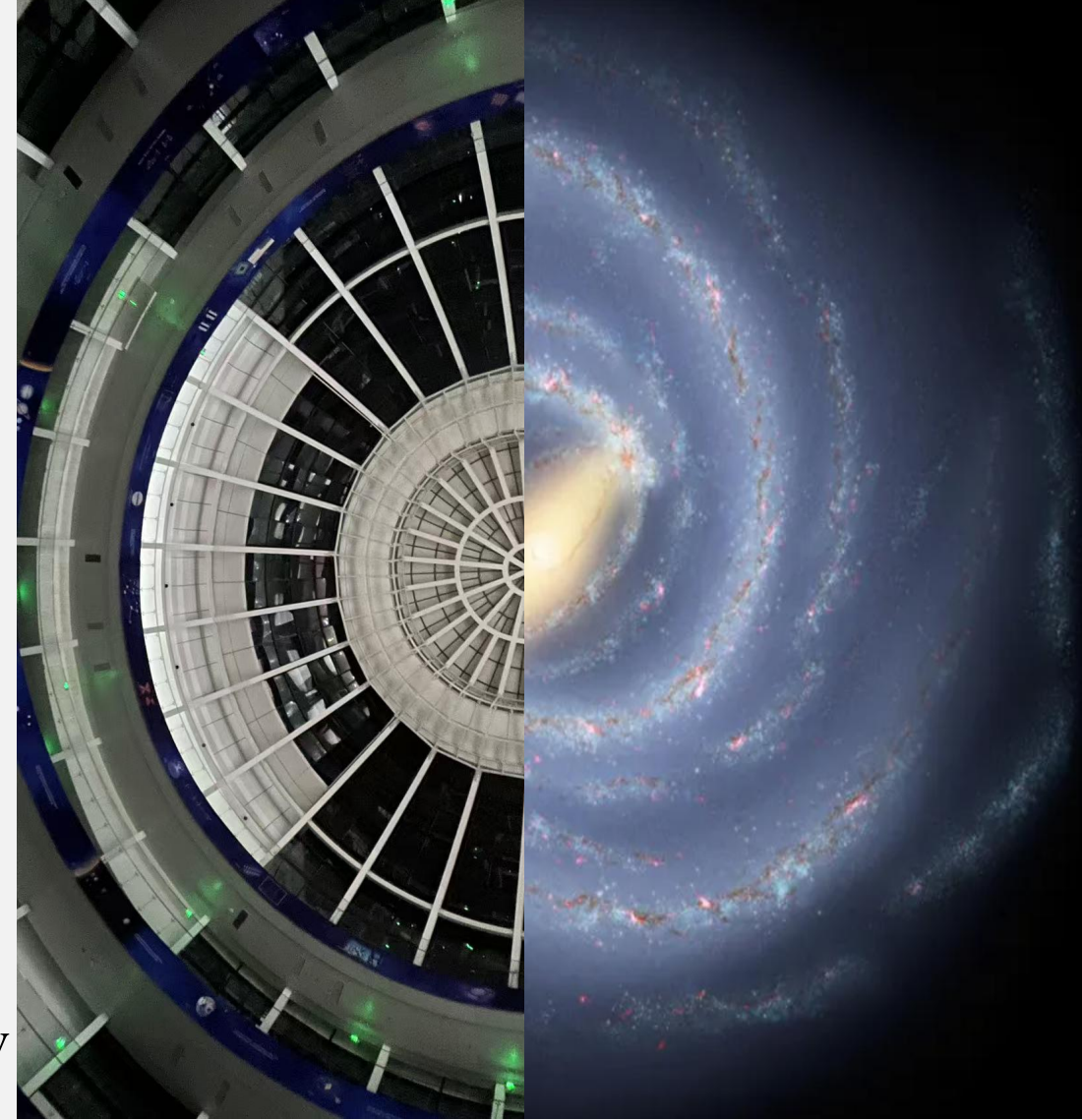


Testing Neutrino Mass Origins with Supernova Neutrinos

Chui-Fan Kong

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Tsung-Dao Lee Institute, Shanghai Jiao Tong University



arXiv:2404.17352 [hep-ph], PRL 133 (2024) 12, 121802

In collaboration with: Shao-Feng Ge & Alexei Y. Smirnov



李政道研究所
TSUNG-DAO LEE INSTITUTE

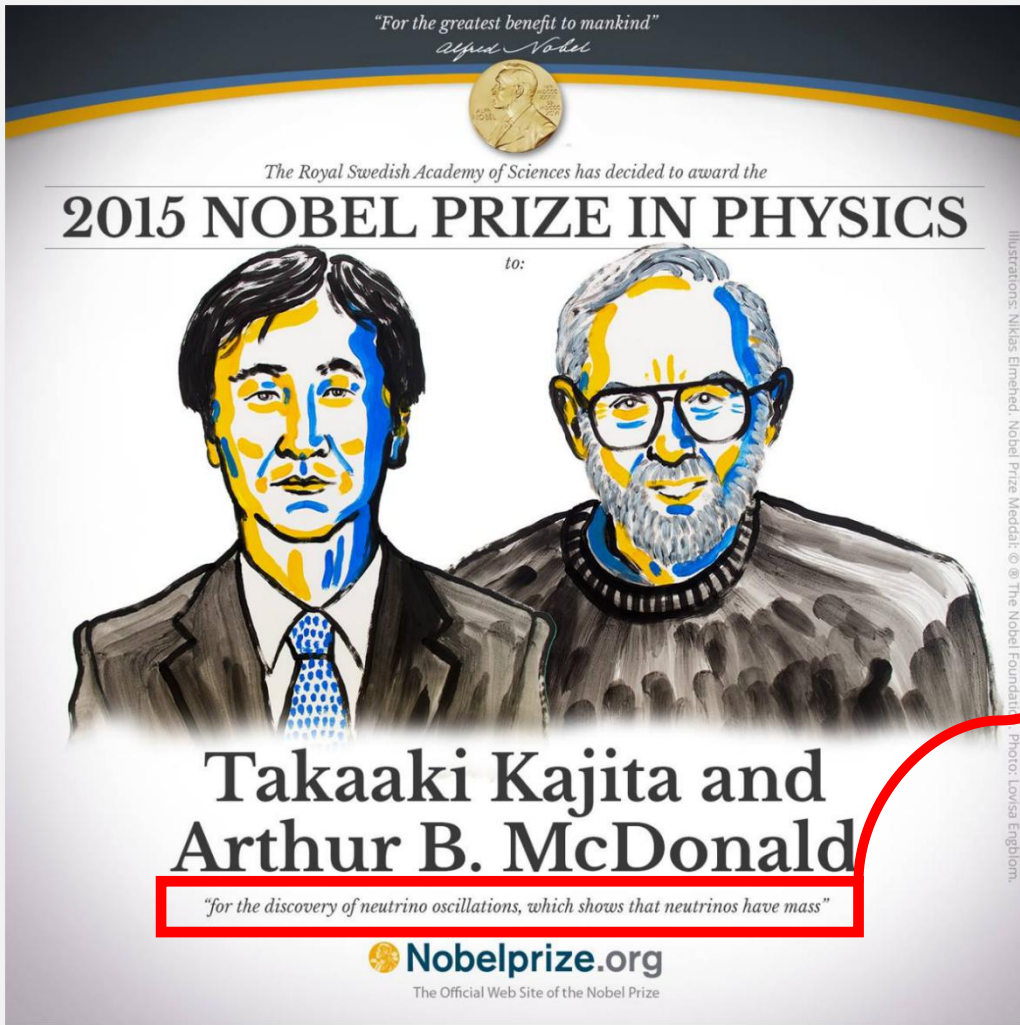


上海交通大学
SHANGHAI JIAO TONG UNIVERSITY

SPCS 2024 @ TDLI

Nov 13, 2024

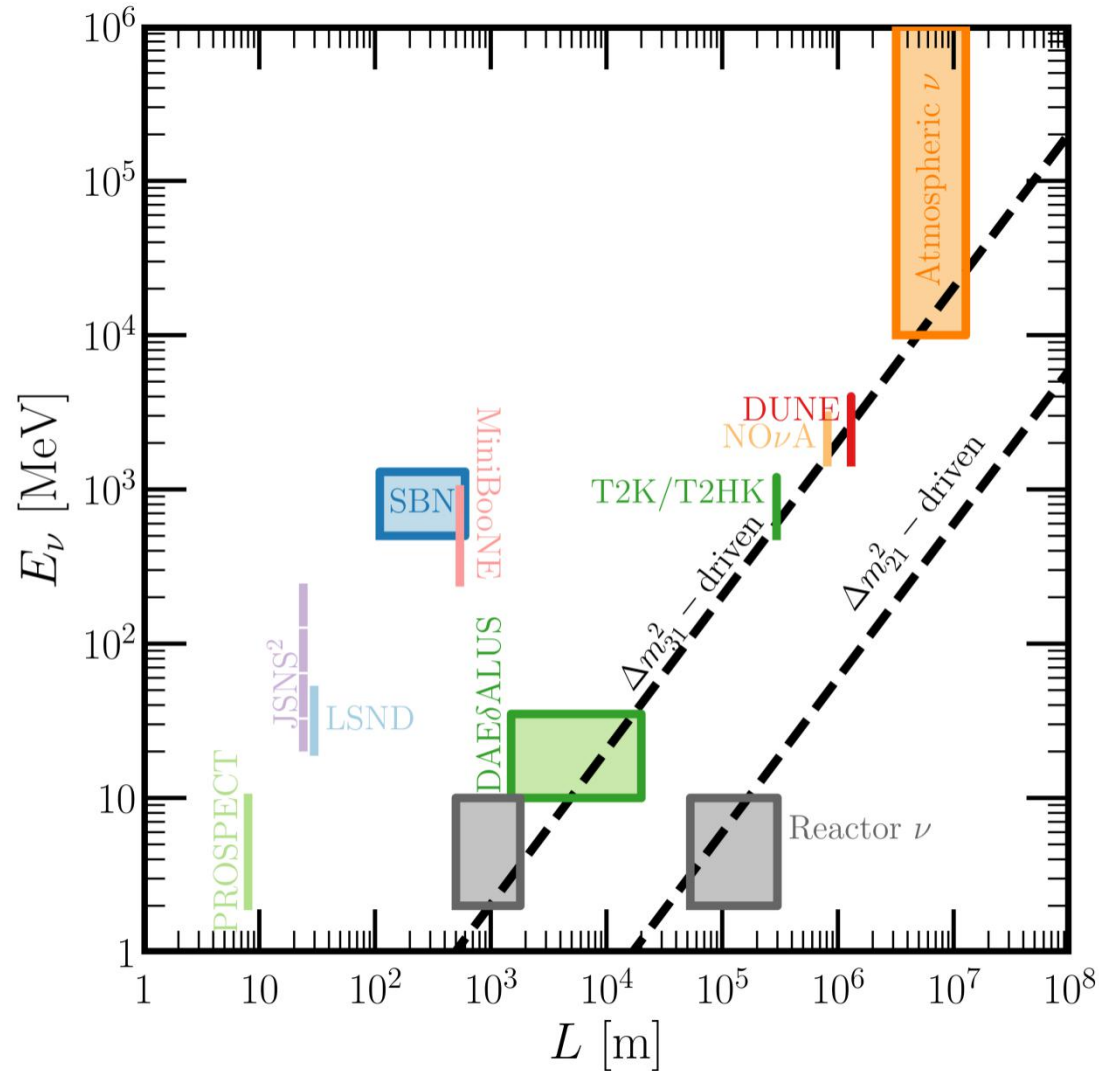
• Evidence of Neutrino Mass



“for the discovery of neutrino oscillations, which shows that neutrinos have mass”

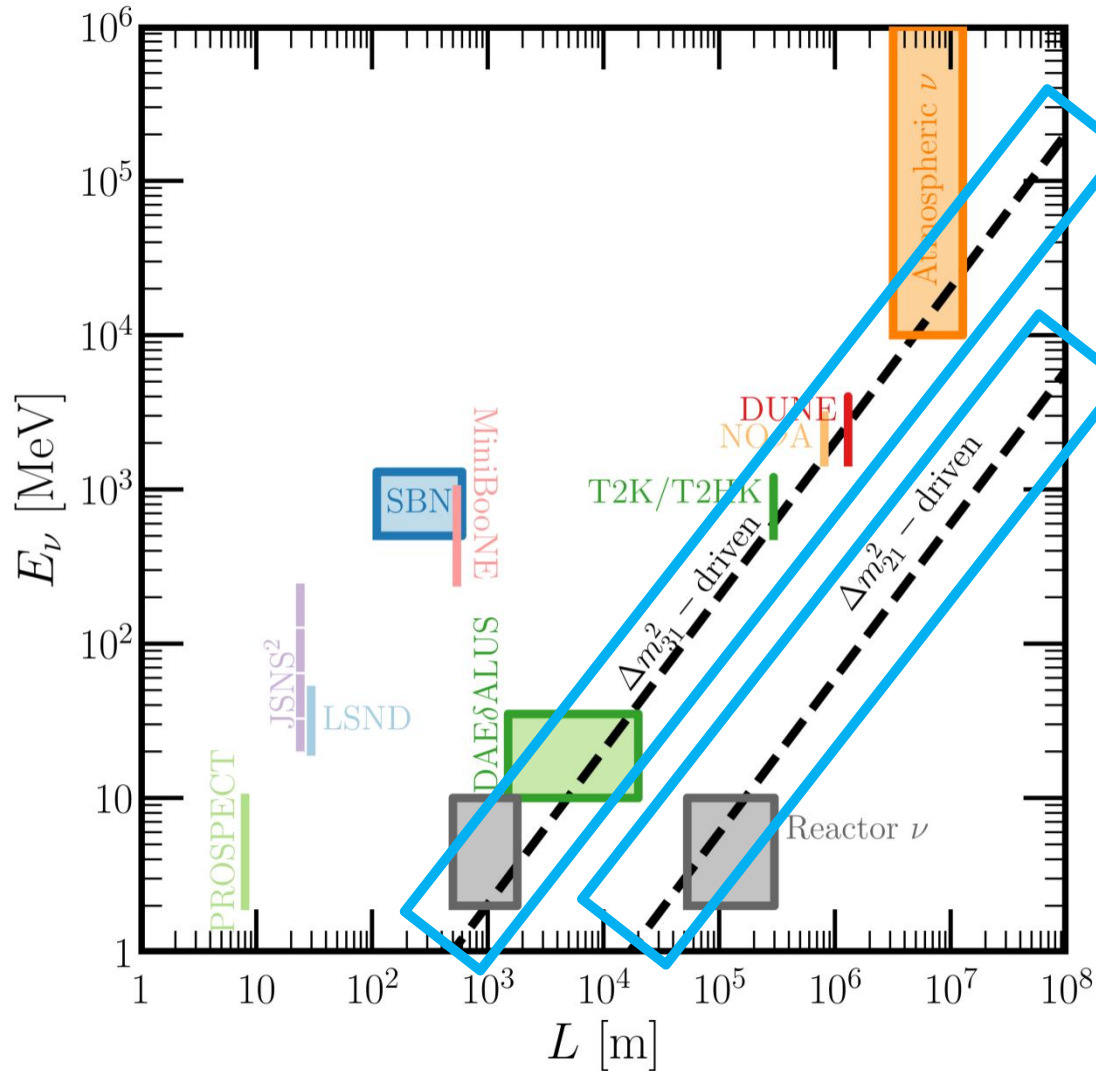
• Evidence of Neutrino Mass

*[see talks by Concha Gonzalez-Garcoa,
Shun Zhou, Jun-Jie Jiang]*



*R. Harnik, K. Kelly, P. Machado
arXiv: 1911.05088*

• Evidence of Neutrino Mass

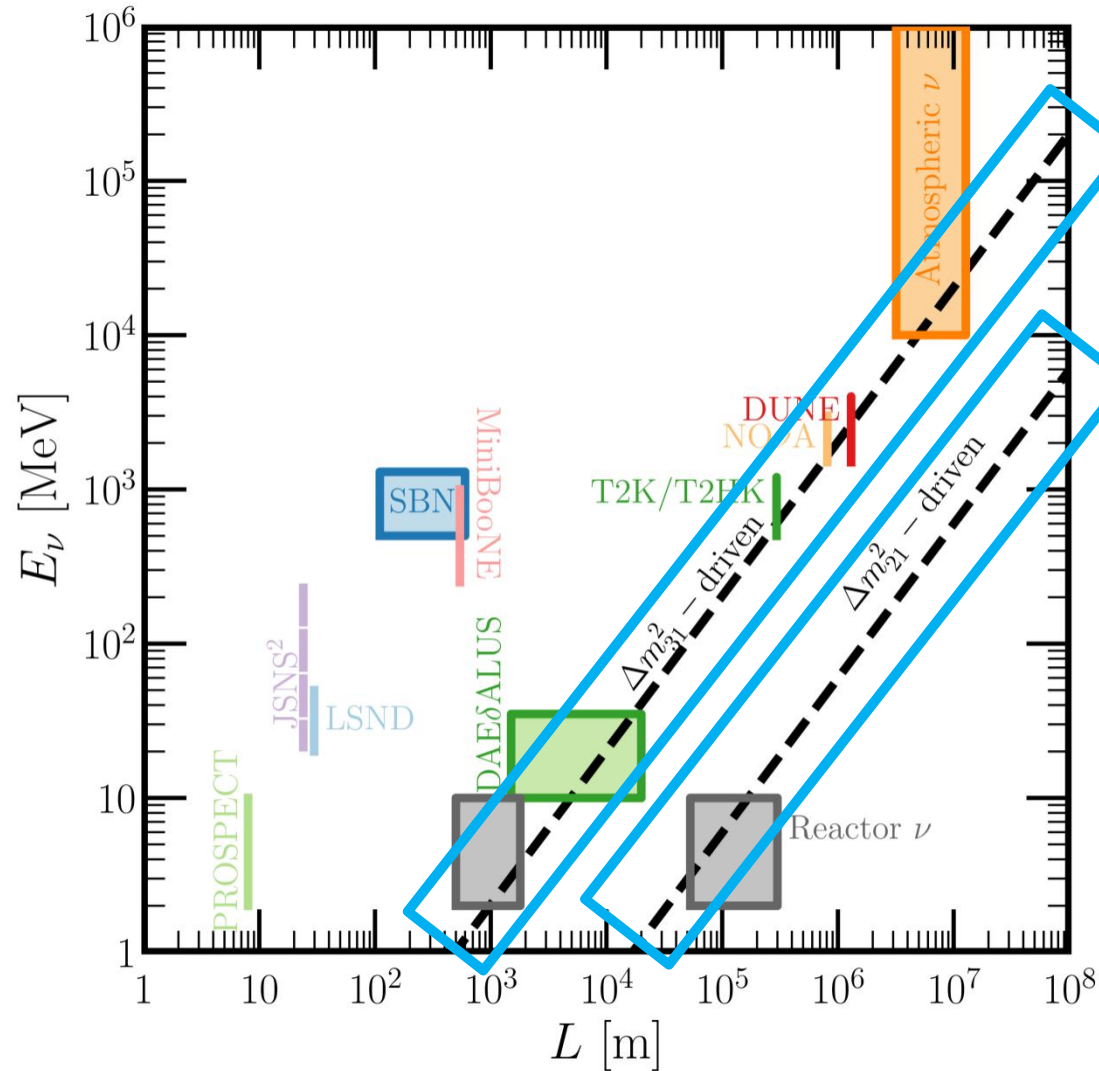


$$\text{oscillation phase} : \propto \frac{\Delta m_{ij}^2 L}{E_\nu}$$

Neutrino masses drive the oscillation behavior !

*R. Harnik, K. Kelly, P. Machado
arXiv: 1911.05088*

• Evidence of Neutrino Mass



$$\text{oscillation phase} : \propto \frac{\Delta m_{ij}^2 L}{E_\nu}$$

Neutrino masses drive the oscillation behavior !



What's **the origin** of neutrino mass?

*R. Harnik, K. Kelly, P. Machado
arXiv: 1911.05088*

• Neutrino Mass Origins

Neutrino mass origins



vacuum neutrino mass

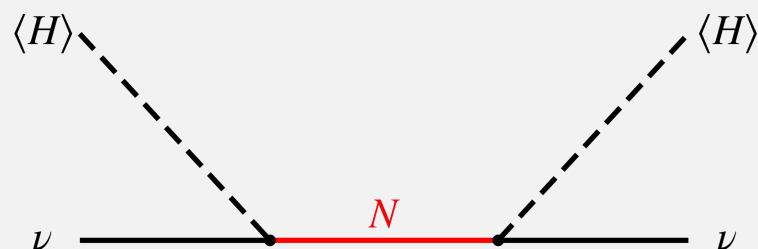
dark neutrino mass

• Neutrino Mass Origin I: vacuum mass

[see talk by Shun Zhou]

Vacuum Neutrino Mass

Type-I seesaw

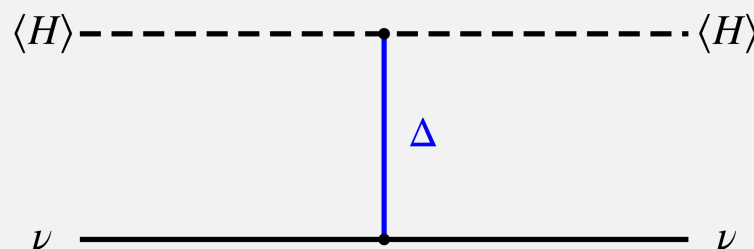


$$M_\nu = -\frac{1}{2} Y_\nu \frac{v^2}{M_R} Y_\nu^T$$

*P. Minkowski
T. Yanagida
M. Gell-Mann*

...

Type-II seesaw

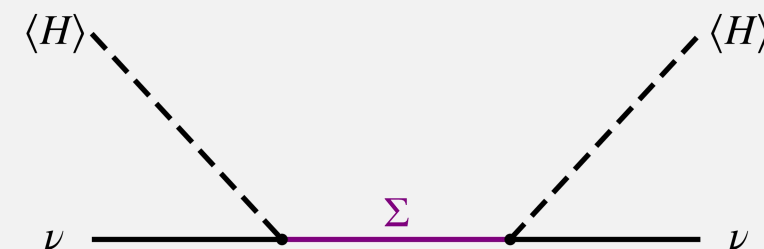


$$M_\nu = \lambda_\Delta Y_\Delta \frac{v^2}{M_\Delta}$$

*M. Magg & C. Wetterich
G. Lazarides, Q. Shafi, & C. Wetterich
R. Mohapatra & G. Senjanovic*

...

Type-III seesaw



$$M_\nu = -\frac{1}{2} Y_\Sigma \frac{v^2}{M_\Sigma} Y_\Sigma^T$$

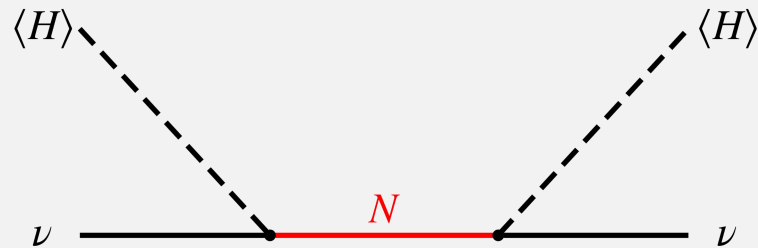
*R. Foot, H. Lew, X.-G. He, & G.C. Joshi
E. Ma*

...

• Neutrino Mass Origin I: vacuum mass

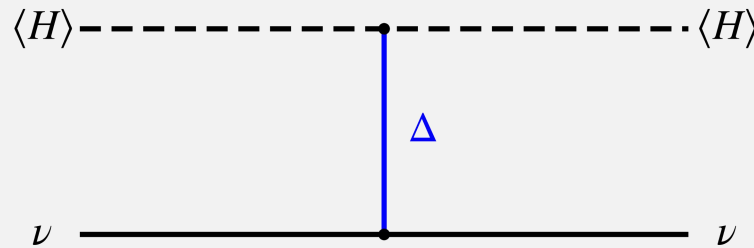
Vacuum Neutrino Mass

Type-I seesaw



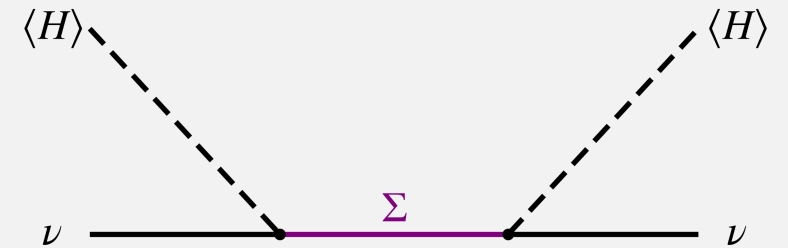
$$M_\nu = -\frac{1}{2} Y_\nu \frac{v^2}{M_R} Y_\nu^T$$

Type-II seesaw



$$M_\nu = \lambda_\Delta Y_\Delta \frac{v^2}{M_\Delta}$$

Type-III seesaw



$$M_\nu = -\frac{1}{2} Y_\Sigma \frac{v^2}{M_\Sigma} Y_\Sigma^T$$

$$m_{\text{vac}}^2 = A$$

• Neutrino Mass Origin II: dark mass

$$H \sim \sqrt{p^2 + |m|^2} \approx p + \boxed{\frac{|m|^2}{2E}}$$

neutrino
oscillation

• Neutrino Mass Origin II: dark mass

$$H \sim \sqrt{p^2 + |m|^2} \approx p + \frac{|m|^2}{2E}$$

What if $m = 0$, but neutrino matter potential

$$H \approx p + V, \quad \text{with } V = \frac{\dots}{2E}$$

• Neutrino Mass Origin II: dark mass

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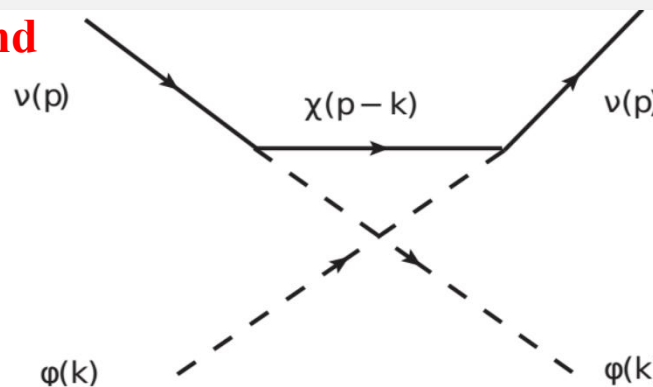
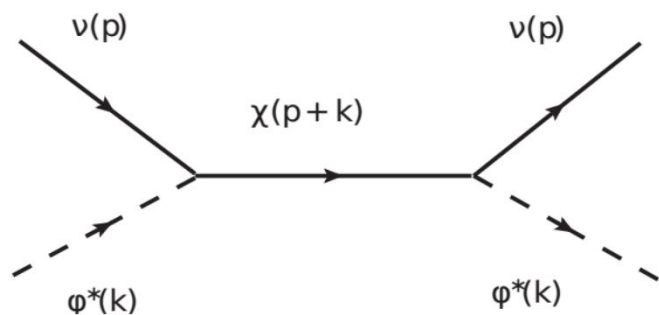
What if $m = 0$, but neutrino matter potential

$$H \approx p + V, \quad \text{with } V = \frac{\boxed{\dots}}{2E} \begin{array}{l} \text{effective mass} \\ \text{or} \\ \text{“dark” mass} \end{array}$$

• Neutrino Mass Origin II: dark mass

Dark Neutrino Mass

Forward scattering with DM background



Introduce the effective or refractive mass squared as

$$V = m_{\text{ref}}^2 / 2E$$

$$m_{\text{ref}}^2 = 2EV$$

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$$m_{\text{ref}}^2 = m_{\text{as}}^2 \frac{y(y - \varepsilon)}{y^2 - 1}$$

$$m_{\text{as}}^2 = \sum_k g_{\alpha k} g_{\beta k}^* \frac{\rho_\phi}{m_\phi^2}$$

A. Y. Smirnov, talks@MAYORANA Workshop

[S.-F. Ge & H. Murayama, arXiv:1904.02518;

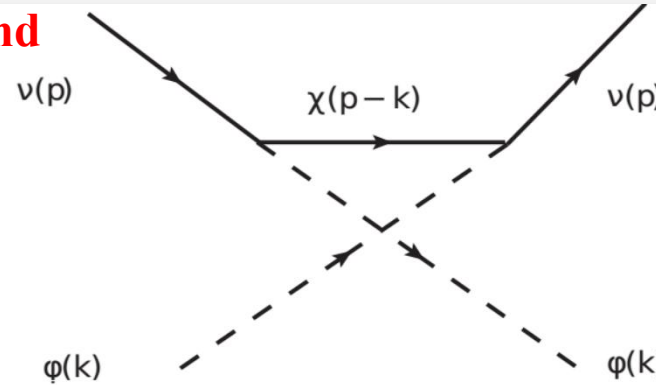
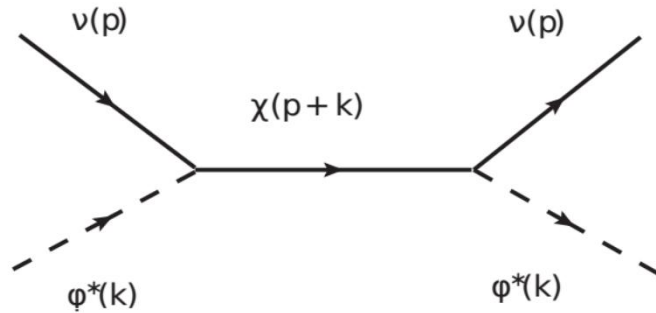
K. Y. Choi, E. J. Chun & J. Kim, arXiv:1909.10478, 2012.09474;

M. Sen and A. Y. Smirnov, arXiv:2306.15718]

• Neutrino Mass Origin II: dark mass

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A. Y. Smirnov, talks@MAYORANA Workshop

$$m_{\text{dark}}^2(x) \propto \rho_\phi$$

• Neutrino Mass Origins Comparison

Vacuum Neutrino Mass: $m_{\text{vac}}^2 = A$

vs.

Dark Neutrino Mass: $m_{\text{dark}}^2(x) \propto \rho_\phi$

• Neutrino Mass Origins Comparison

Vacuum Neutrino Mass: $m_{\text{vac}}^2 = A$

vs.

Dark Neutrino Mass: $m_{\text{dark}}^2(x) \propto \rho_\phi$

Can we distinguish these two origins ?

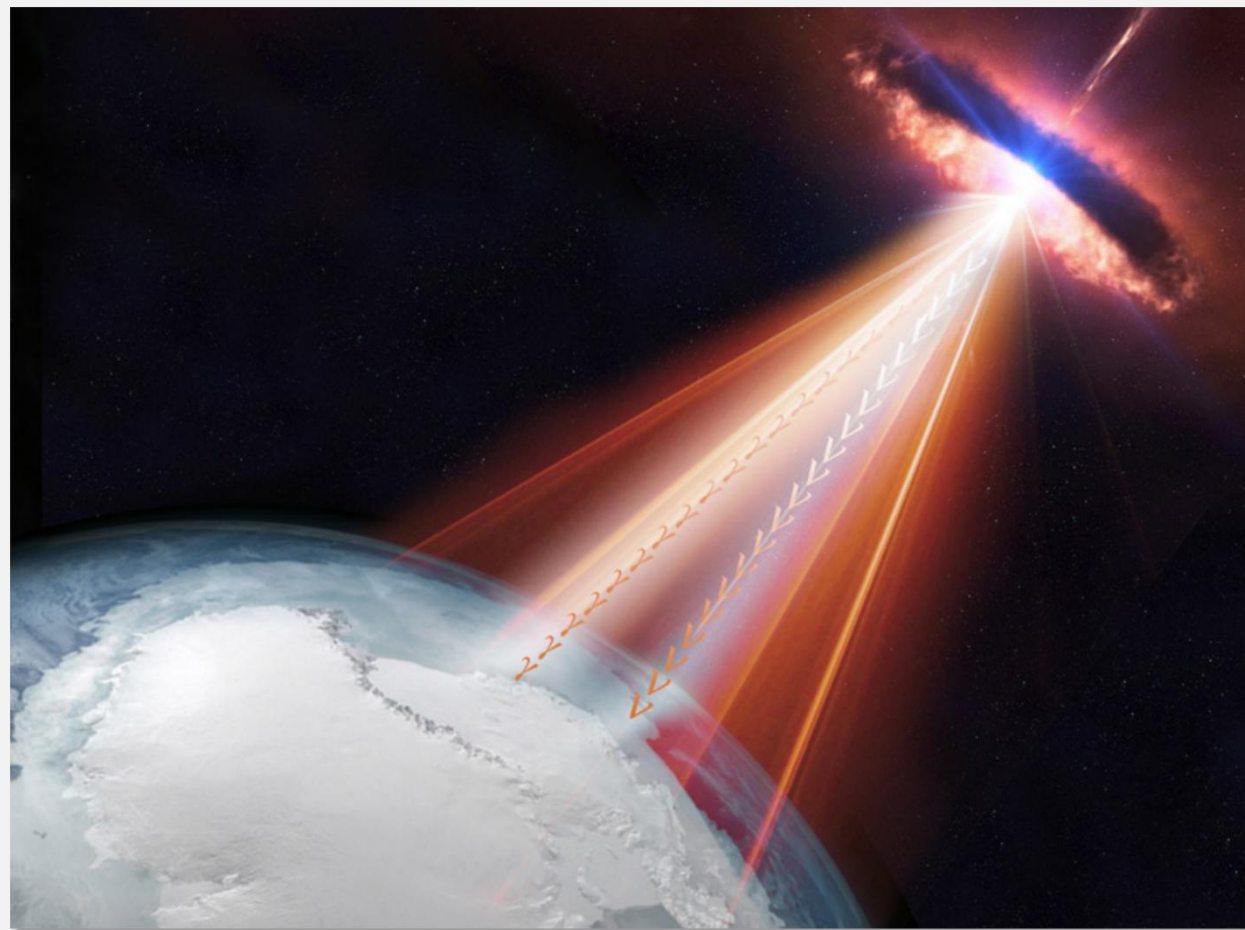
• Large Scales

Yes! Look into larger scales!

$$m_{\text{vac}}^2 = A$$

vs.

$$m_{\text{dark}}^2(x) \propto \rho_\phi$$



Credit: IceCube

• Supernova Neutrino Time Delay

Galactic supernovae are ideal neutrino sources!

POSSIBILITY OF DETERMINING THE UPPER LIMIT OF THE NEUTRINO MASS FROM THE TIME OF FLIGHT

G. I. Zatsepin

P. N. Lebedev Physics Institute, USSR Academy of Sciences

Submitted 20 July 1968

ZhETF Pis. Red. 8, No. 6, 333-334 (20 September 1968)

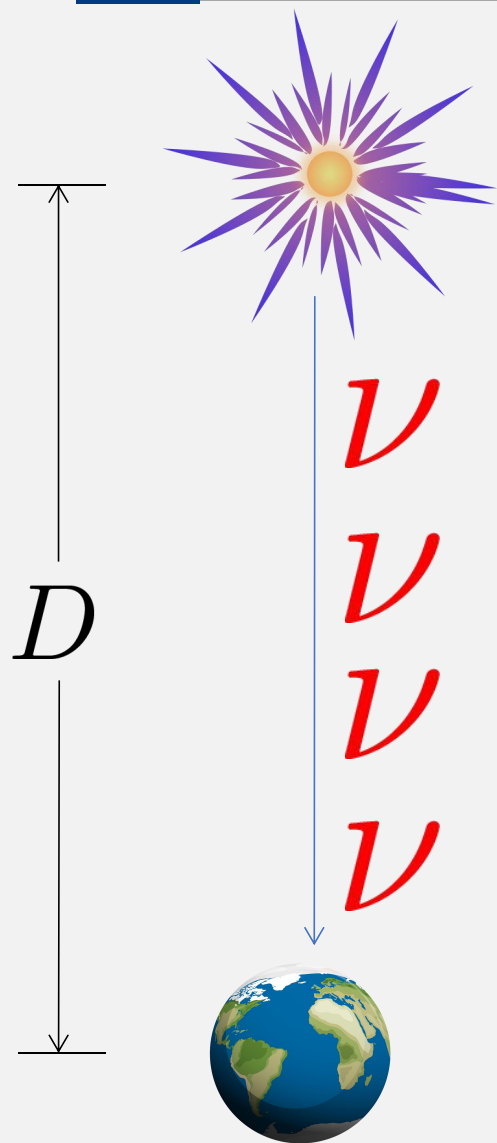
56 years ago!

[T. J. Loredo and D. Q. Lamb, *astro-ph/0107260*; E. Nardi and J. I. Zuluaga, *astro-ph/0306384*, *hep-ph/0412104*; G. Pagliaroli, F. Rossi-Torres and F. Vissani 1002.3349; J. S. Lu, J. Cao, Y. F. Li and S. Zhou, 1412.7418; R. S. L. Hansen, M. Lindner and O. Scholer, 1904.11461; F. Pompa, F. Capozzi, O. Mena and M. Sorel, 2203.00024; F. Pompa and O. Mena, 2310.05474; G. Parker and M. Wurm, 2311.10682 ...]

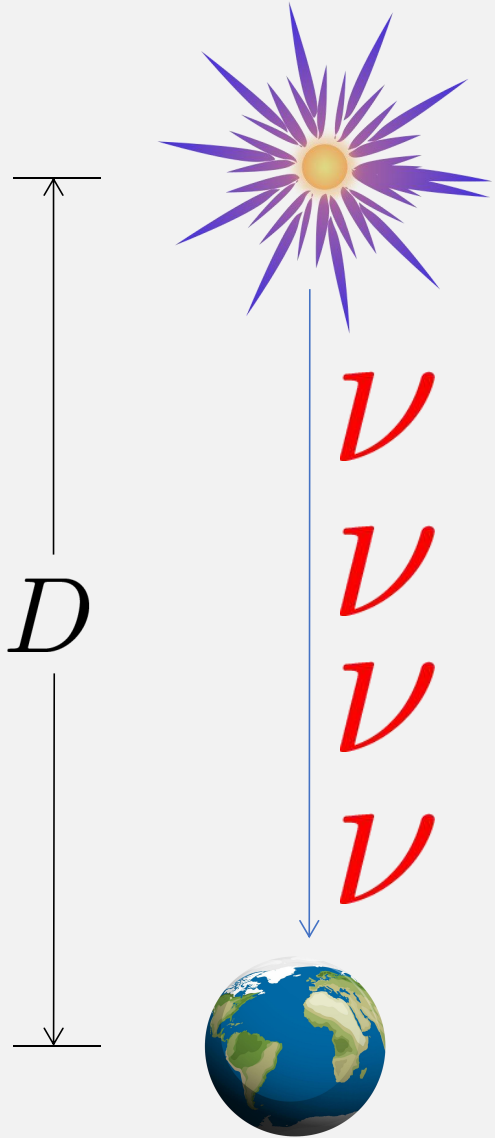
Credit: IceCube

• Supernova Neutrino Time Delay

[see talk by Yu-Feng Li]



• Supernova Neutrino Time Delay (vacuum neutrino mass)

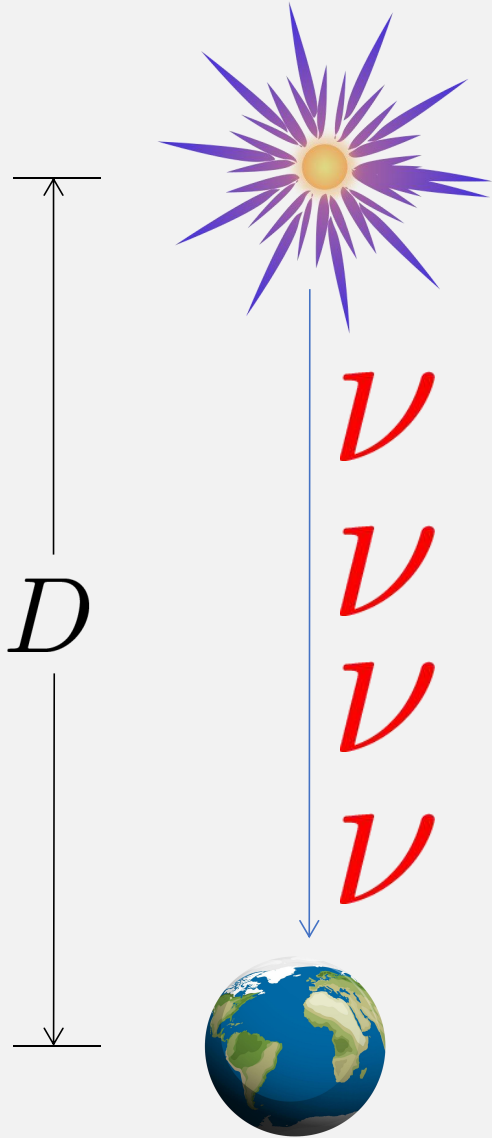


$$\Downarrow E_\nu = \sqrt{p_\nu^2 + m^2}, \quad v = \frac{dE_\nu}{dp_\nu}$$

group velocity:

$$v = \frac{p}{E} = \sqrt{1 - \frac{m_{\text{vac}}^2}{E^2}} \approx 1 - \frac{m_{\text{vac}}^2}{2E^2}$$

• Supernova Neutrino Time Delay (vacuum neutrino mass)



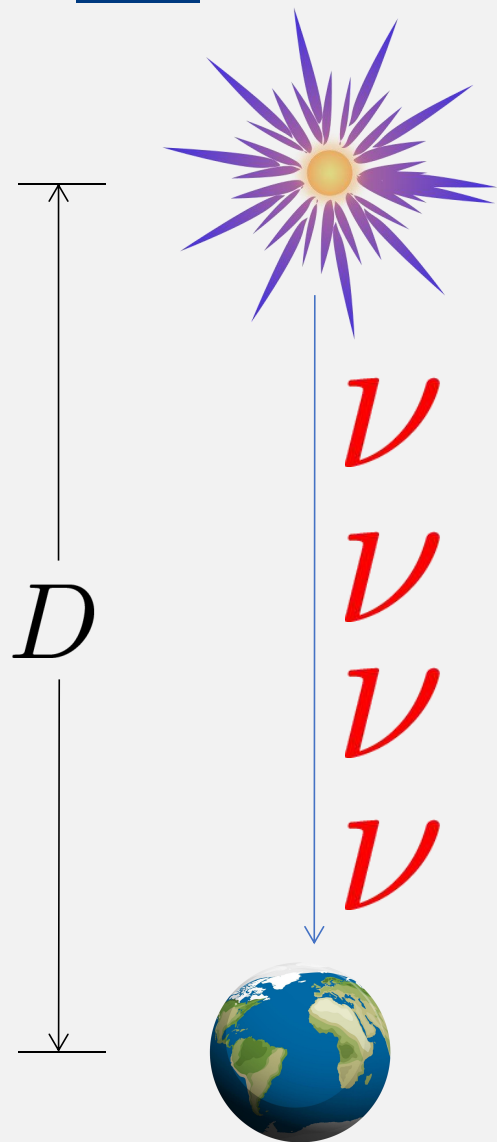
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smaller than the speed of light
&
space-time independent

• Supernova Neutrino Time Delay (vacuum neutrino mass)



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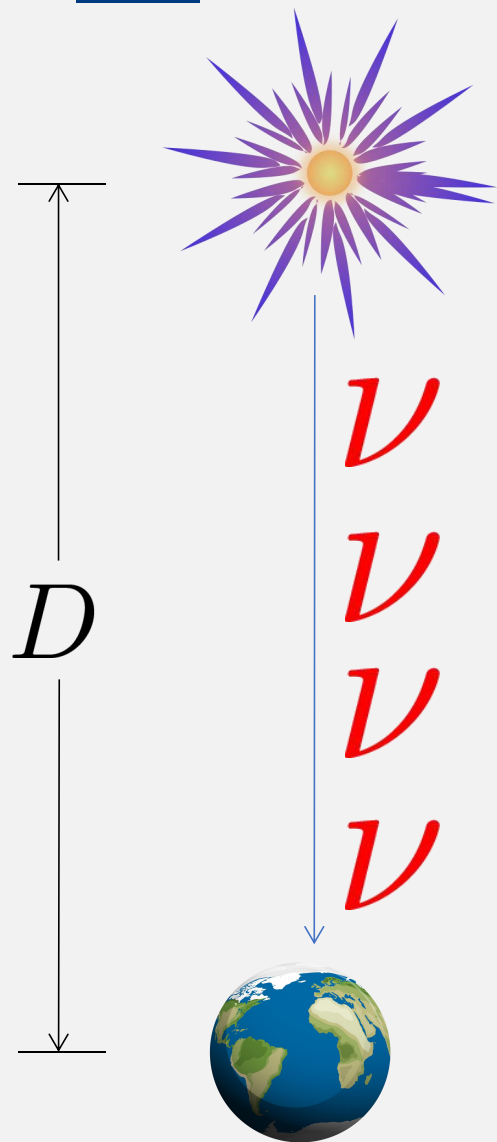
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time delay:

$$\Delta t_{\text{vac}} \equiv \frac{D}{v} - \frac{D}{c(\equiv 1)} = \frac{m_{\text{vac}}^2}{2E^2} D \approx 5.14 \text{ ms} \left(\frac{m_{\text{vac}}}{\text{eV}} \right)^2 \left(\frac{10 \text{ MeV}}{E} \right)^2 \frac{D}{10 \text{ kpc}}$$

• Supernova Neutrino Time Delay (vacuum neutrino mass)



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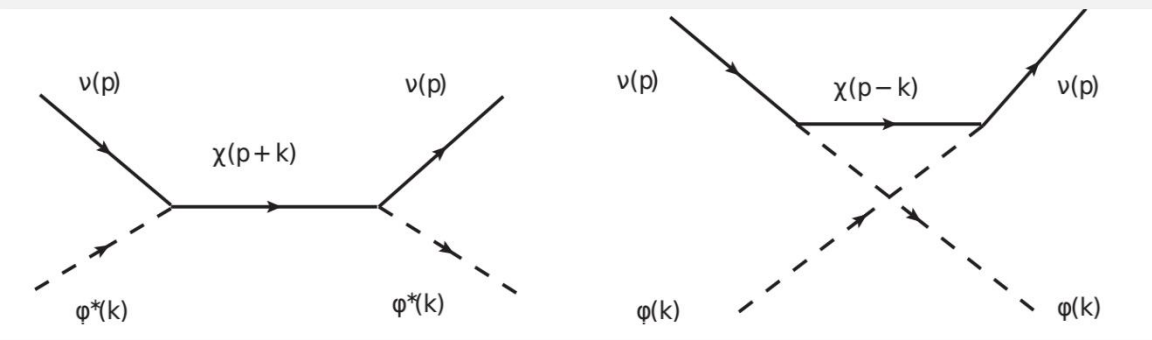
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• Supernova Neutrino Time Delay (dark neutrino mass)

Recall



Introduce the effective or refractive mass squared as

$$V = m_{\text{ref}}^2 / 2E$$

$$m_{\text{ref}}^2 = 2EV$$



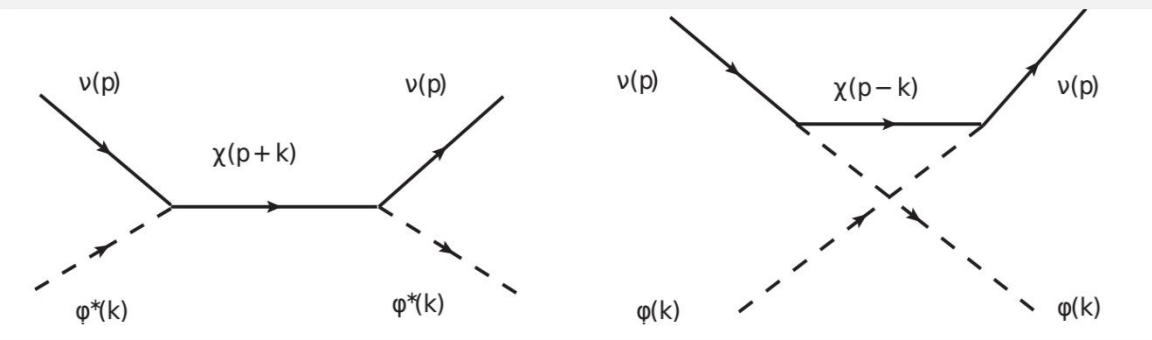
$$E_\nu = p_\nu + V, \quad v = \frac{dE_\nu}{dp_\nu}$$

group velocity:

$$1 - v(\mathbf{x}) = \frac{m_{\text{dark}}^2(\mathbf{x}, p_\nu)}{2p_\nu^2} - \frac{1}{2p_\nu} \frac{dm_{\text{dark}}^2(\mathbf{x}, p_\nu)}{dp_\nu}$$

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Recall



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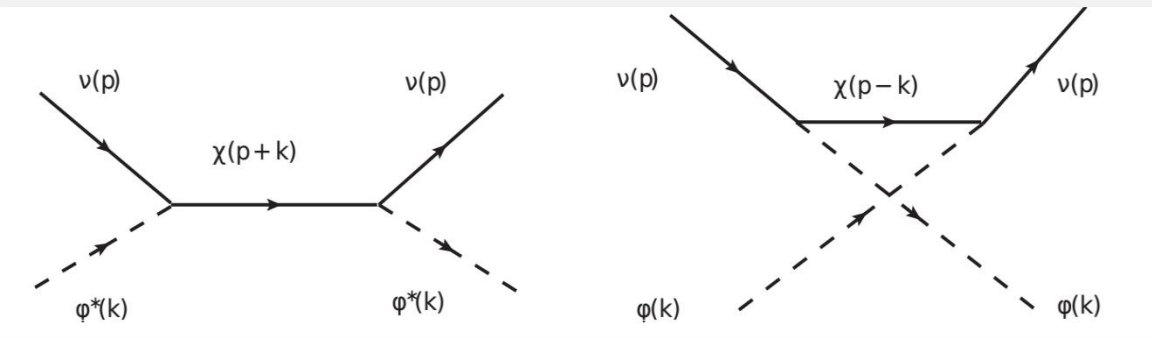
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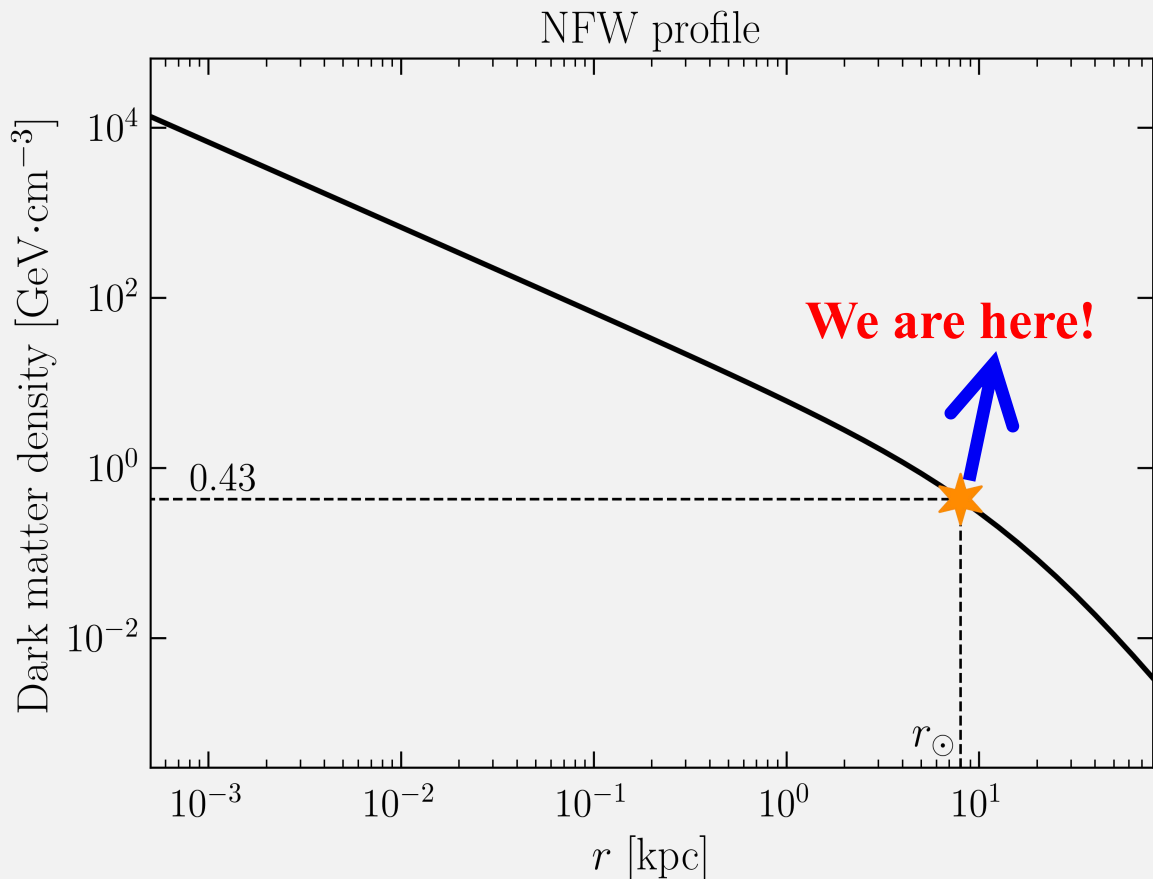
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$$1 - v(\mathbf{x}) = \frac{m_{\text{dark}}^2(\mathbf{x}_\odot)}{2E^2} \frac{\rho_\phi(\mathbf{x})}{\rho_\phi(\mathbf{x}_\odot)}$$

space-time dependent!

[$\mathbf{x}_\odot$: solar system position]

• Supernova Neutrino Time Delay (dark neutrino mass)



Navarro-Frenk-White profile

$$E_{\nu} = p_{\nu} + V, \quad v = \frac{dE_{\nu}}{dp_{\nu}}$$

group velocity:

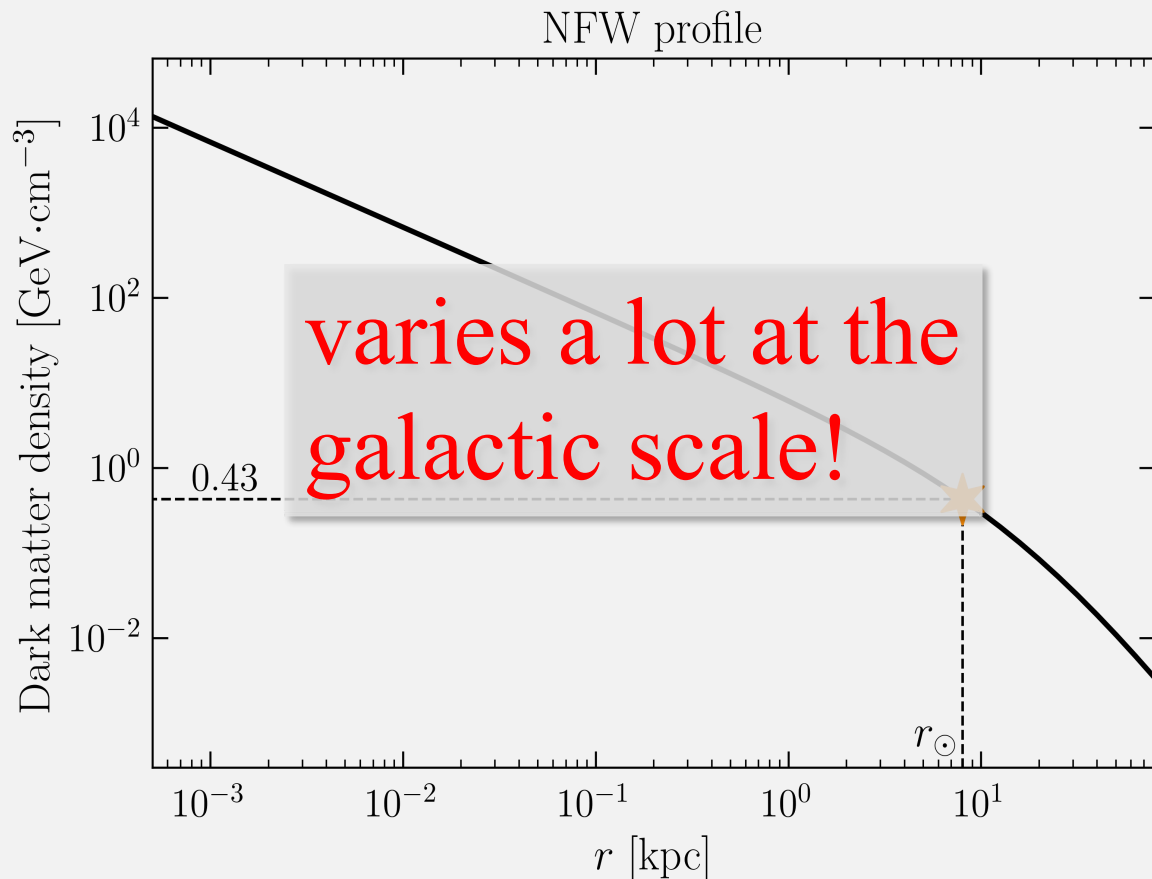
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• Supernova Neutrino Time Delay (dark neutrino mass)

...

$$1 - v(\mathbf{x}) = \frac{m_{\text{dark}}^2(\mathbf{x}_{\odot})}{2E^2} \frac{\rho_{\phi}(\mathbf{x})}{\rho_{\phi}(\mathbf{x}_{\odot})}$$

$$\Delta t_{\text{dark}} \equiv \int_{\mathbf{x}_{\star}}^{\mathbf{x}_{\odot}} \left(\frac{1}{v(\mathbf{x})} - 1 \right) |d\mathbf{x}| \approx \int_{\mathbf{x}_{\star}}^{\mathbf{x}_{\odot}} (1 - v(\mathbf{x})) |d\mathbf{x}|$$

just an integration over neutrino trajectory

• Supernova Neutrino Time Delay (dark neutrino mass)

...

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vacuum neutrino mass

differed by this factor!

• Supernova Neutrino Time Delay (dark neutrino mass)

...

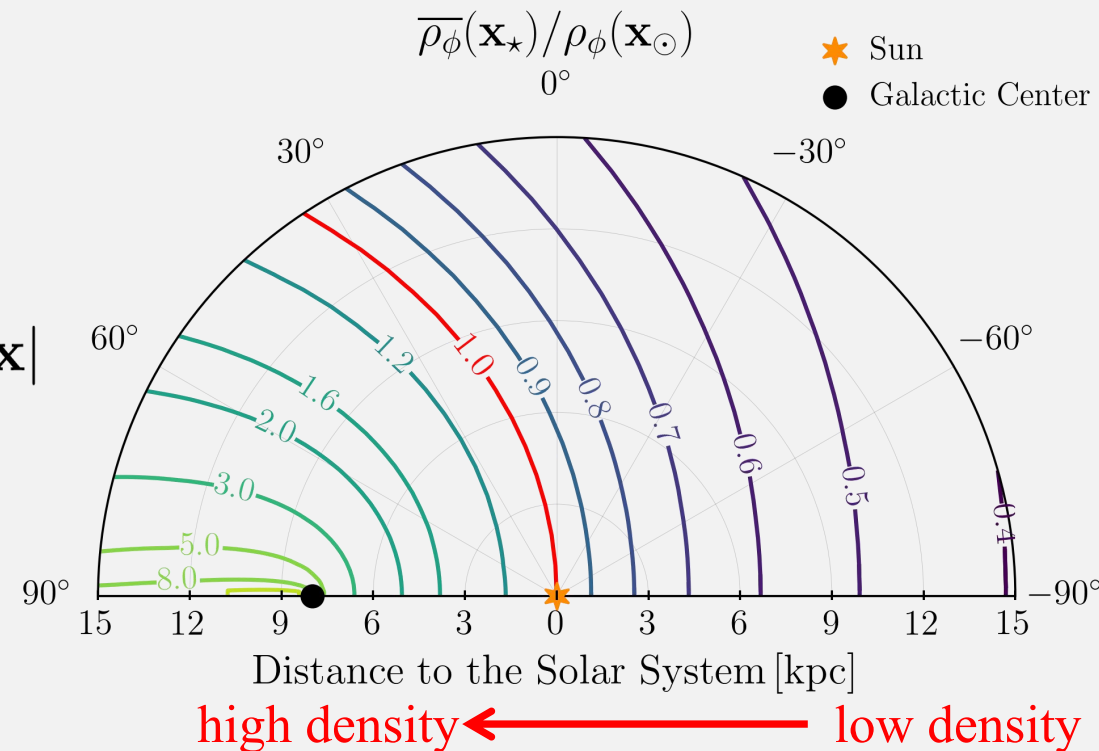
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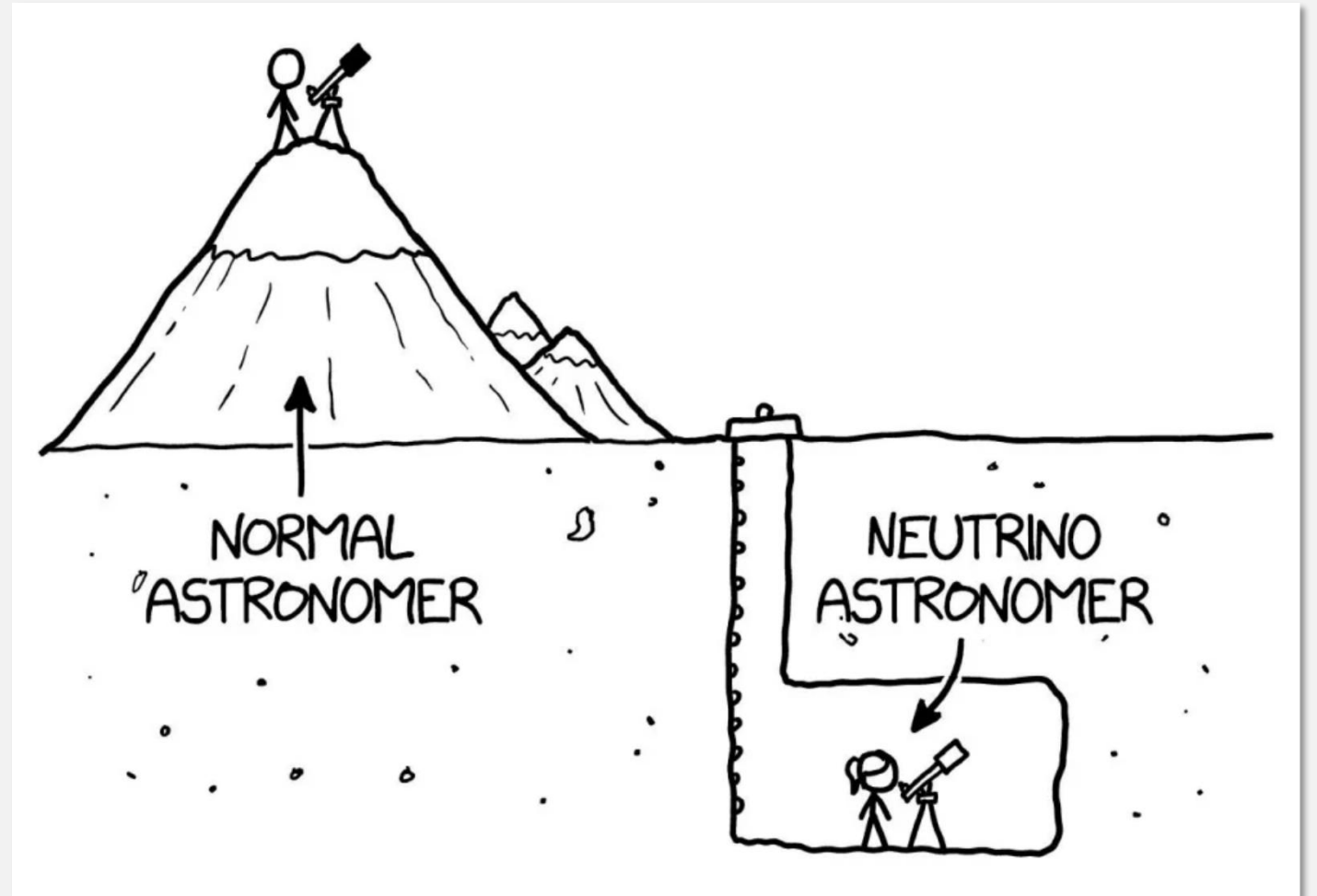
vacuum neutrino mass

differed by this factor!



Ge, **CFK**, Smirnov
arXiv: 2404.17352

Experimental Sensitivity



credit: PHYSICSGG

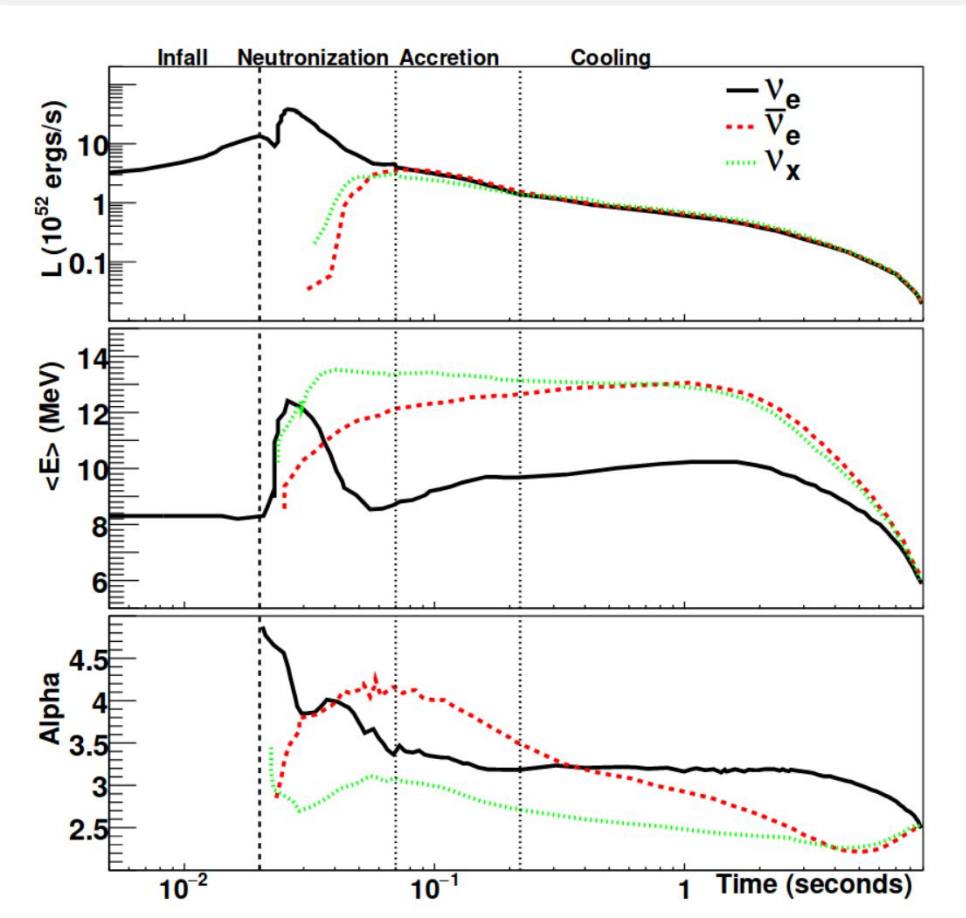
• Supernova Neutrino Production

❖ ν_e SN burst production (Garching model):

$$\Phi_{\nu_\beta}^0(t_e, E_\nu) = \frac{L_{\nu_\beta}(t_e)}{\langle E_{\nu_\beta}(t_e) \rangle} \varphi_{\nu_\beta}(t_e, E_\nu)$$

$$\varphi_{\nu_\beta}(t_e, E_\nu) \equiv \xi_\beta(t_e) \left(\frac{E_\nu}{\langle E_{\nu_\beta}(t_e) \rangle} \right)^{\alpha_\beta(t_e)} e^{-\frac{(\alpha_\beta(t_e)+1)E_\nu}{\langle E_{\nu_\beta}(t_e) \rangle}}$$

• Supernova Neutrino Production



DUNE Collaboration
arXiv: 2008.06647

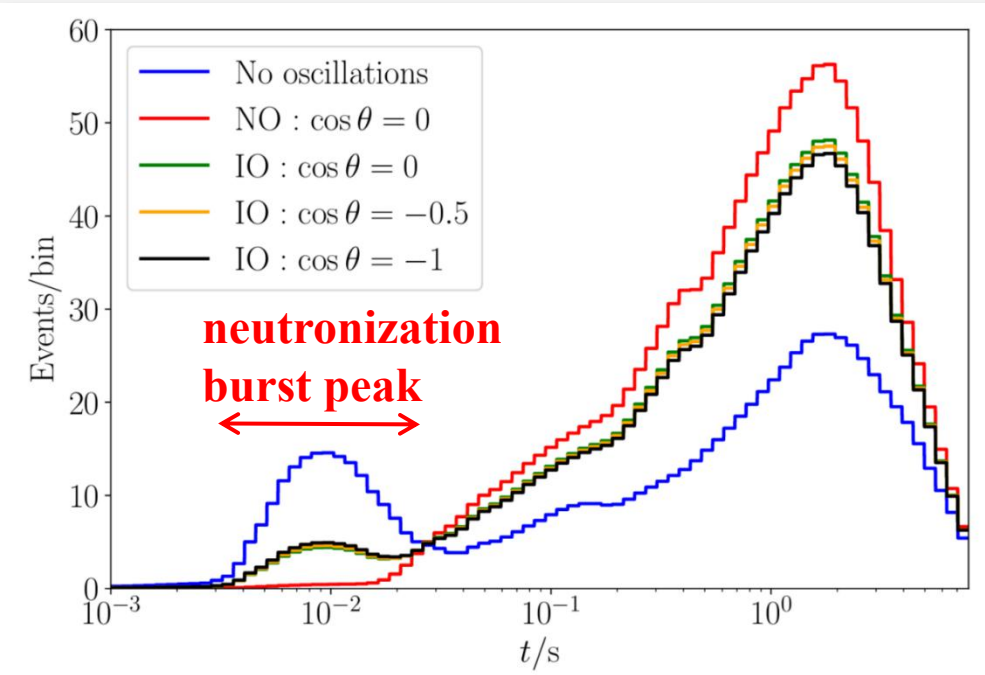
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• Supernova Neutrino Production

NO: normal ordering
IO: inverted ordering



F. Pompa, F. Capozzi, O. Mena, & M. Sorel
arXiv:2203.00024

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❖ MSW matter effect (from core to surface):

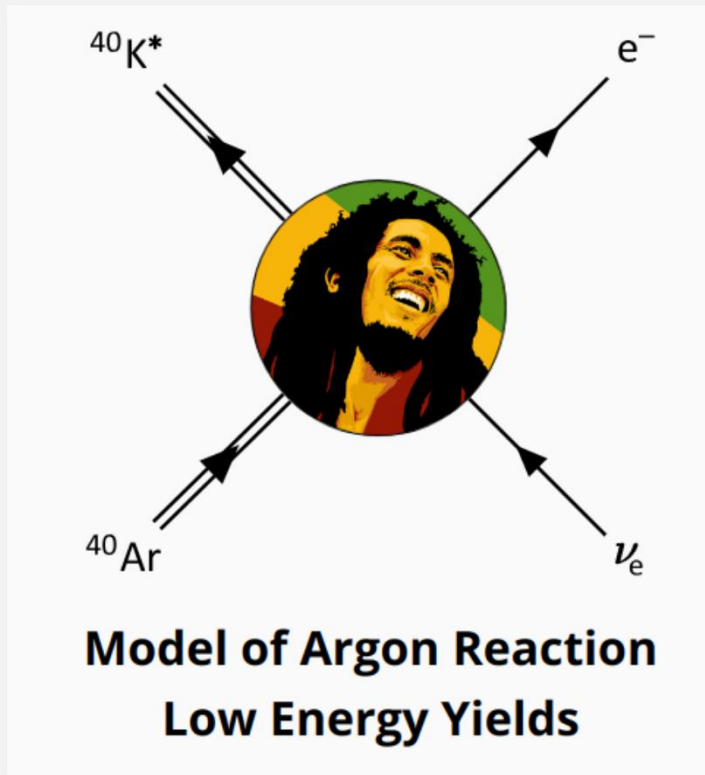
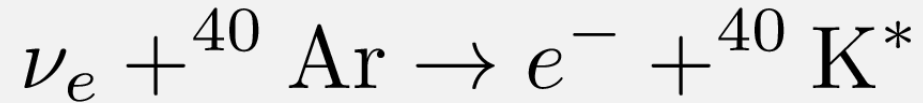
$$\Phi_{\nu_e} = p\Phi_{\nu_e}^0 + (1-p)\Phi_{\nu_x}^0$$

$$p = |U_{e3}|^2 \approx \sin^2 \theta_{13}, \text{ NO}$$

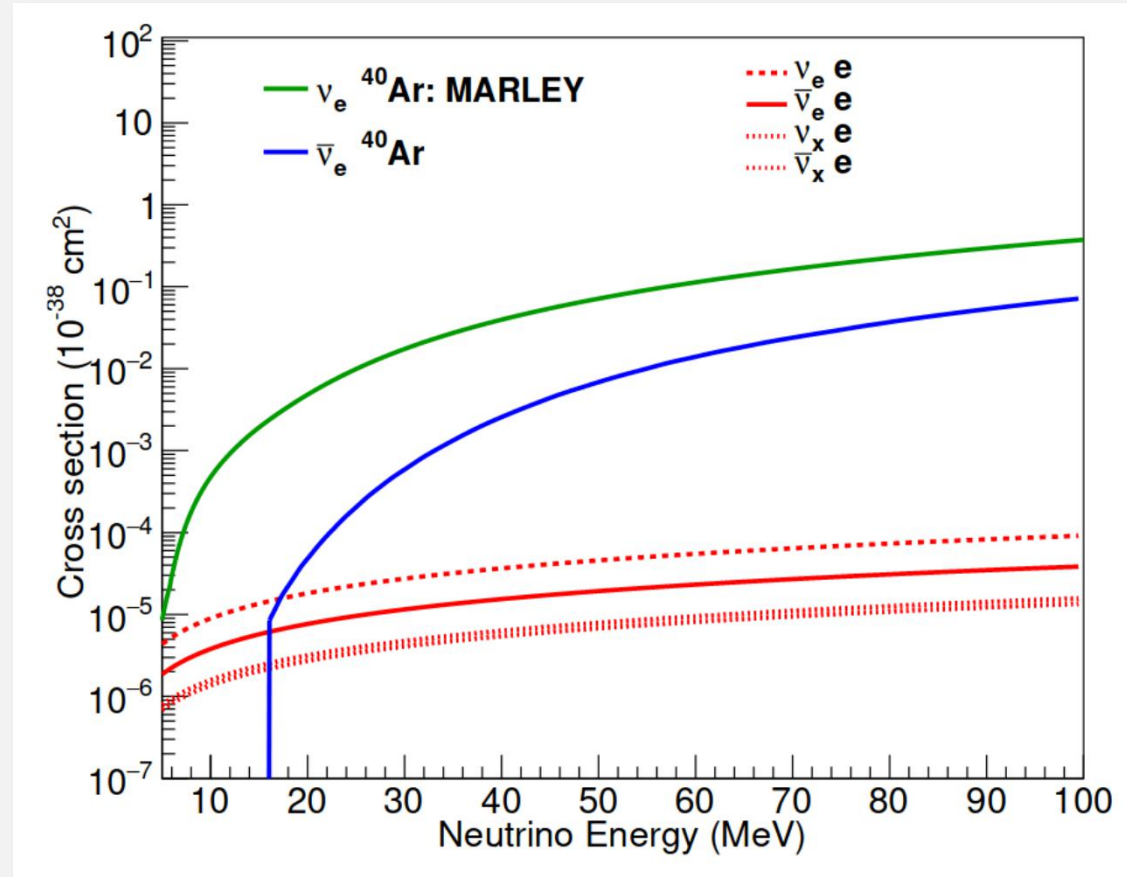
$$p \approx |U_{e2}|^2 \approx \sin^2 \theta_{12}, \text{ IO}$$

$$[\sin^2 \theta_{13} \approx 0.022, \sin^2 \theta_{12} \approx 0.3]$$

• Supernova Neutrino Detection @ DUNE



*S. Gardiner, 2010.02393
& 2101.11867*



*DUNE Collaboration
arXiv: 2008.06647*

• Time Distribution

Event rate:

$$R(t, m, E) = \frac{\Phi_{\nu_e}}{4\pi D^2} * A * \sigma_{\nu_e} * \epsilon$$

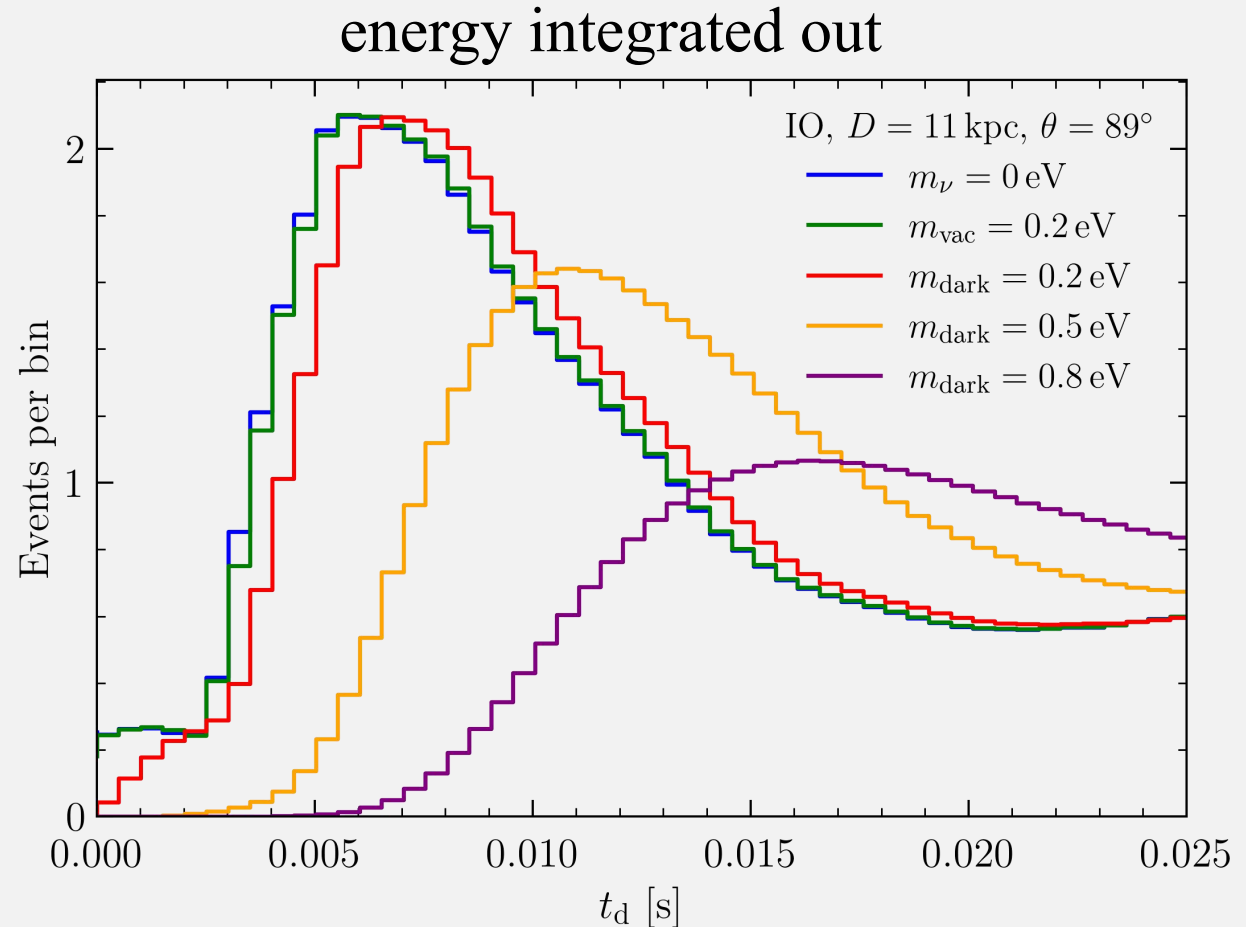
$[\Phi_{\nu_e} : \nu_e \text{ flux}]$

A : target nucleon number

σ_{ν_e} : cross section

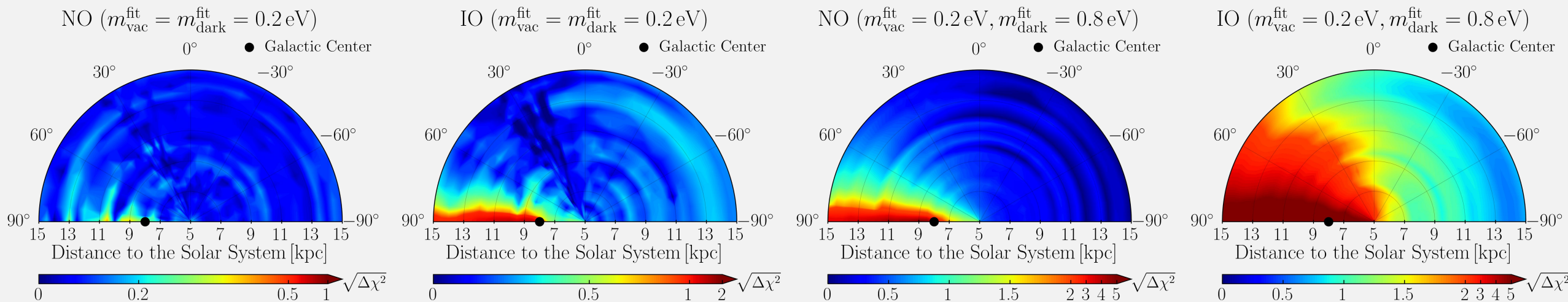
ϵ : efficiency]

❖ The time distribution becomes wider as the neutrino mass increases



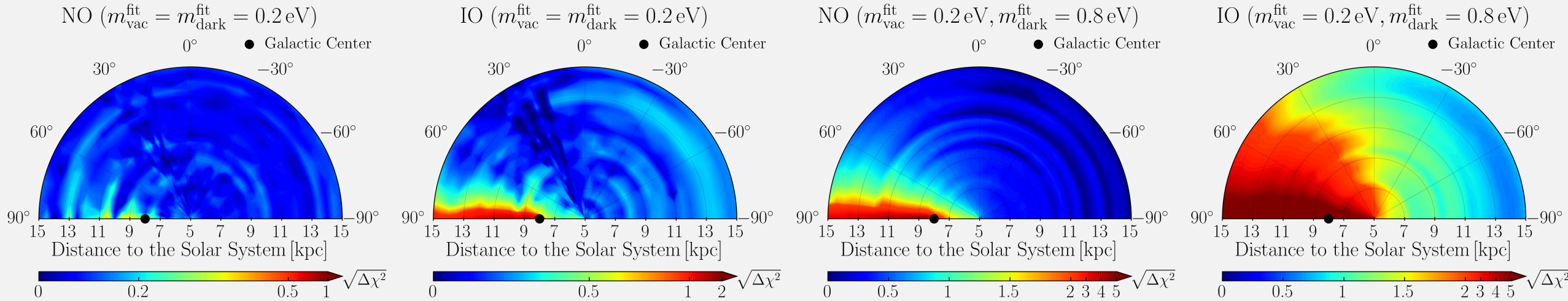
Ge, CFK, Smirnov
arXiv: 2404.17352

Sensitivities



Ge, CFK, Smirnov
arXiv: 2404.17352

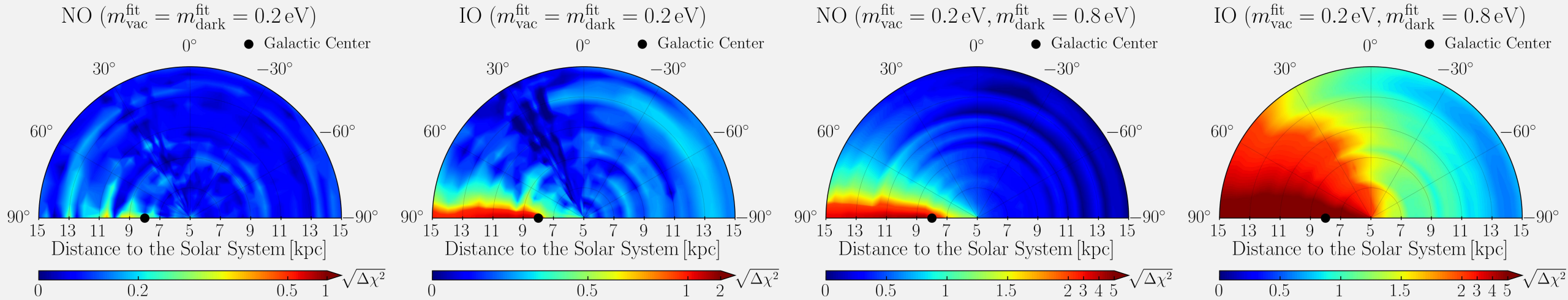
Sensitivities



❖ The sensitivity is enlarged by measuring supernova neutrinos around the galaxy center

Ge, CFK, Smirnov
arXiv: 2404.17352

Sensitivities



- ❖ The sensitivity is enlarged by measuring supernova neutrinos around the galaxy center
- ❖ Sensitivity for normal ordering (NO) is reduced by MSW matter effect

*Ge, CFK, Smirnov
arXiv: 2404.17352*

• Summary

- The dark neutrino mass is **space-time dependent** due to the DM distribution
- The supernova neutrino time delay can be **much enhanced** around galaxy center
- The neutrino mass origins (vacuum or dark mass) can be tested by measuring supernova neutrinos
- Better test can be done by measuring neutrinos from supernovae at different locations

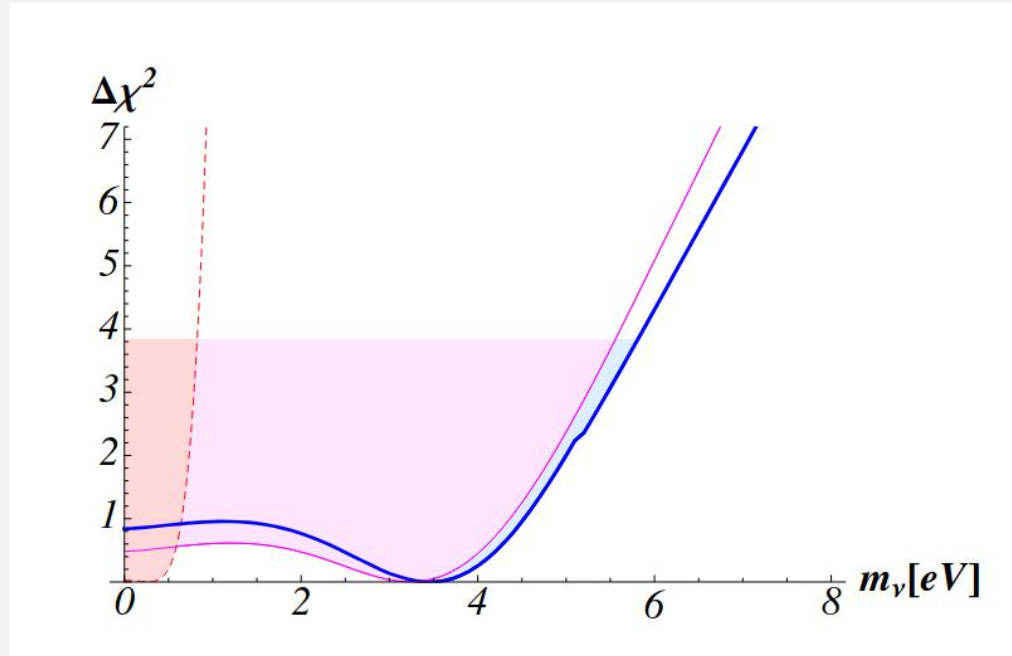
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Thank you for your attention!

• Backup

SN1987A



The minimum is located at ~ 3.5 eV, although not statistically significant

G. Pagliaroli, F. Rossi-Torres, & F. Vissani
arXiv:1002.3349

• Backup

parameter space

(i) $m_\phi \sim 10^{-10}$ eV, $g \sim 10^{-10}$, $m_\chi \sim 10^{-4}$ eV, and (ii)
 $m_\phi \sim 10^{-22}$ eV, $g \sim 10^{-21}$, $m_\chi \sim 10^{-10}$ eV.

M. Sen and A. Y. Smirnov, arXiv:2306.15718, 2407.02462

• Backup

matter potential

$$V_{\alpha\beta} = \sum_k g_{\alpha k} g_{\beta k}^* \left[\frac{\bar{n}_\phi (2Em_\phi - m_{\chi k}^2)}{(2Em_\phi - m_{\chi k}^2)^2 + (m_\chi \Gamma_{\chi k})^2} + \frac{n_\phi}{2Em_\phi + m_{\chi k}^2} \right],$$

M. Sen and A. Y. Smirnov, arXiv:2306.15718