_j}{(2\pi)^3 (2E_j)} \frac{\lambda^2}{f_a^2} (2p_Q p_q + 2p_{\mathcal{H}} p_q + 2p_Q p_{\mathcal{H}}) \\
 &\quad \times (2\pi)^4 \delta^4(p_\phi + p_{\mathcal{H}} - p_Q - p_q) e^{-(E_\phi + E_{\mathcal{H}})/T} \\
 &= \frac{g_{\mathcal{H}} g_Q g_q \lambda^2}{16(2\pi)^3} \frac{T^5}{f_a^2 m_\phi^2} \frac{\mathcal{I}(m_\phi/T)}{K_2(m_\phi/T)} \\
 \mathcal{I}(\zeta) &= \int_\zeta^\infty d\xi (\xi^2 - \zeta^2)(2\xi^2 - \zeta^2) K_1(\xi)
 \end{aligned}$$

The interaction rate for  $a$  is obtained by taking massless limit of  $\tilde{\Gamma}_\phi$ ,

$$\tilde{\Gamma}_a \approx \frac{g_{\mathcal{H}} g_Q g_q \lambda^2}{(2\pi)^3} \frac{T^3}{f_a^2}.$$

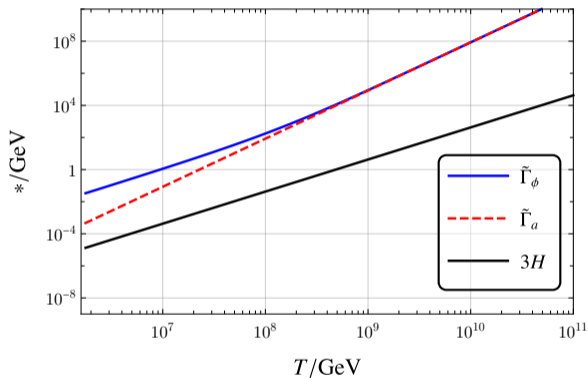


Figure: Here  $f_a = 2 \times 10^{11}$  GeV and  $m_\phi = 10^9$  GeV. So  $T_{\text{dec}}^a \approx 5 \times 10^4$  GeV.