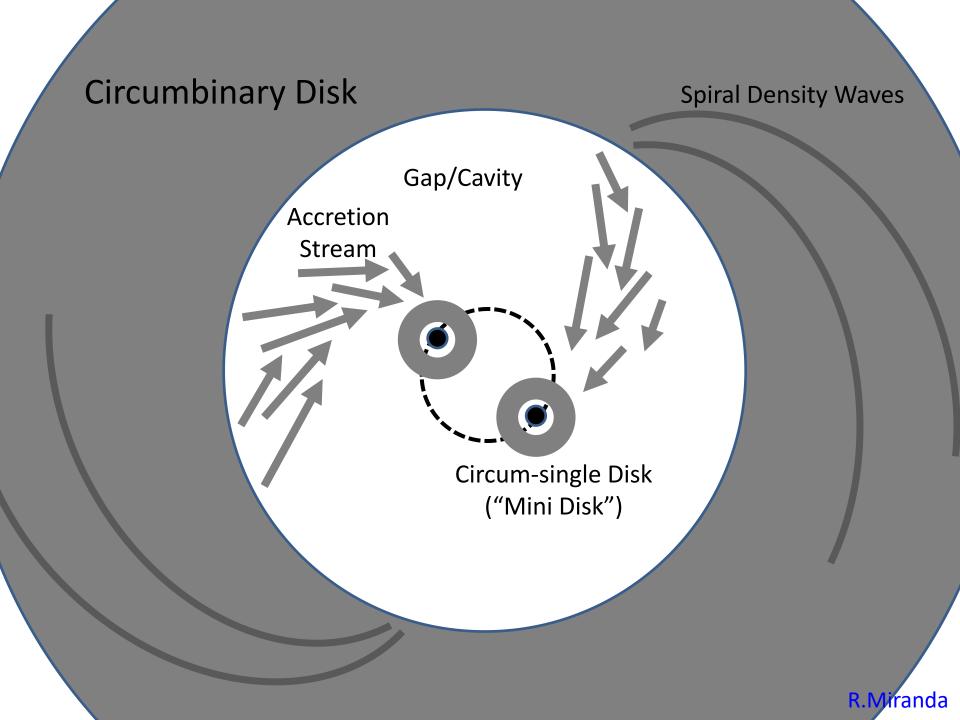
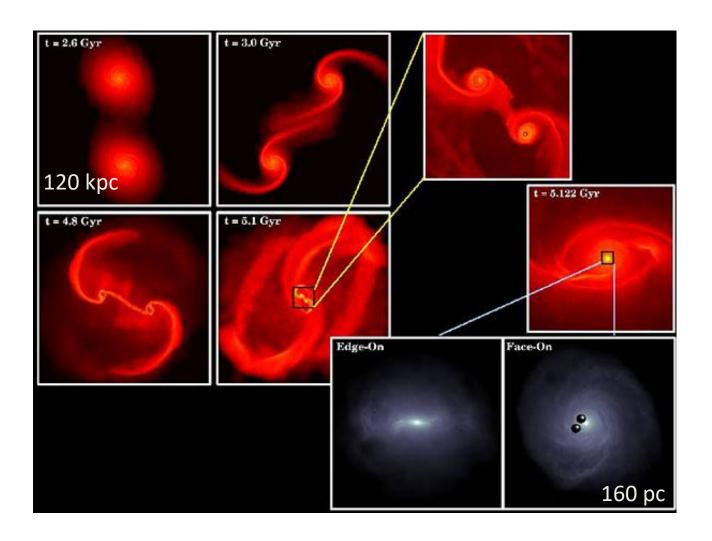
Circumbinary Accretion onto Black-Hole Binaries

Dong Lai(赖东)

Cornell University & T-D Lee Institute



Galaxy merger → SMBH binary in gas disk/torus



Some key questions:

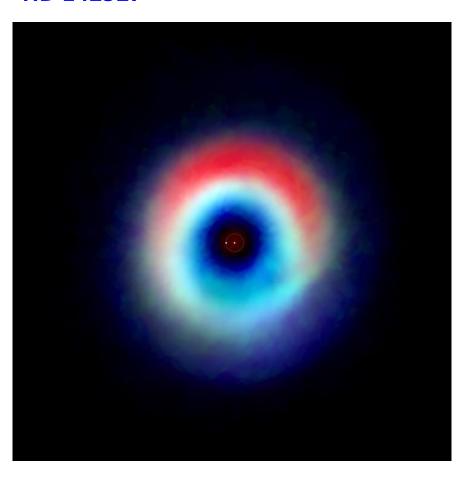
Accretion variability?

observational search for SMBH binaries. EM counterparts of low-freq. GWs (LISA, Pulsar timing arrays)

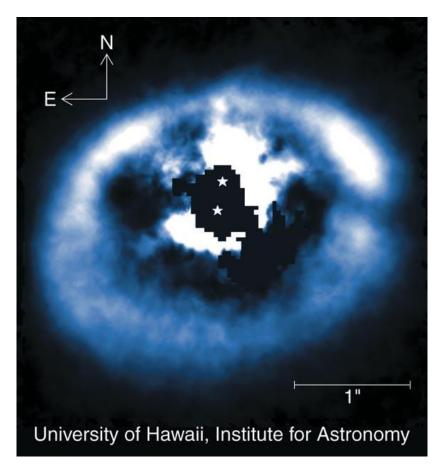
Long-term evolution of the binary? (Does the orbit decay?) final pc problem (?)

Disks around proto-stellar binaries

HD 142527



GG Tau



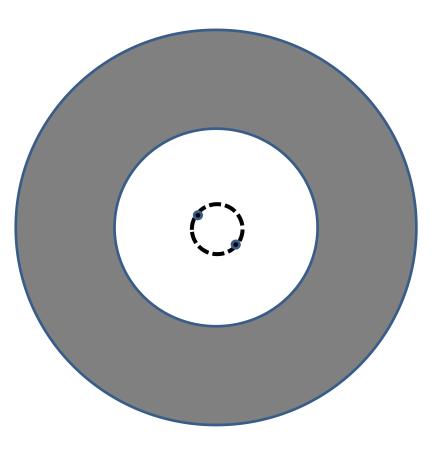
Outer disk: >100 AU Gap (cavity): 10-100 AU

Inner binary: ~20 AU

A. Isella/ALMA

Binary: ~60 AU

Disk around Binary: Gap/Cavity opening



Binary produces a gravitational potential on disk:

$$\Phi(\mathbf{r},t) = \sum_{m} \Phi_{mn}(r) \cos(m\phi - m\Omega_{b}t)$$

Transfer angular momentum to the disk through "Lindblad resonance":

$$m\Omega_b - m\Omega(r) = \kappa \simeq \Omega(r)$$

→ Disk is "pushed" outward

Viscosity → disk diffuses inward

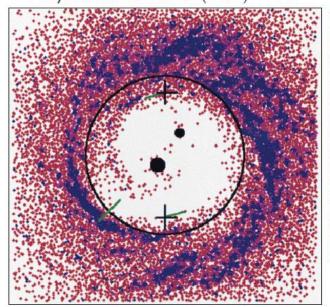
Cavity radius $\approx (2-3)a_b$

Simulations of Circumbinary Accretion

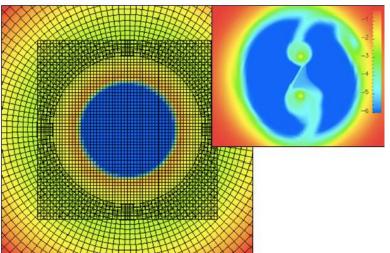
Artymowicz & Lubow 1996; Günther & Kley 02; MacFadyen & Milosavljević 08; Cuadra et al.09; Hanawa et al. 10; de Val-Borro et al. 11; Roedig et al. 12; Noble et al.12; Shi et al. 12; D'Orazio et al. 13; Pelupessy & Portegies-Zwart 13; Farris et al. 14; Shi & Krolik 15; Lines et al. 15; O'Ozario et al. 16; Ragusa et al. 16, Munoz & Lai 2016; Miranda, Munoz & Lai 2017; Tang et al. 17; Bowen et al.17,19; Munoz, Miranda, Lai 2019; Moody, Shi & Stone 19; Munoz, Lai et al.2020; Duffell et al.20; Tiede et al. 20; Heath & Nixon 20; D'Orazio & Duffell 21; Zrake et al.21; Penzlin et al.22; Siwek et al.22; Wang et al. 2023; Siwek et al. 2024; Duffell et al. 2024....

Some pioneering works:

Artymowicz & Lubow (1996) - SPH



Günther & Kley (2002) - Hybrid grid



Simulations of Circumbinary Accretion

Artymowicz & Lubow 1996; Günther & Kley 02; MacFadyen & Milosavljević 08; Cuadra et al.09; Hanawa et al. 10; de Val-Borro et al. 11; Roedig et al. 12; Noble et al.12; Shi et al. 12; D'Orazio et al. 13; Pelupessy & Portegies-Zwart 13; Farris et al. 14; Shi & Krolik 15; Lines et al. 15; O'Ozario et al. 16; Ragusa et al. 16, Munoz & Lai 2016; Miranda, Munoz & Lai 2017; Tang et al. 17; Bowen et al.17,19; Munoz, Miranda, Lai 2019; Moody, Shi & Stone 19; Munoz, Lai et al.2020; Duffell et al.20; Tiede et al. 20; Heath & Nixon 20; D'Orazio & Duffell 21; Zrake et al.21; Penzlin et al.22; Siwek et al.22, Wang et al.2023; Siwek et al. 2024; Duffell et al. 2024....

Many simulations excised the inner "cavity"

Some cover the whole domain: Circumbinary disk \rightarrow stream \rightarrow circumsingle disks:

Using finite-volume moving mesh codes:

DISCO: Farris, Duffell, MacFadyen, Haiman 2014...

AREPO: resolve accretion onto individual body to 0.02a_b

(Munoz & Lai 2016; Munoz, Miranda & Lai 2019; Munoz, Lai et al 2020...)

ATHENA++ (Moody, Shi & Stone 2019; Wang, Bai & Lai 2023)

Summary of Key Dynamical Results

- Short-term variabilities
- Long-term variabilities
- Angular momentum transfer and binary evolution

"Idealized" Simulations:

- -- Solve viscous hydrodynamic equations in 2D
- -- alpha viscosity, (locally) isothermal sound speed (or EOS with simple cooling)

```
Disk H/r \sim 0.1, \alpha = 0.05 - 0.1 (down to 0.01)
```

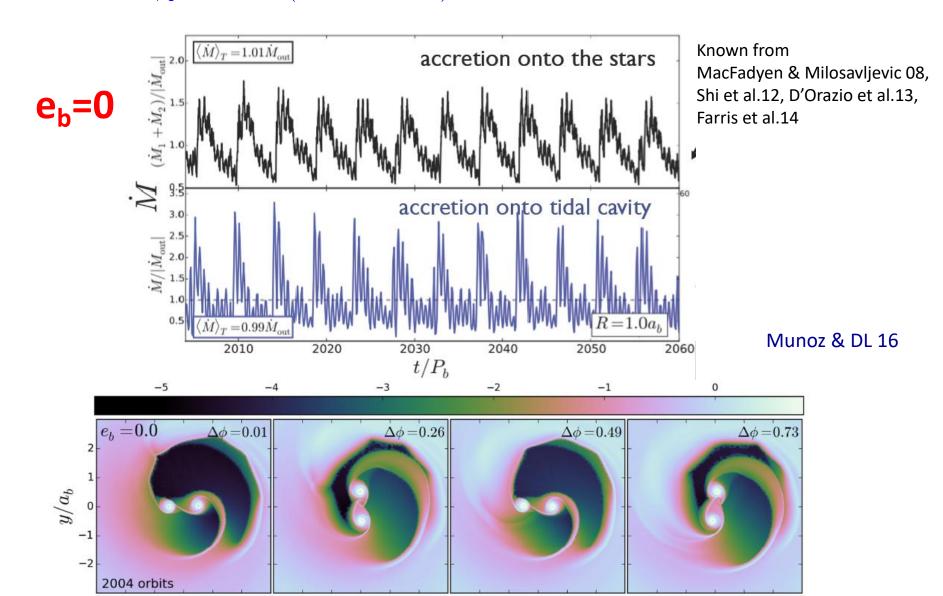
```
Our own works: with Diego Munoz (Harvard PhD'13->Cornell -> ... -> NAU)
Ryan Miranda (Cornell Ph.D.'17->IAS -> Data science)
Haiyang Wang (Fudan U.-> Caltech)
Xuening Bai (Tsinghua U)

Munoz & DL 2016, ApJ; Miranda, Munoz & DL 2017, MNRAS
Munoz, Miranda & DL 2019; Munoz, DL et al 2020; Wang, Bai, DL et al.2023a,b
```

REFs: Lai & Munoz 2023 ARAA + other recent papers...

Short-term (~P_b) Accretion Variabilities

For $e_b \lesssim 0.05$: $\dot{M} (= \dot{M}_1 + \dot{M}_2)$ varies at $\sim 5 P_b$ (Kepler period at $r_{\rm in}$ ~ 3a_b)



Short-term (~P_b) Accretion Variabilities

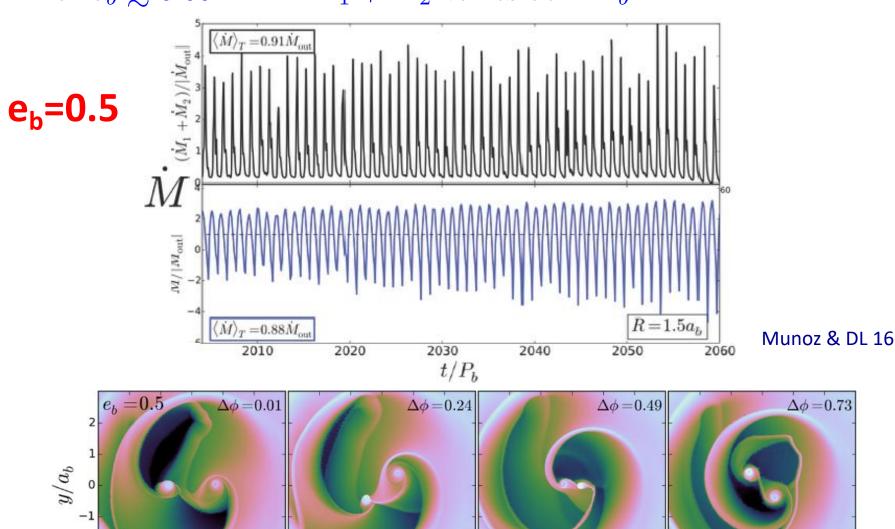
For $e_b \gtrsim 0.05$: $\dot{M} = \dot{M}_1 + \dot{M}_2$ varies at $\simeq P_b$

-2

2

-2

2004 orbits



-2

2

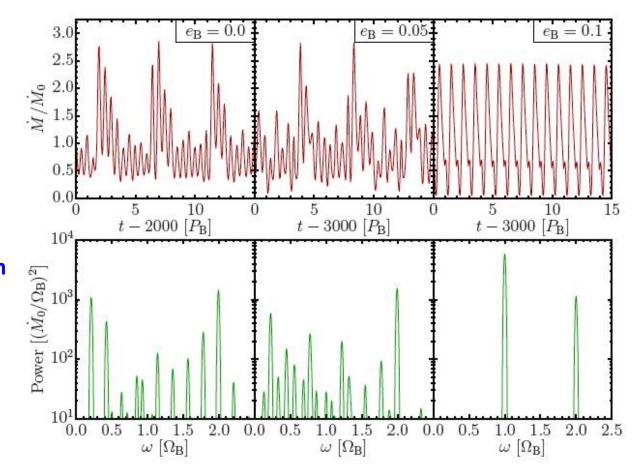
-2

2

Short-term (~P_b) Accretion Variabilities

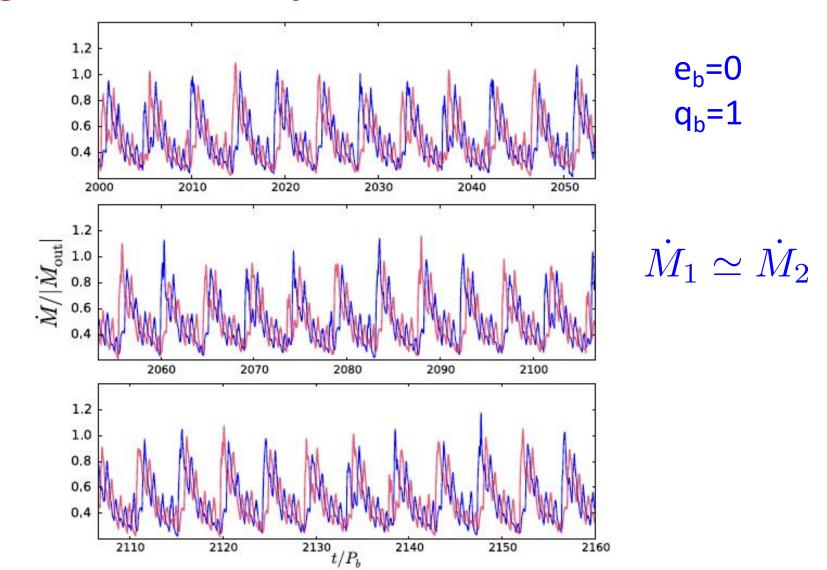
For $e_b \lesssim 0.05$: $\dot{M} (= \dot{M}_1 + \dot{M}_2)$ varies at $\sim 5P_b$

For $e_b \gtrsim 0.05$: $\dot{M} = \dot{M}_1 + \dot{M}_2$ varies at $\simeq P_b$

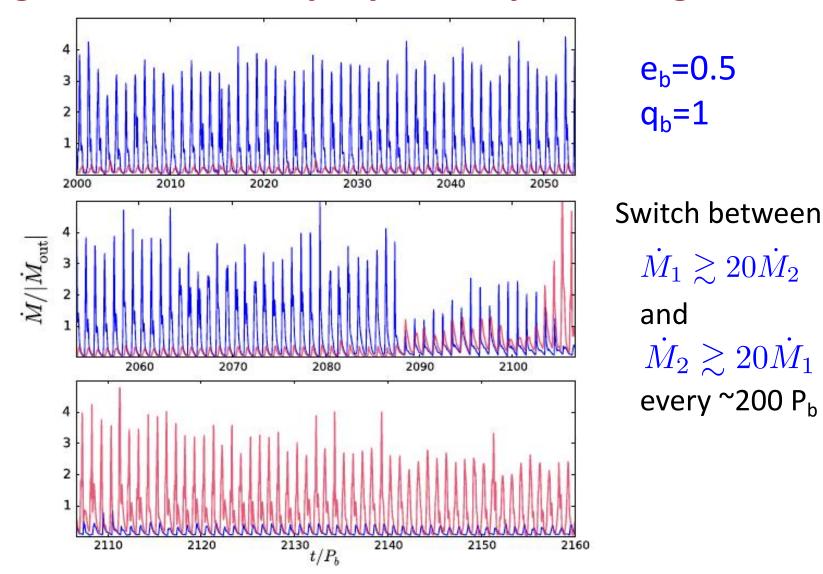


Power spectrum

Long-Term Variability:



Long-Term Variability: Symmetry Breaking

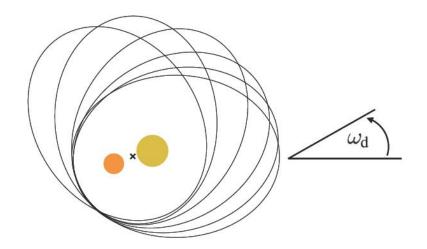


Single AGN with binary BHs?

Apsidal precession of eccentric disk around the binary

$$\dot{\omega}_{\rm d} \simeq \frac{3\Omega_{\rm b}}{4} \frac{q_{\rm b}}{(1+q_{\rm b})^2} \left(1 + \frac{3}{2}e_{\rm b}^2\right) \left(\frac{a_{\rm b}}{R}\right)^{7/2}$$
 $\sim 0.006 \,\Omega_{\rm b} \left(\frac{3a_{\rm b}}{R}\right)^{7/2},$

Precession period 200-300 P_b



Theory of eccentric disks around binary: see Miranda, Munoz & Lai 2017

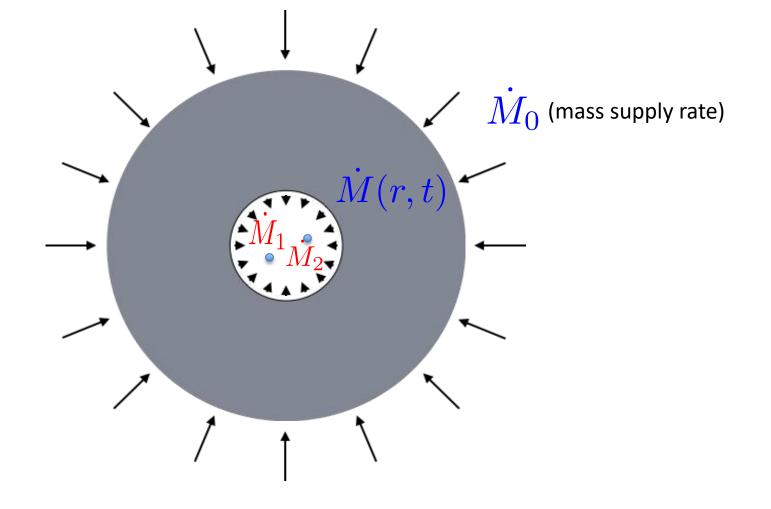
Munoz & Lithwick (2020)

Wang HY, Lai, Bai (2023)

Angular Momentum Transfer to Binary and Long-term Orbital Evolution

Many claims of orbital decays (1980s-2017): Suppressed accretion onto binary (?), binary loses AM through outer Lindblad torque ...

First indication that the binary may expand: Miranda, Munoz & Lai 2017 (using PLUTO, excised cavity)



 $\dot{M}(r,t), \dot{M}_1, \dot{M}_2$ are highly variable

Quasi-Steady State: $\langle \dot{M}(r,t) \rangle = \langle \dot{M}_1 \rangle + \langle \dot{M}_2 \rangle = \dot{M}_0$

Two ways of computing the torque on the binary:

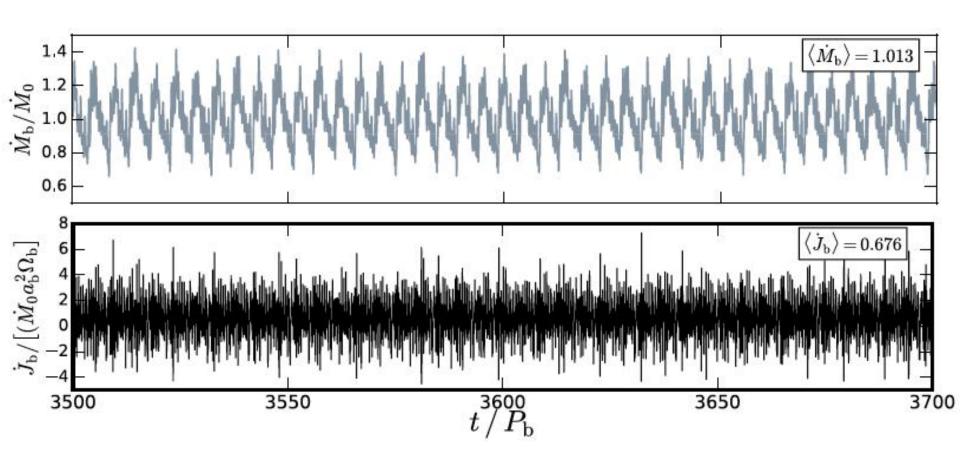
1. Direct computation:

Gravitational torque from all gas

+ Accretion torque (due momentum of accreting gas onto each star)

$$\dot{J}_b = (\dot{L}_b)_{\text{grav}} + (\dot{L}_b)_{\text{acc}} + (\dot{S}_1)_{\text{acc}} + (\dot{S}_2)_{\text{acc}}$$

Direct computation of torque on the binary



$$l_0 \equiv \frac{\langle \dot{J}_b \rangle}{\langle \dot{M}_b \rangle} = 0.68 a_b^2 \Omega_b$$

Angular momentum transfer to the binary per unit accreted mass

 $e_b = 0$

2. Angular Momentum Current (Transfer Rate) in CBD

$$\dot{J}(r,t) = \dot{J}_{\text{adv}} - \dot{J}_{\text{visc}} - T_{\text{grav}}^{>r}$$

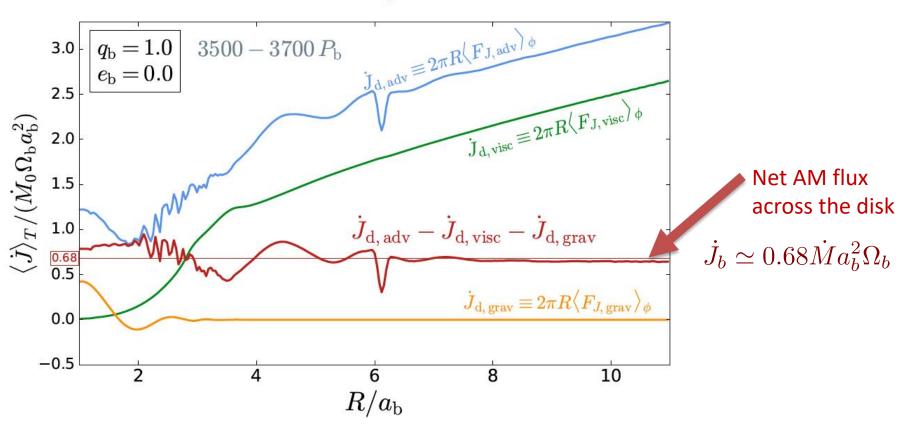
$$\dot{J}_{\text{adv}} = -\oint r^2 \Sigma u_r u_\phi d\phi$$

$$\dot{J}_{\text{visc}} = -\oint r^3 \nu \Sigma \left[\frac{\partial}{\partial r} \left(\frac{u_\phi}{r} \right) + \frac{1}{r^2} \frac{\partial u_r}{\partial \phi} \right] d\phi$$

$$T_{\text{grav}}^{>r} = \int_r^{r_{\text{out}}} \frac{dT_{\text{grav}}}{dr} dr, \qquad \frac{dT_{\text{grav}}}{dr} = -\oint r \Sigma \frac{\partial \Phi}{\partial \phi} d\phi$$

2. Angular Momentum Current (Transfer Rate) in CBD

$$\dot{J}(r,t) = \dot{J}_{\text{adv}} - \dot{J}_{\text{visc}} - T_{\text{grav}}^{>r}$$



Recap: Although the accretion flow is highly dynamical, the system reaches quasi-steady state:

$$\langle \dot{M}(r,t) \rangle = \langle \dot{M}_1 \rangle + \langle \dot{M}_2 \rangle = \dot{M}_0$$

 $\langle \dot{J}_b \rangle \simeq \langle \dot{J}_{\rm disk}(r,t) \rangle = {\rm const}$

Angular momentum transferred to the binary per unit accreted mass:

$$l_0\equiv rac{\langle\dot{J}_b
angle}{\langle\dot{M}_b
angle}=0.68a_b^2\Omega_b$$
 (for alpha=0.05-0.1, H/r=0.05-0.1)

Munoz, Miranda & DL 2019

Confirmed by Moody, Shi & Stone 2019 (ATHENA++)
Duffell et al. (2020,2024),

Implication of $\dot{J}_B > 0$:

For q = 1, $e_B = 0$ binary: $\dot{J}_B = \dot{M}_B l_0$ $l_0 \simeq 0.68 l_B$ where $l_B = a_B^2 \Omega_B$ $\Rightarrow \frac{\dot{a}_B}{a_B} = 8 \left(\frac{l_0}{l_B} - \frac{3}{8} \right) \frac{\dot{M}_B}{M_B}$

Binaries can expand due to circumbinary accretion!

For e_B=0:
$$\frac{\dot{a}_B}{a_B} \simeq 2.68 \frac{\dot{M}_B}{M_B}$$

Eccentric Binaries

To obtain \dot{a}_b and \dot{e}_b , we need \dot{J}_b and \dot{E}_b

$$\mathcal{E}_b \equiv \frac{1}{2}\dot{\mathbf{r}}_b^2 - \frac{GM_b}{r_b}$$
 where $\mathbf{r}_b = \mathbf{r}_1 - \mathbf{r}_2$, $M_b = M_1 + M_2$

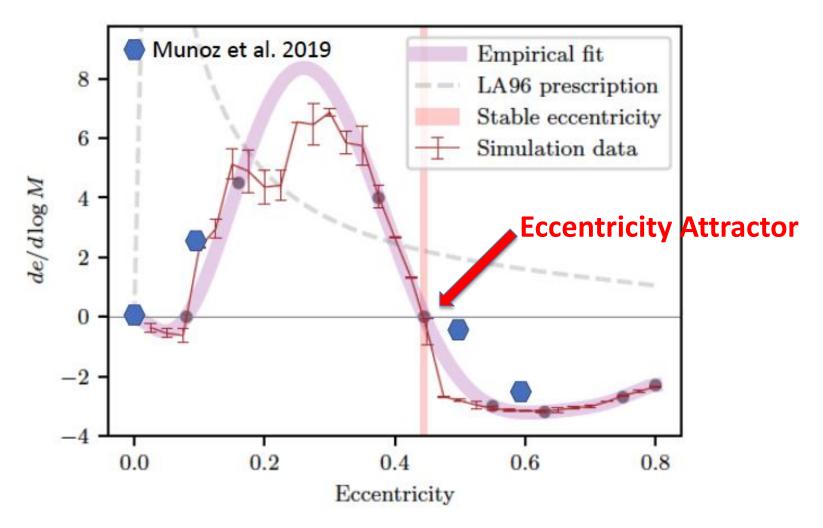
$$\frac{d\mathcal{E}_b}{dt} = -\frac{G\dot{M}_b}{r_b} + \dot{\mathbf{r}}_b \cdot (\mathbf{f}_1 - \mathbf{f}_2)$$

$$\mathbf{f}_1 = (\text{force/mass on } M_1) = \mathbf{f}_{1,\text{gravity}} + \mathbf{f}_{2,\text{accretion}}$$

Munoz et al. 2019

e_b	$\dot{J}_b \left[\dot{M}_b a_b^2 \Omega_b \right]$	$\dot{a}_b/a_b \left[\dot{M}_b/M_b\right]$	$\dot{e}_b \left[\dot{M}_b / M_b \right]$
0	0.68	2.2	0.0
0.1	0.43	0.75	2.4
0.5	0.78	0.95	-0.20
0.6	0.81	0.47	-2.34

Eccentric Binaries



Zrake et al. 2021 See also D'Orazio & Duffell 2021 Siwek et al. 2023,2024

$$q = M_2/M_1 < 1$$

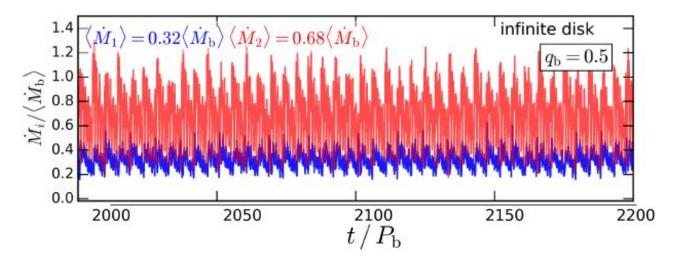
 $e_b=0 \quad$ Munoz, Lai, Kratter, Miranda 2020

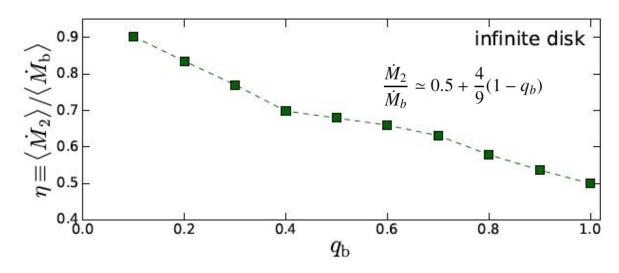
See also Duffell+2020,2024; Siwek et al 2024

$$q=M_2/M_1<1$$
 $e_b=0\,$ Munoz, Lai et al 2020

-- Low-mass component accretes more

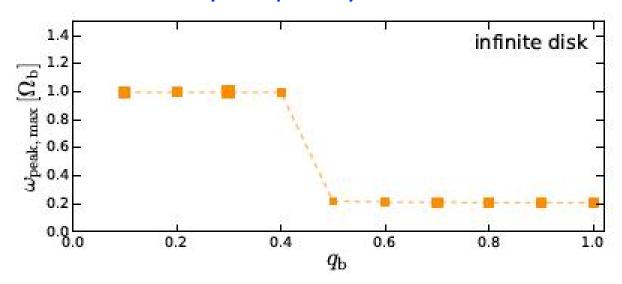
See also Bate+2000; Farris+2014





$$q=M_2/M_1<1$$
 $e_b=0$ Munoz, DL +2020

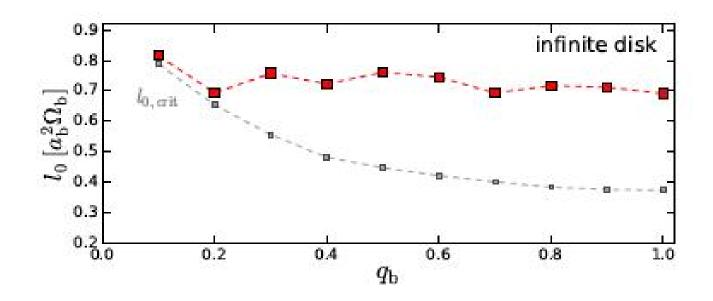
-- Dominant variability frequency



$$q = M_2/M_1 < 1$$

$$e_b = 0$$
 Munoz, DL +2020

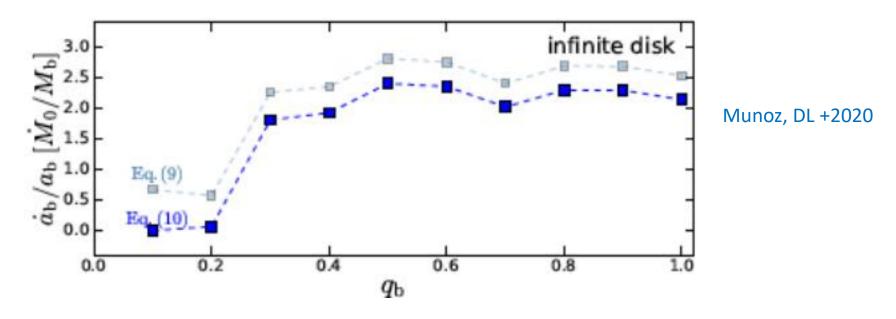
-- Angular momentum transfer



$$q = M_2/M_1 < 1$$

$$e_b = 0$$

-- Orbit evolution



See also Duffell et al. 2020: $\dot{a}_b < 0 \,\, {
m for} \,\, q_b \lesssim 0.05$

Unequal-mass, eccentric binaries:

Siwek et al. 2023

Recap:

In quasi-steady state, comparable-mass binary can expand while accreting from CBD

Eccentricity attractor: ~0.4

Is binary decay possible?

e.g. Supermassive BH Binaries, final pc problem

Is binary decay possible?

e.g. Supermassive BH Binaries, final pc problem

Yes/maybe...

e.g. Thin (low-viscosity) disks

"steady-state"? finite torus = mass-fed disk? Pressure?

Tiede et al. 2022,2024

e.g. Large (locally) massive disk:

$$\Sigma \pi a_b^2 \gtrsim M_2$$

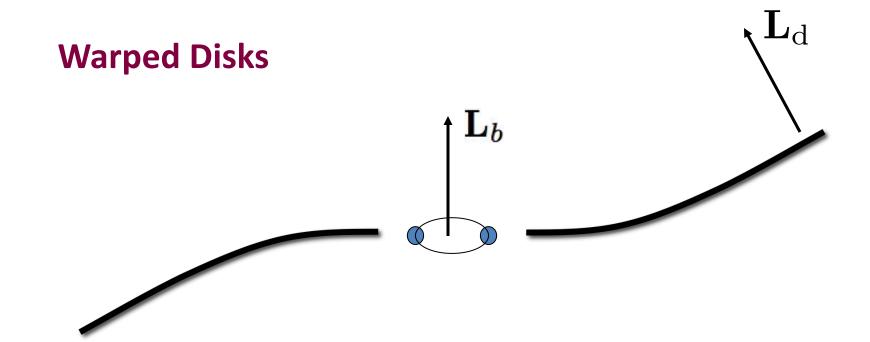
e.g. Gas could get ejected in outflow (?)...

Caveats of 2D viscous hydro simulations:

Equation of state/cooling (Haiyang Wang et al 2023) B fields, turbulence.....

So far: Co-planar disks

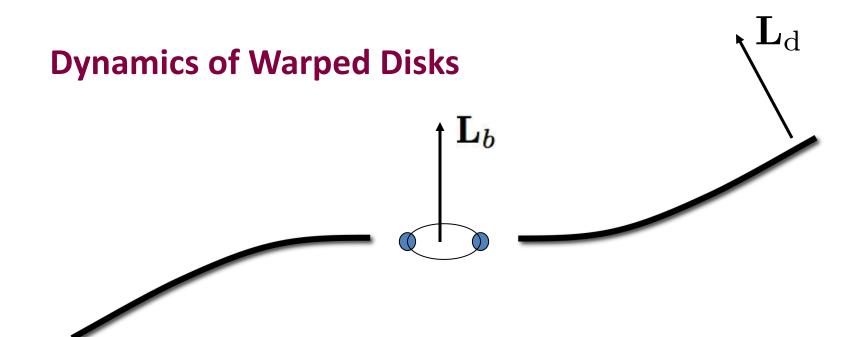
What about misaligned disks?



Torque from binary on disk => disk (ring) nodal precession

$$\Omega_p(r) \simeq \frac{3\mu}{4M_t} \left(\frac{a}{r}\right)^2 \Omega(r)$$

Differential precession + internal fluid stress ==> warped/twisted disk



Warp + Viscosity \rightarrow Dissipation \rightarrow Align L_b and L_d

$$\begin{split} \frac{\partial \hat{\mathbf{l}}}{\partial \ln r} \sim \frac{\alpha}{c_{\mathrm{s}}^2} \mathbf{T}_{\mathrm{ext}} & |\mathbf{T}_{\mathrm{ext}}| \sim r^2 \Omega \, \omega_{\mathrm{ext}}, \quad \omega_{\mathrm{ext}} = \Omega_{\mathrm{prec}} \\ \left| \frac{\mathrm{d} \hat{\mathbf{l}}}{\mathrm{d} \, t} \right|_{\mathrm{visc}} \sim \left\langle \left(\frac{\alpha}{c_{\mathrm{s}}^2} \right) \frac{\mathbf{T}_{\mathrm{ext}}^2}{r^2 \Omega} \right\rangle \sim \left\langle \frac{\alpha}{c_{\mathrm{s}}^2} (r^2 \Omega) \omega_{\mathrm{ext}}^2 \right\rangle \end{split}$$

Typical alignment time can be short (~ precession period)

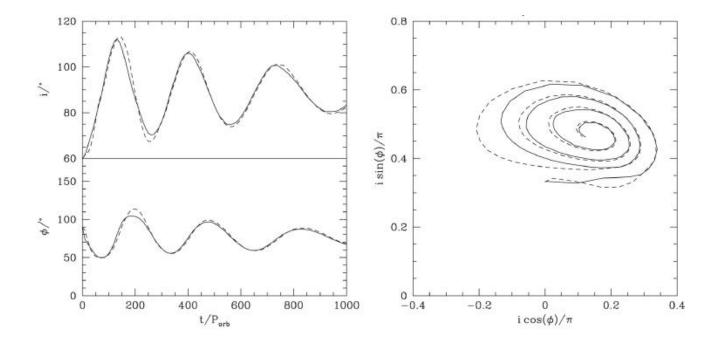
Foucart & DL 2014 Zanazzi & DL 2018

Surprise: Disk around eccentric binary may evolve toward polar alignment

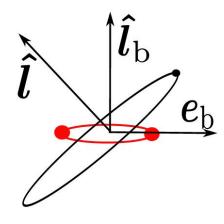
Martin & Lubow (2017): viscous hydro simulation using SPH

Initial disk-binary inclination $I(0) = 60^{\circ}$

Binary eccentricity $e_b = 0.5$.

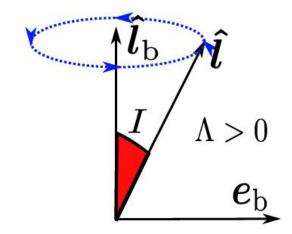


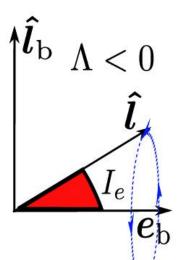
Theoretical Understanding of Polar Alignment of Disks Around Eccentric Binaries



Test particle around eccentric binary has two "masters"

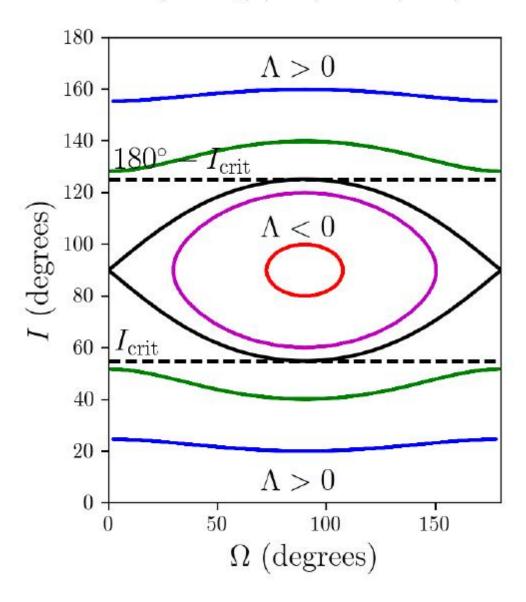
$$\Lambda = (1 - e_{\rm b}^2)(\hat{\boldsymbol{l}} \cdot \hat{\boldsymbol{l}}_{\rm b})^2 - 5(\hat{\boldsymbol{l}} \cdot \boldsymbol{e}_{\rm b})^2$$





Zanazzi & Lai 2018

$$\Lambda = (1 - e_{\rm b}^2)(\hat{\boldsymbol{l}} \cdot \hat{\boldsymbol{l}}_{\rm b})^2 - 5(\hat{\boldsymbol{l}} \cdot \boldsymbol{e}_{\rm b})^2$$



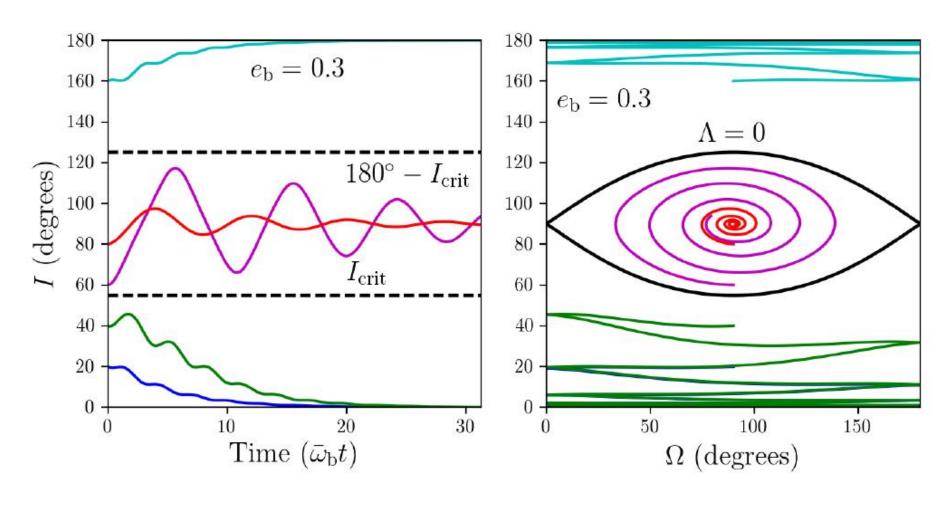
For \hat{l} to precess around \hat{e}_b , require $\sin I > \sin I_{\rm crib}$

$$I_{\text{crit}} = \cos^{-1} \sqrt{\frac{5e_{\text{b}}^2}{1 + 4e_{\text{b}}^2}}$$

Zanazzi & DL 2018

Warped viscous disk around eccentric binary

Evolve towards either align (anti-align) or polar align with the binary

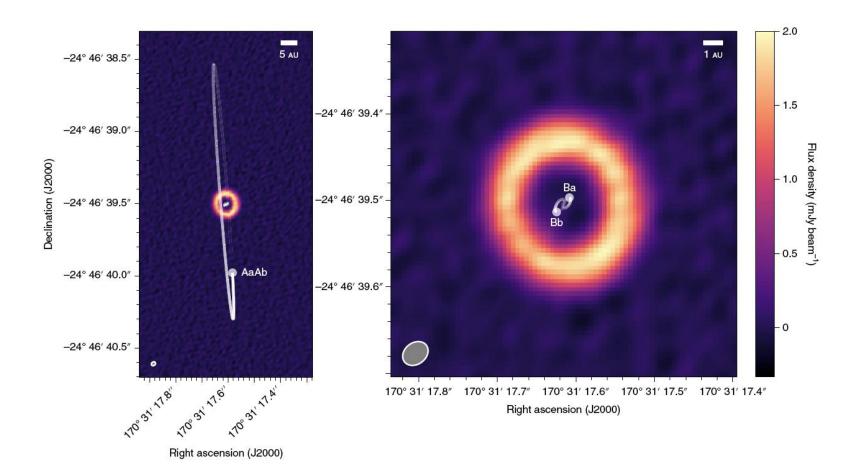




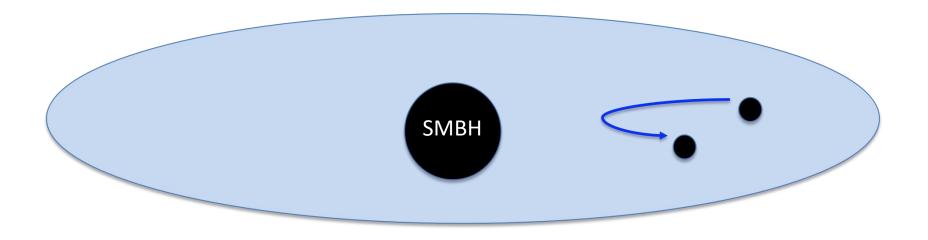
Corrected: Publisher Correction

A circumbinary protoplanetary disk in a polar configuration

Grant M. Kennedy 1.2*, Luca Matrà, Stefano Facchini 4.5, Julien Milli, Olja Panić, Daniel Price 8.9, David J. Wilner 3, Mark C. Wyatt and Ben M. Yelverton



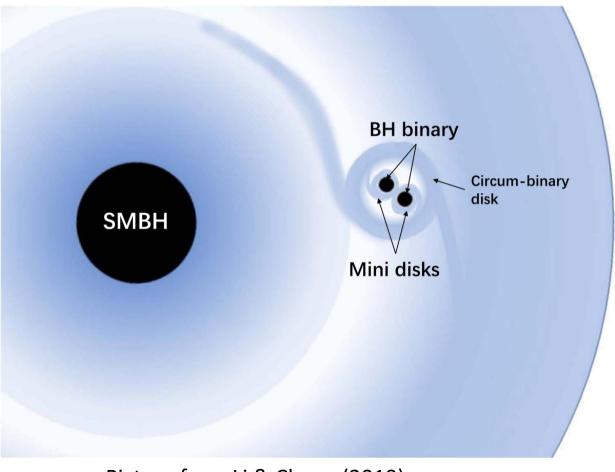
Small Binary embedded in ANG Disk



Binary BH mergers in AGN disks?

McKernan+12, Bellovary+16, Bartos+17, Stone+17, McKernan+18, Secunda+18, Yang+19, Tagawa+20, etc

Is it like "Circumbinary Accretion"?



Not clear in general What is Mdot? How does binary evolve?

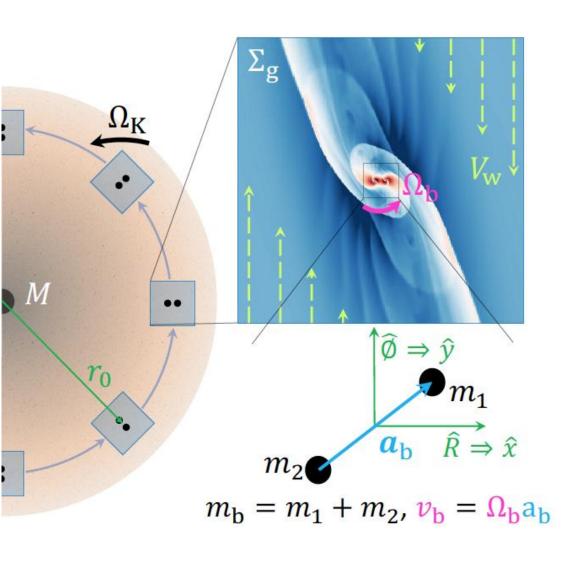
Picture from Li & Cheng (2019)

Numerical studies:

Baruteau et al. 2011 Y.Li,... H.Li... 2021 Dempsey, H.Li... 2023 R.Li & DL 2022,23,24

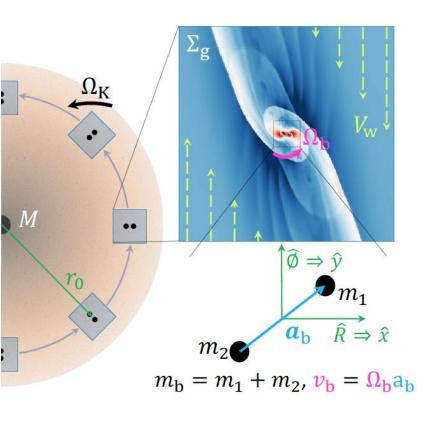
Local simulations of binary in disk

Rixin Li & Lai 2022,2023,2024



Local shearing box (not "local wind tunnel box" used by Kaaz et al. 2021)

ATHENA
Mesh refinement
Resolution: $a_b \sim 250$ cells
zero softening in gravity



Length scales of the problem:

$$a_b, R_{\rm B} \sim \frac{Gm_b}{c_{\infty}^2}, R_{\rm H} \sim r_0 \left(\frac{m_b}{M}\right)^{1/3}, H$$

Velocity scales of the problem:

$$v_b, c_\infty, V_{\rm shear}$$

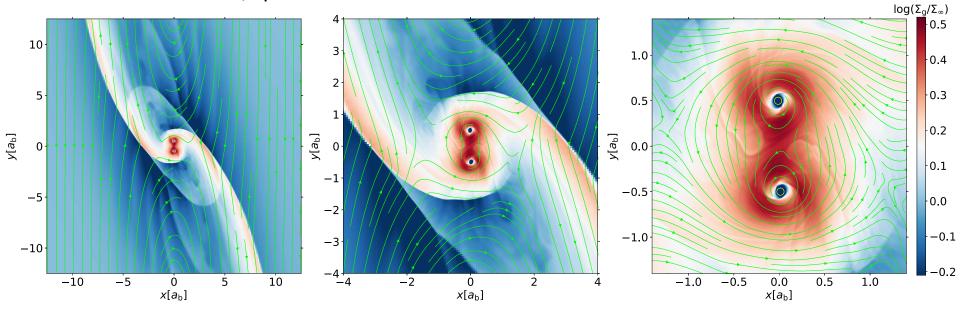
→ Dimensionless ratios:

$$\frac{q}{h^3}$$
, $\frac{R_{\rm H}}{a_b} \equiv \lambda$
where $q = m_b/M$, $h = H/r_0$

$$m_2/m_1$$
, e_b , EOS (e.g. γ law)

Example of flow structure

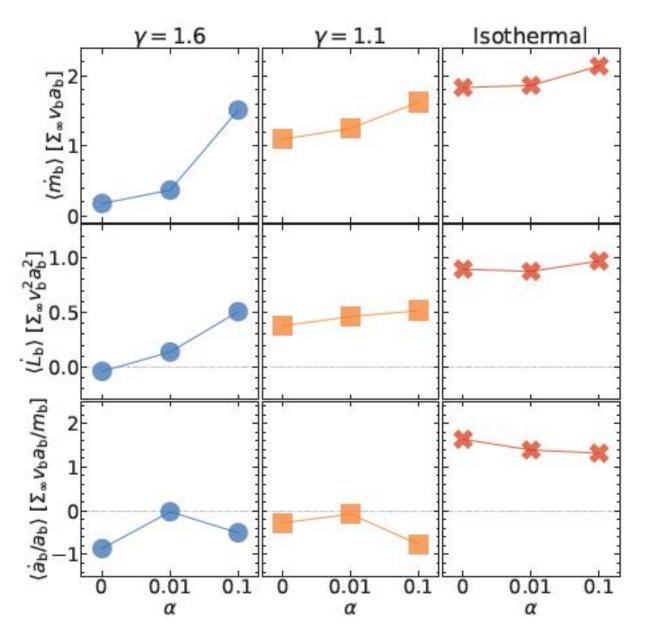
Pairs of bow shocks, spiral shocks



BH = absorbing sphere: sink radius: $r_{\rm sink} = 0.04~a_{\rm b} \simeq 10~{\rm cells}$

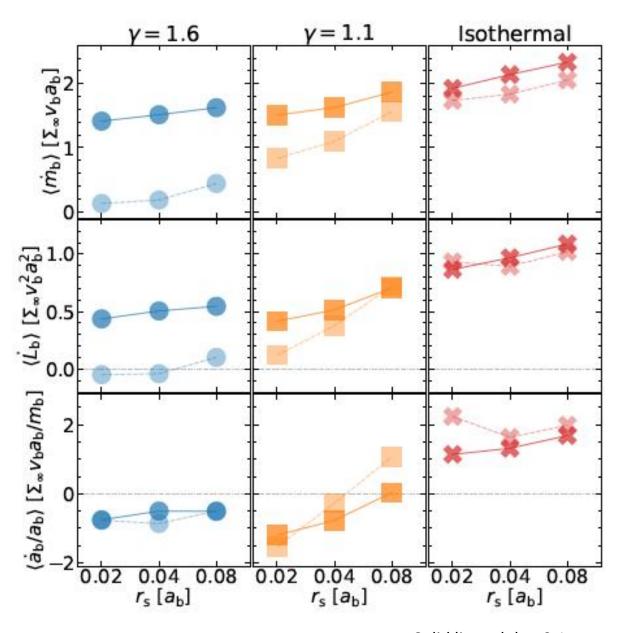
Force on each BH: from gravity + accretion + pressure

lacktriangle Torque on binary, energy transfer rate lacktriangle $\dot{a}_b, \quad \dot{e}_b$



Rixin Li & DL 2024

$$rac{m_1}{m_2}=1,\;e_b=0,\;rac{R_{
m H}}{H}=\left(rac{q}{h^3}
ight)^{\!1/3}\!\!=3^{1/3},\;rac{R_{
m H}}{a_{
m b}}=5$$
 prograde



Solid line: alpha=0.1 Dashed line: alpha=0

Recap: Embedded binaries in gas disks

Prograde binaries:

Orbital decay or expansion? Depends on gas thermodynamics, viscosity, size of accretor...

Retrograde binaries:

Always orbital decay

In general, orbital evolution of the binary is much faster than migration of the center of mass of binary in AGN disk.

Summary

Understanding circumbinary accretion is

Important: connect to SMBH binaries, PPDs and planets
Challenging: long-term secular effect in the presence of highly dynamical flows

Key Recent Results:

- -- short-term variabilities: $\sim 5 P_b$ (for $e_b \sim 0$) vs P_b (finite e_b or q<0.4)
- -- Small-mass accretes more; symmetry breaking in accretion (q=1, finite e_b)
- -- Binary can gain angular momentum and can expand (q>0.1)
- -- Eccentricity attractor e_b~0.4

Misaligned Disks

- -- Dissipation leads to either alignment or polar alignment with binary
- ♦ Binary in a Big Disk

Reference: Lai & Munoz 2023, ARAA +