



Dark Matter Freeze-out via **Catalyzed Annihilation**

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The DM+nu forum @TDLI/SJTU

Oct. 13, 2021



1/ Dark Matter Overview

2/ Thermal Freeze-out

3/ Catalyzed Annihilation

4/ Summary

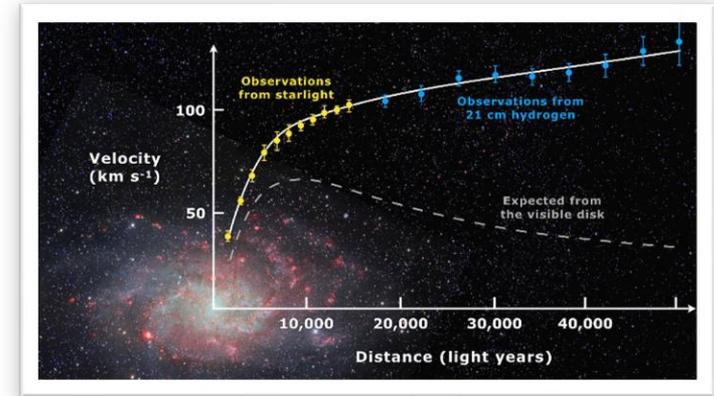
PART 01

Dark Matter Overview

► Existence of Dark Matter

Lots of evidence:

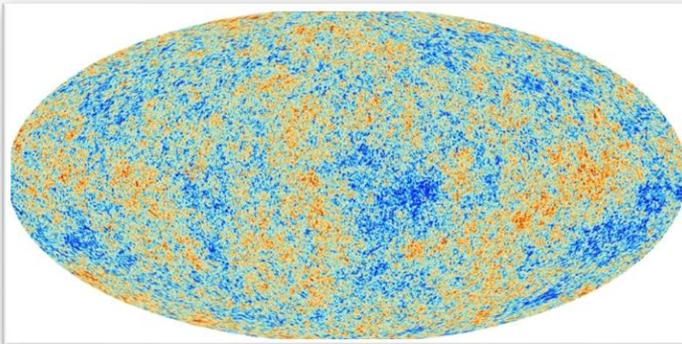
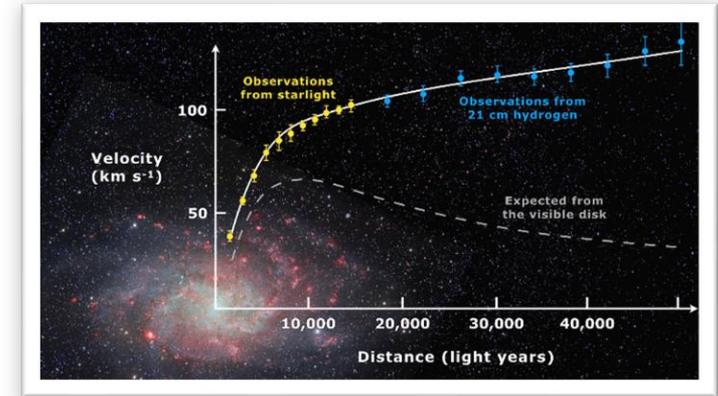
1. Galaxy rotation curves.



► Existence of Dark Matter

Lots of evidence:

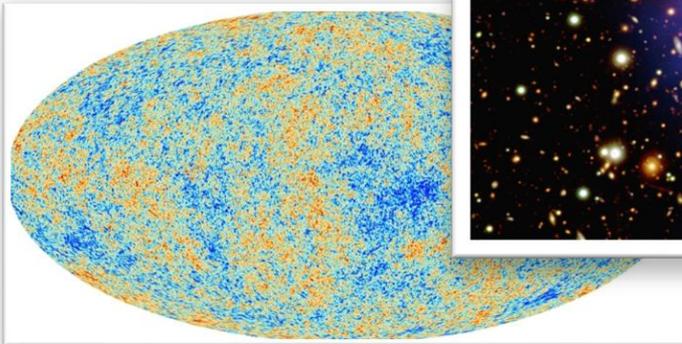
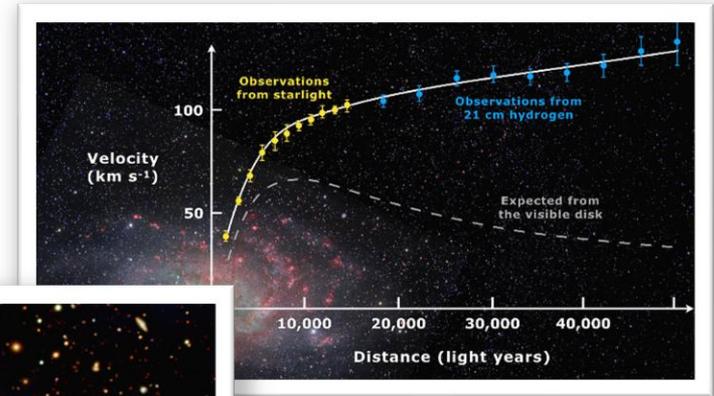
1. Galaxy rotation curves.
2. CMB.



► Existence of Dark Matter

Lots of evidence:

1. Galaxy rotation curves.
2. CMB.
3. Bullet cluster.
4. ...



Pink: X-ray image;
Blue: gravitational lensing

arXiv:astro-ph/0608407

►► What do we know about DM?

1/ Stable.

- If DM decays, its lifetime is longer than the age of the Universe.
 $\tau \gtrsim 10^{17} \text{s}$.
- Much more stringent bound from CMB.
 $\tau \gtrsim 10^{25} \text{s}$.

arXiv:1308.2578

►► What do we know about DM?

1/ Stable.

2/ Dark.

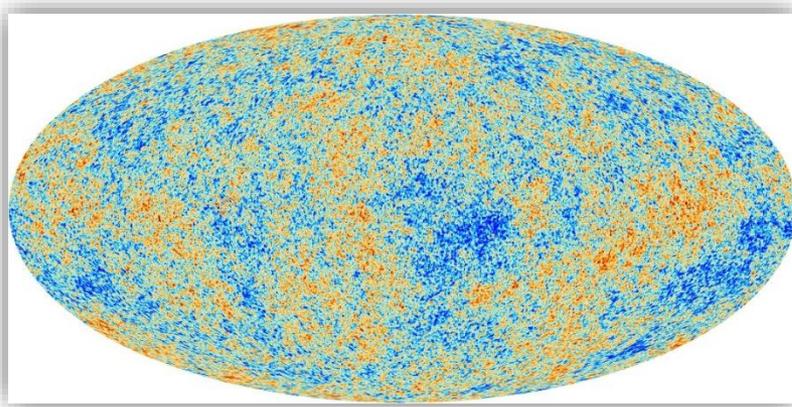
- DM is neutral.
- Or its electric charge is tiny.

► What do we know about DM?

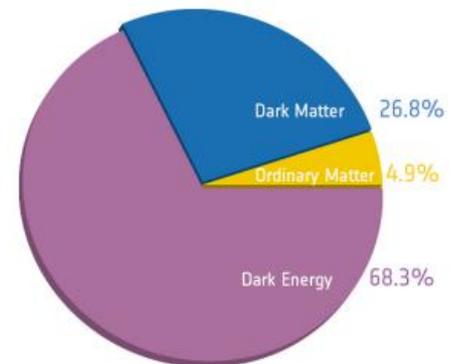
1/ Stable.

2/ Dark.

3/ DM abundance. $\Omega h^2 = 0.12$

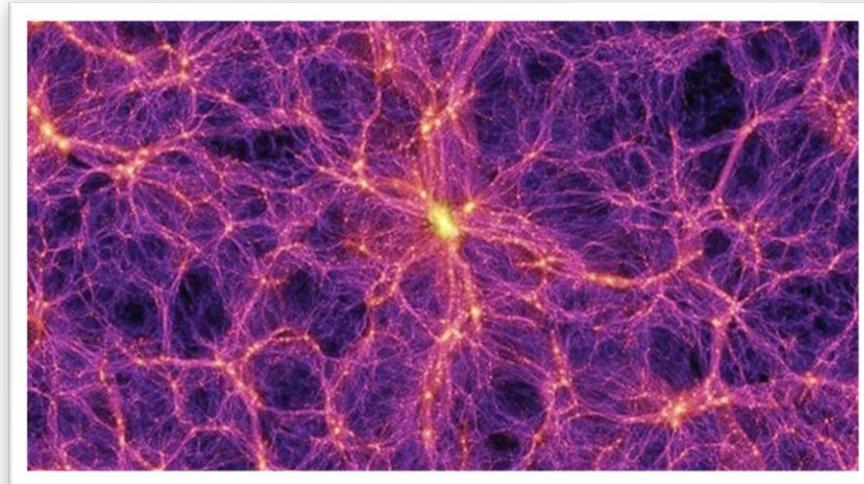


Planck Collaboration.



► What do we know about DM?

- 1/ Stable.
- 2/ Dark.
- 3/ DM abundance. $\Omega h^2 = 0.12$
- 4/ Seed structures in the universe.



► What do we know about DM?

1/ Stable.

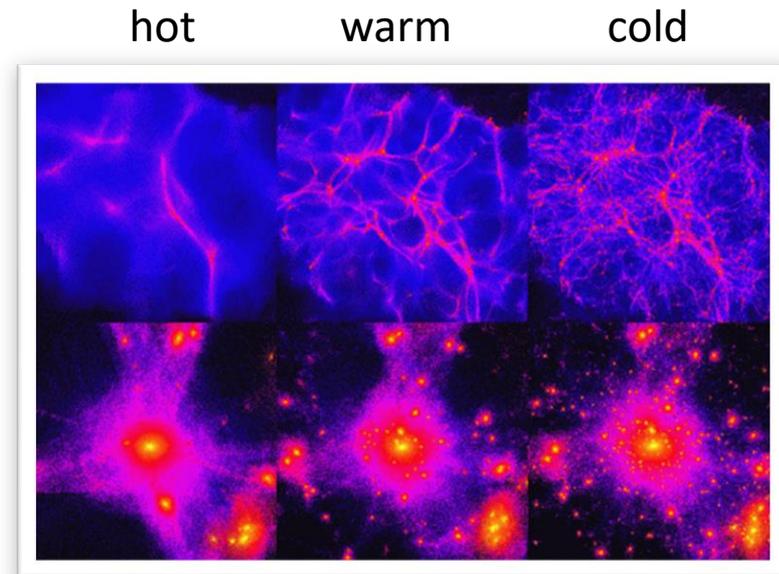
2/ Dark.

3/ DM abundance. $\Omega h^2 = 0.12$

4/ Seed structures in the universe.

5/ Cold.

Non-relativistic: kinetic energy \ll mass.



►► What do we know about DM?

1/ Stable.

2/ Dark.

3/ DM abundance. $\Omega h^2 = 0.12$

4/ Seed structures in the universe.

5/ Cold.

Question of the day:

What does it tell us?

PART 02

Thermal Freeze-out

►► What is thermal freeze-out

Thermal freeze-out:

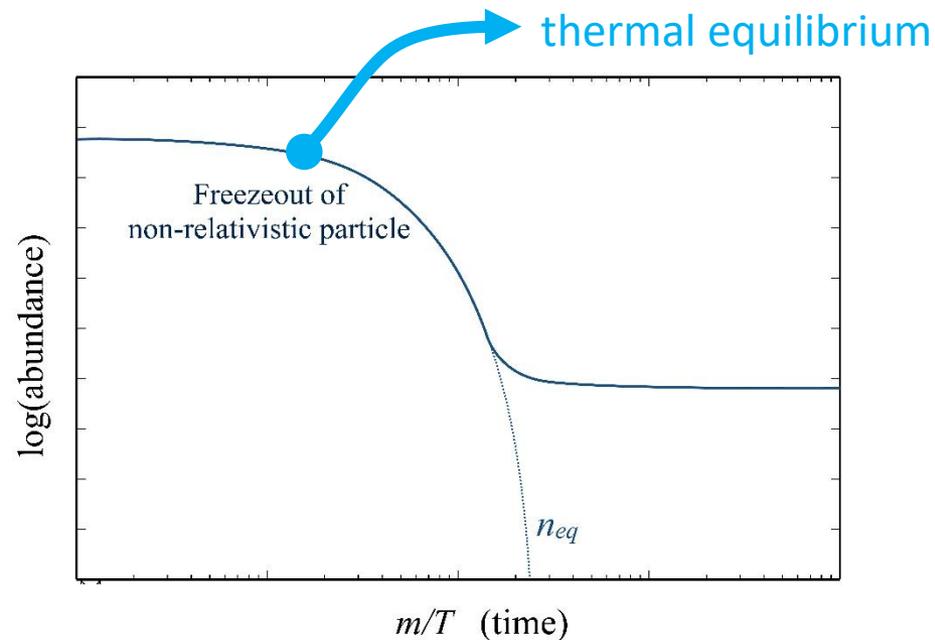
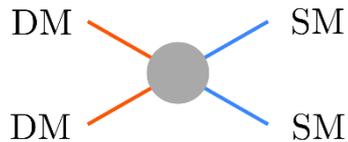
- In the early universe, DM keeps in **thermal equilibrium with SM particles**.

►► What is thermal freeze-out

Thermal freeze-out:

- In the early universe, DM keeps in **thermal equilibrium** with **SM particles**.

Example:

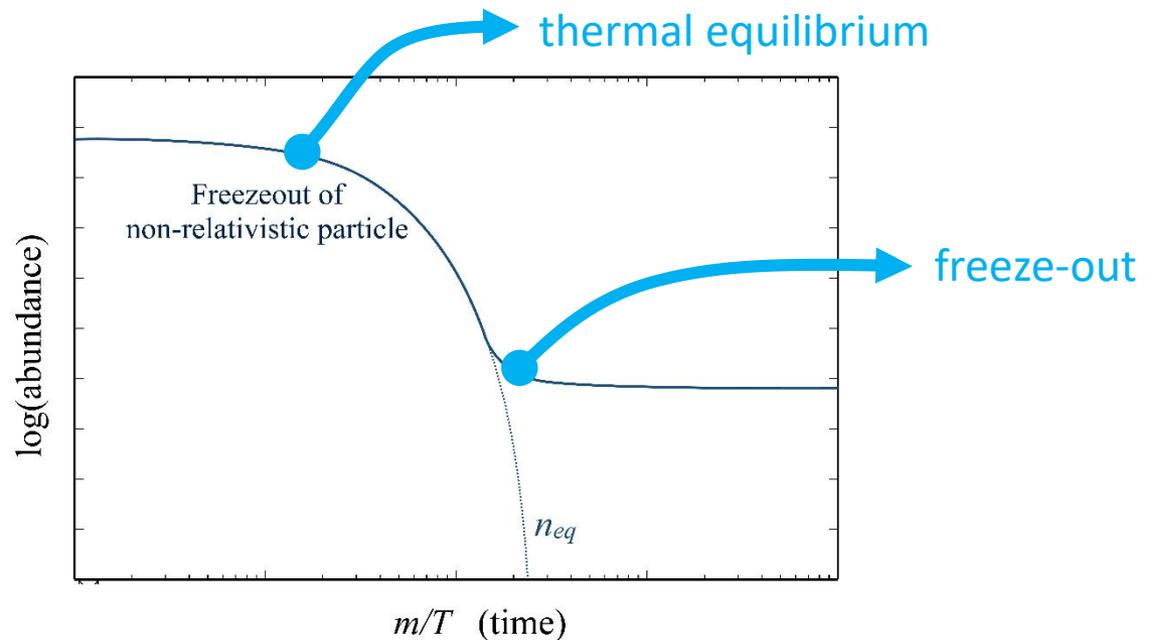
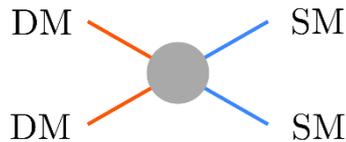


►► What is thermal freeze-out

Thermal freeze-out:

- In the early universe, DM keeps in **thermal equilibrium with SM particles**.
- As the universe expands, DM **drops out of equilibrium** to its observed abundance.

Example:

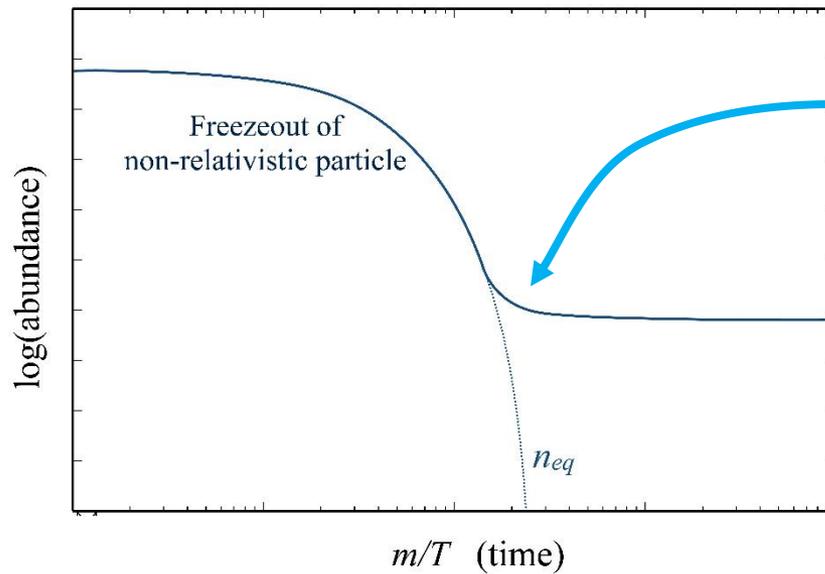
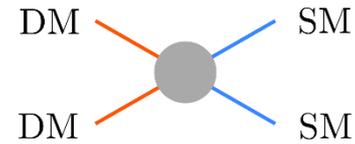


Why is thermal freeze-out appealing:

- **Reasonable!**
SM relics (photons, neutrinos, nuclei) are determined by this mechanism.
- **Testable!**
Thermal equilibrium implies interaction between DM and SM.
- **Insensitive to initial conditions!**
What happens before freeze-out is not related.

► To determine DM abundance

Condition for freeze-out and DM abundance:

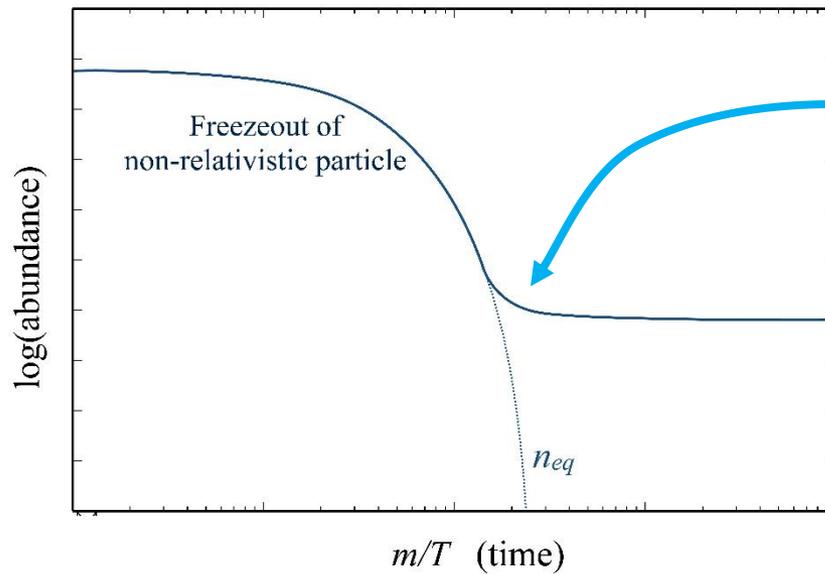
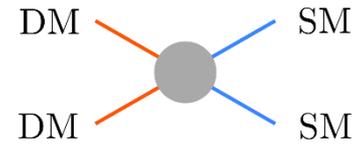


$$\Gamma_{DM \rightarrow SM} \simeq H.$$

Γ : annihilation rate;
 H : Hubble constant.

► To determine DM abundance

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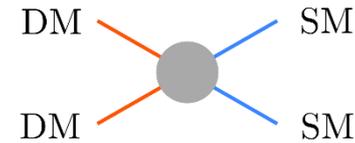


$$\Gamma_{\text{DM} \rightarrow \text{SM}} \simeq H.$$

$$\Omega h^2 = 0.12$$

$$\langle \sigma v \rangle \approx 2 \times 10^{-26} \text{ cm}^3/\text{s}$$

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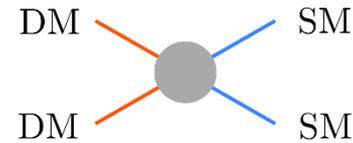


1. $O(1)$ coupling. (Weakly interacting)
2. 100GeV mass. (massive particles)

WIMPs

► WIMPs

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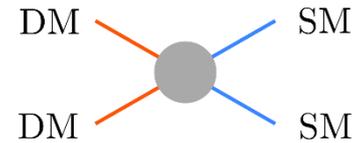
WIMPs



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Electroweak

Condition for freeze-out and DM abundance:



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“WIMP Miracle”

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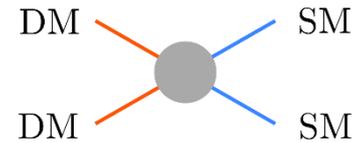


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WIMPs



1. $O(1)$ coupling.
2. 100GeV mass.

Electroweak

SUSY DM
composite DM
...

► Boltzmann equation

Quantitatively, we should solve for the Boltzmann equations to get DM abundance.

$$\frac{dn_\chi}{dt} + 3Hn_\chi = -\langle\sigma v\rangle_{\chi\bar{\chi}\rightarrow\phi\phi} [n_\chi^2 - n_\chi^{\text{eq}2}]$$

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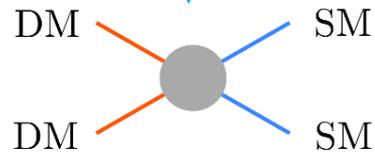


- The expansion of the Universe.
- Radiation dominated.

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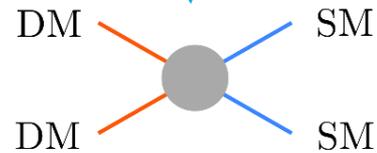


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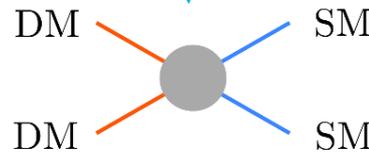
- The expansion of the Universe.
- Radiation dominated.

- Annihilation and inverse annihilation
- Squared for 2 particle interaction

► Boltzmann equation

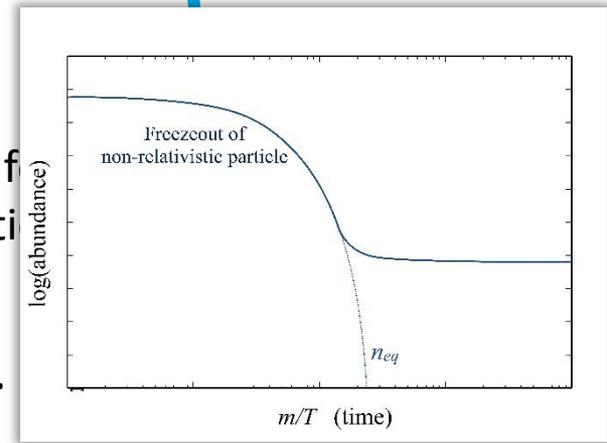
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- The expansion of the Universe.
- Radiation dominated.

- Squared f
- Annihilation



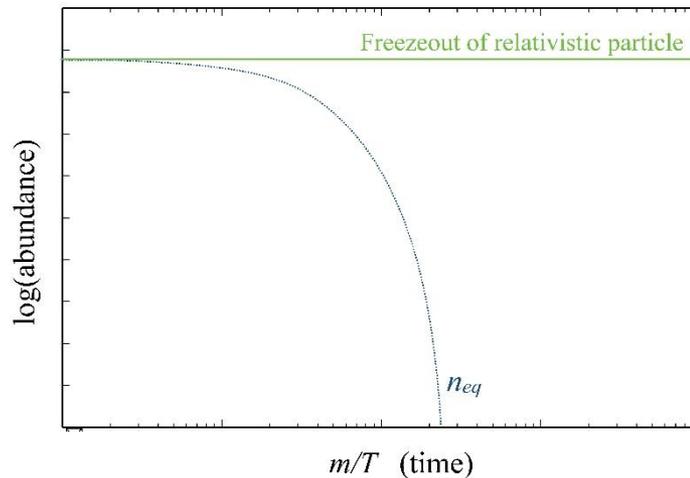
The Boltzmann equation can be solved numerically.

► Mass range



Lower bound:

Since $\rho \simeq m_{DM} \cdot n$, small DM mass indicates large number density.



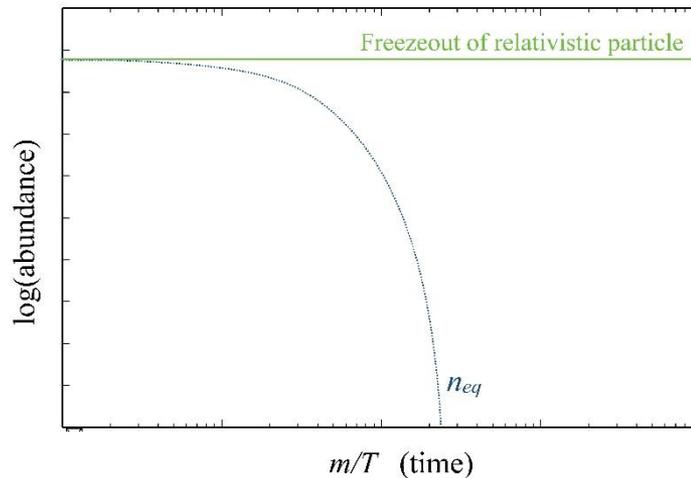
$$\Omega_{\chi} h^2 \simeq 0.12 \times \frac{g}{g_{*,S}(T_{fo})} \left(\frac{m_{\chi}}{2 \text{ eV}} \right).$$

► Mass range



Lower bound:

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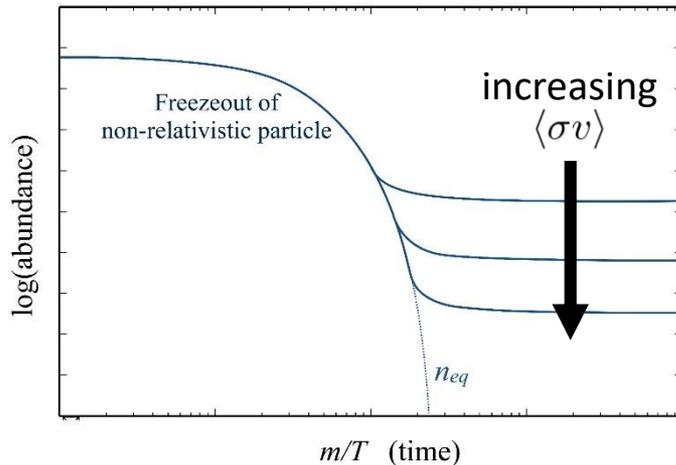
$$m_{DM} \gtrsim 1 \text{ eV}$$

► Mass range



Upper bound:

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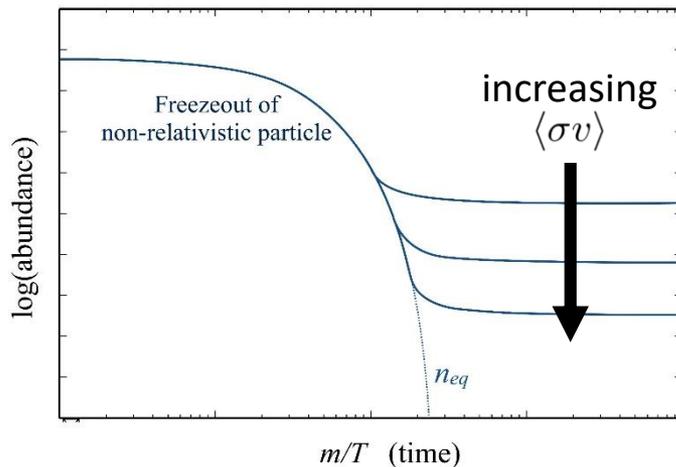


► Mass range



Upper bound:

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Unitarity limit for 2 DM annihilation:

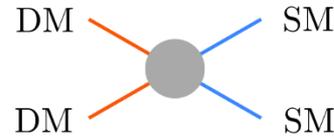
$$\sigma v \leq \frac{4\pi}{m_{DM}^2 v}$$



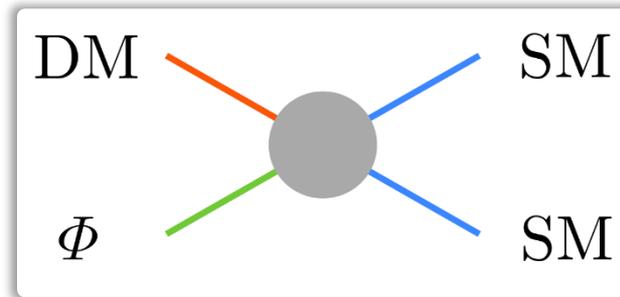
$$m_{DM} \lesssim 100\text{TeV}$$

►► The WIMP neighborhood

Beyond self-annihilation:



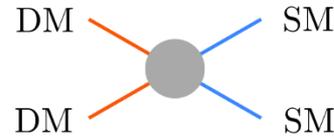
- Co-annihilation.



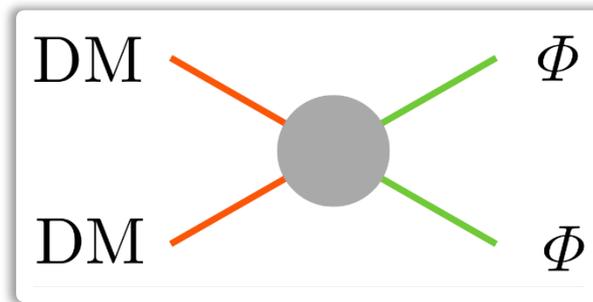
- DM and Φ are both odd under dark $U(1)$ or Z_2 .
- $m_\Phi > m_{DM}$ to ensure DM stability.

► The WIMP neighborhood

Beyond self-annihilation:



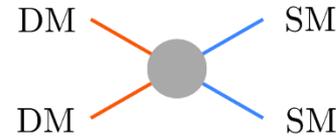
- Co-annihilation.
- Forbidden annihilation.



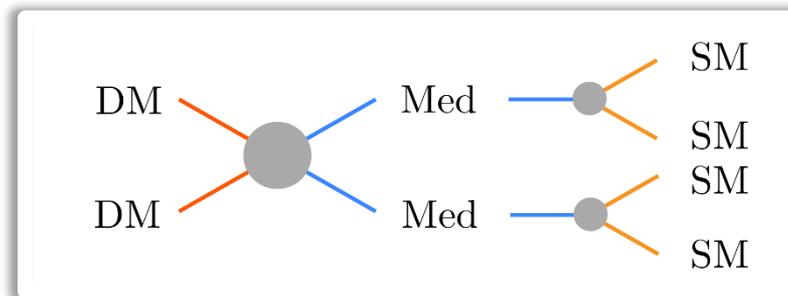
- DM annihilation to heavier states dominated. $m_{\Phi} > m_{DM}$.
- The channel is forbidden at low temperature.
- The mass gap should be small.

► The WIMP neighborhood

Beyond self-annihilation:



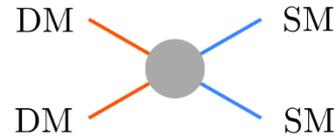
- Co-annihilation.
- Forbidden annihilation.
- Secluded annihilation.



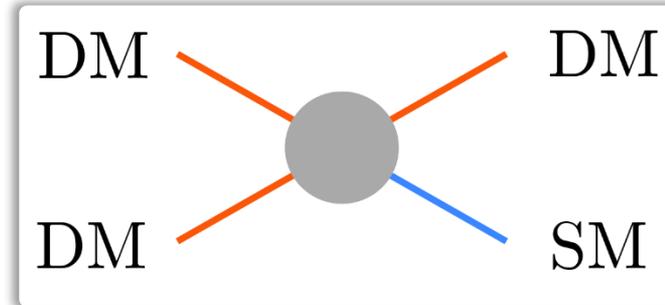
- DM annihilates to mediator particles instead of SM.
- Mediator particles decays to SM.
- Mediator particles is in equilibrium with SM.

► The WIMP neighborhood

Beyond self-annihilation:



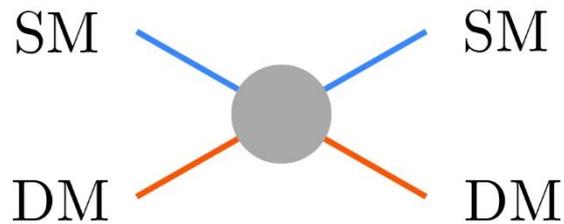
- Co-annihilation.
- Forbidden annihilation.
- Secluded annihilation.
- Semi-annihilation.
- ...



- Only one DM particle consumed.
- Z_3 -odd to ensure stability instead of $U(1)$ or Z_2 .

► Direct Detection

- Theoretically, great achievements in thermal freeze-out.
- Experimentally, direct detection (DD) experiments to search for DM.



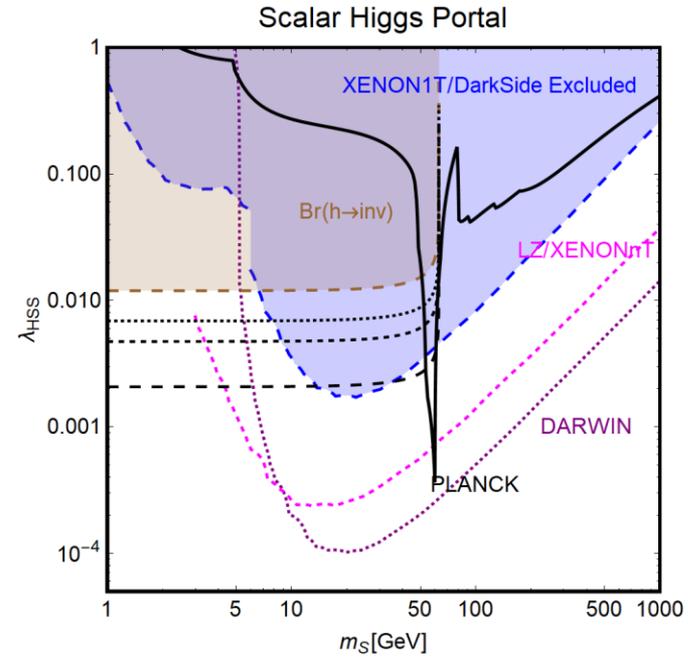
PandaX

- DM is still not found.
- Stringent constraints on WIMP models.

►► The WIMP Crisis

A simple Higgs portal model:

$$\Delta\mathcal{L} = -\frac{1}{4}\lambda H^\dagger H \chi^2$$

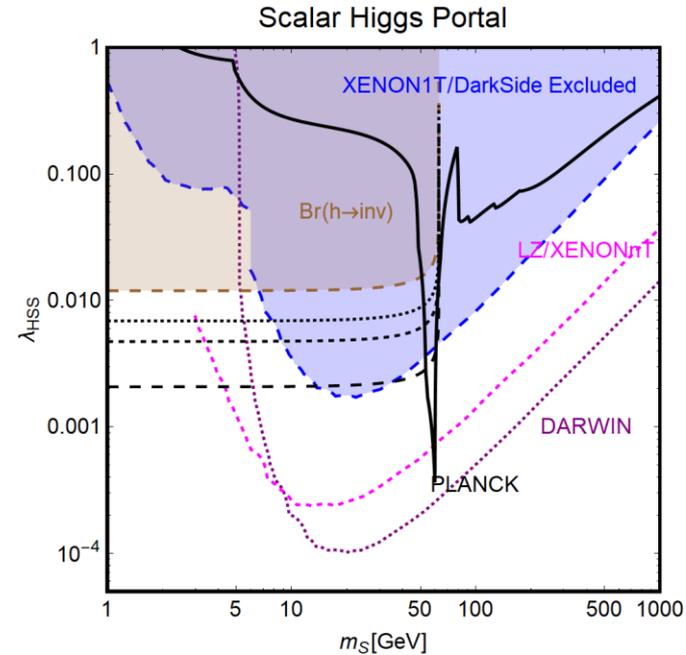


arXiv:1903.03616

► The WIMP Crisis

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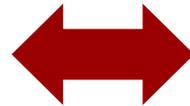
$$\Delta\mathcal{L} = -\frac{1}{4}\lambda H^\dagger H \chi^2$$



arXiv:1903.03616

Relic Abundance

Strongly coupled?



Direct Detection

Weakly coupled?

PART 03

Catalyzed Annihilation

►► DM in a Secluded Sector

Can we reproduce correct abundance in a weakly coupled sector?

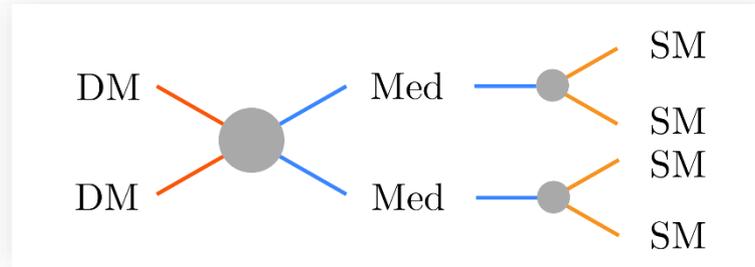


► DM in a Secluded Sector

Can we reproduce correct abundance in a weakly coupled sector?



1 / Secluded DM.



arXiv:0711.4866

- Direct detection bounds are invaded.
- Mediator is short-lived to stay in equilibrium.

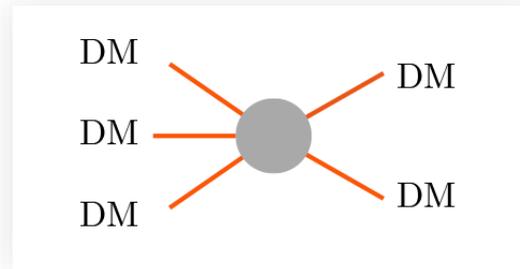
►► DM in a Secluded Sector

Can we reproduce correct abundance in a weakly coupled sector?



1/ Secluded DM.

2/ Strongly Interacting Massive Particles (SIMPs).

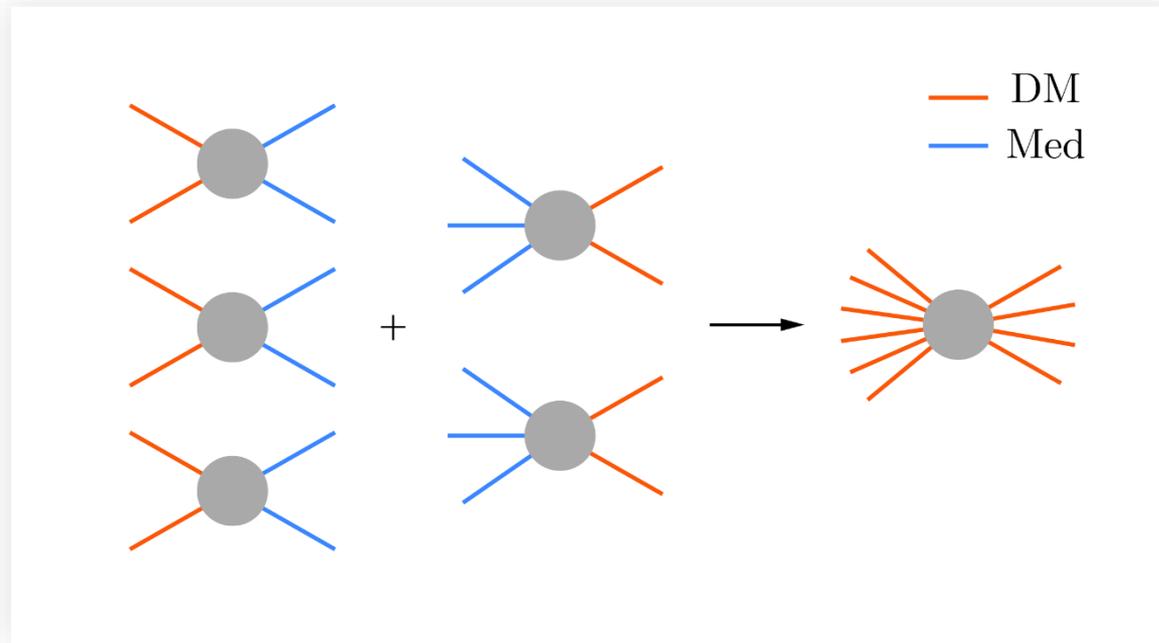


arXiv:1402.5143

- Number-changing annihilation dominated.
- DM-SM coupling is unrelated. Suppressed DD signals.
- Z_3 or Z_5 odd to ensure stability instead of $U(1)$ or Z_2 .
- MeV – GeV DM.

► Catalyzed Annihilation

The Catalyzed Annihilation



- Two processes included: $2\text{DM} \rightarrow 2\text{Med}$ & $3\text{Med} \rightarrow 2\text{DM}$.
- 2 DM particles consumed.
- Mediator is not consumed, like a catalyst.

► Boltzmann Equation

The coupled Boltzmann equations for DM (χ) and Med (A').

$$\begin{aligned}\dot{n}_\chi + 3Hn_\chi &= -\langle\sigma_2 v\rangle\left(n_\chi^2 - \bar{n}_\chi^2 \frac{n_{A'}^2}{\bar{n}_{A'}^2}\right) + \langle\sigma_3 v^2\rangle\left(n_{A'}^3 - \bar{n}_{A'}^3 \frac{n_\chi^2}{\bar{n}_\chi^2}\right), \\ \dot{n}_{A'} + 3Hn_{A'} &= +\langle\sigma_2 v\rangle\left(n_\chi^2 - \bar{n}_\chi^2 \frac{n_{A'}^2}{\bar{n}_{A'}^2}\right) - \frac{3}{2}\langle\sigma_3 v^2\rangle\left(n_{A'}^3 - \bar{n}_{A'}^3 \frac{n_\chi^2}{\bar{n}_\chi^2}\right) - \langle\Gamma_{A'}\rangle(n_{A'} - \bar{n}_{A'}).\end{aligned}$$

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Hubble
expansion



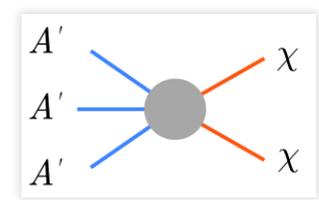
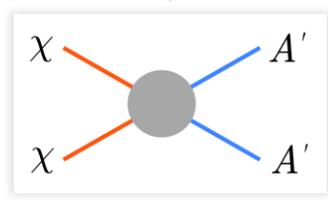
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Hubble expansion



Note: The coefficients and the signs are different!

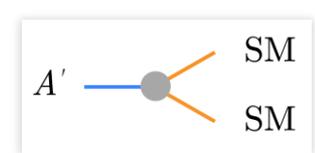
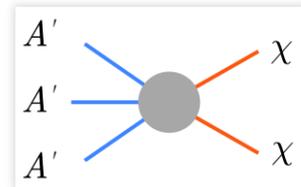
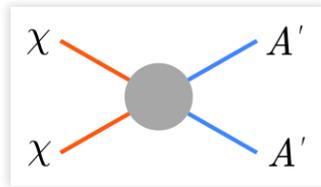
► Boltzmann Equation

The coupled Boltzmann equations for DM (χ) and Med (A').

$$\dot{n}_\chi + 3Hn_\chi = -\langle\sigma_2 v\rangle\left(n_\chi^2 - \bar{n}_\chi^2 \frac{n_{A'}^2}{\bar{n}_{A'}^2}\right) + \langle\sigma_3 v^2\rangle\left(n_{A'}^3 - \bar{n}_{A'}^3 \frac{n_\chi^2}{\bar{n}_\chi^2}\right),$$

$$\dot{n}_{A'} + 3Hn_{A'} = +\langle\sigma_2 v\rangle\left(n_\chi^2 - \bar{n}_\chi^2 \frac{n_{A'}^2}{\bar{n}_{A'}^2}\right) - \frac{3}{2}\langle\sigma_3 v^2\rangle\left(n_{A'}^3 - \bar{n}_{A'}^3 \frac{n_\chi^2}{\bar{n}_\chi^2}\right) - \langle\Gamma_{A'}\rangle(n_{A'} - \bar{n}_{A'}).$$

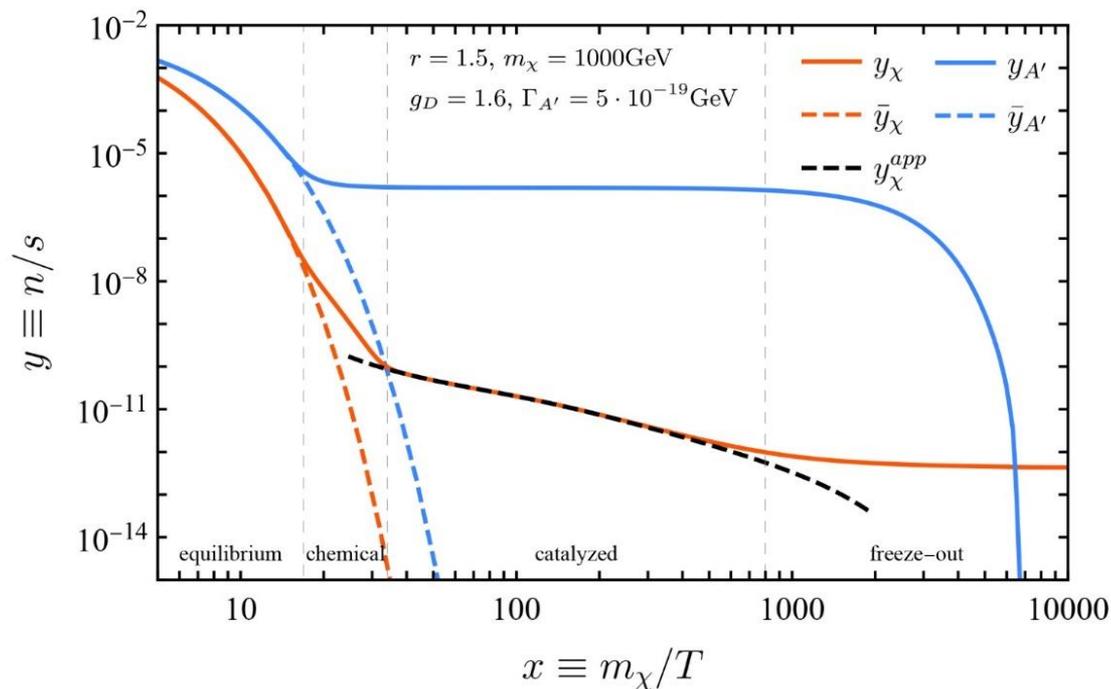
Hubble expansion



Note: The coefficients and the signs are different!

► Thermal Evolution

Thermal evolution of DM/Med



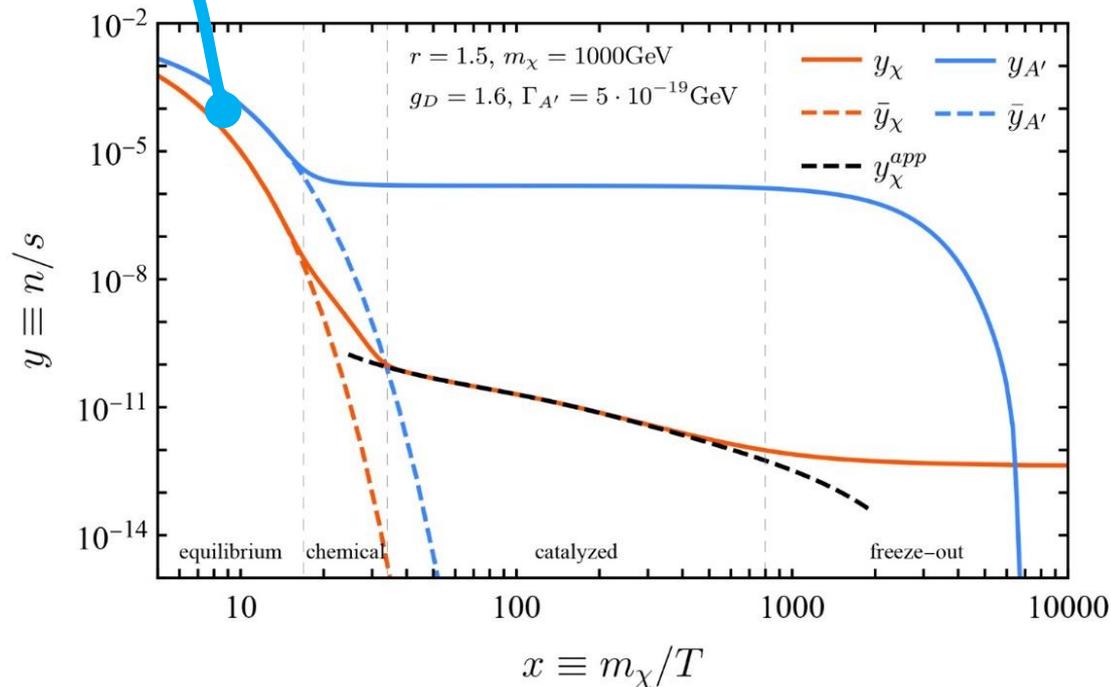
Blue Curve: Med

Red Curve: DM

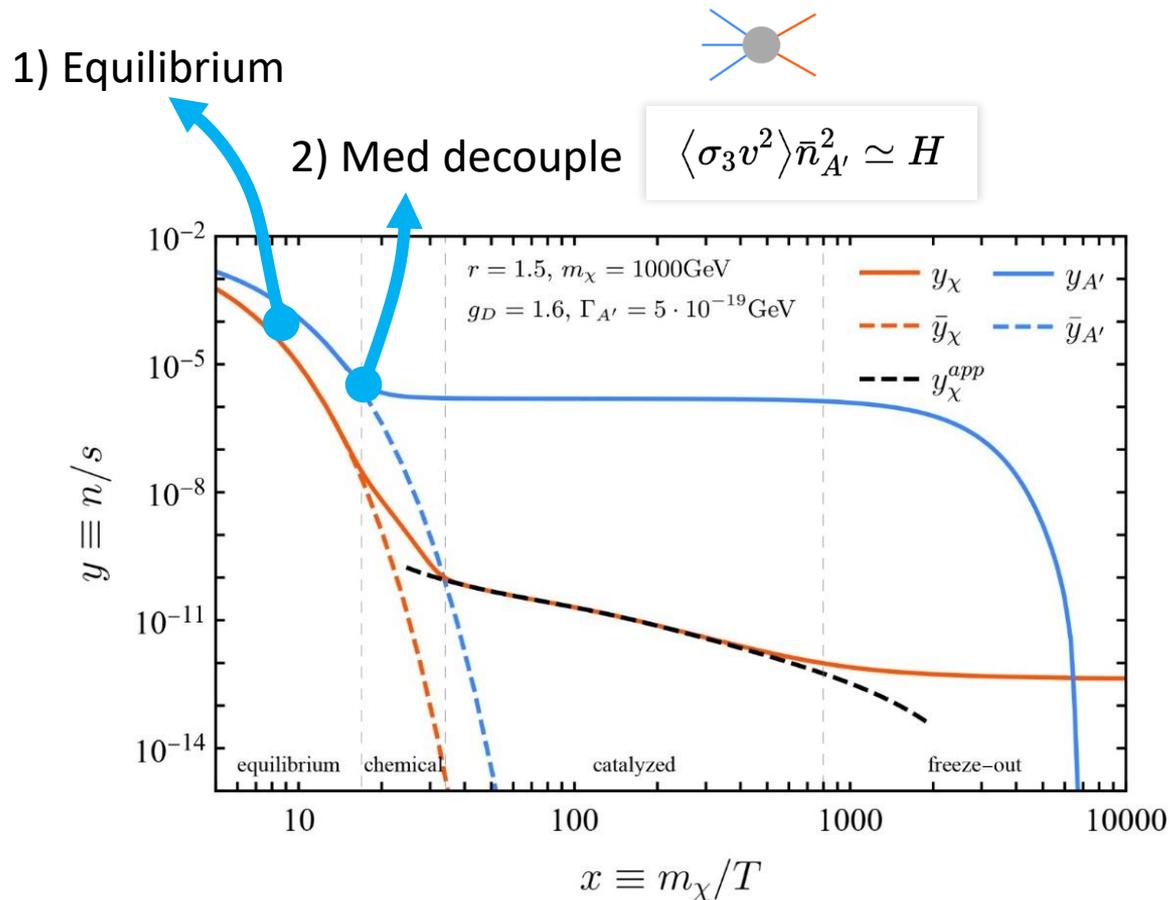
Thermal evolution of DM/Med

1) Equilibrium

$$n_\chi \simeq \bar{n}_\chi, n_{A'} \simeq \bar{n}_{A'}.$$



Thermal evolution of DM/Med



► Thermal Evolution

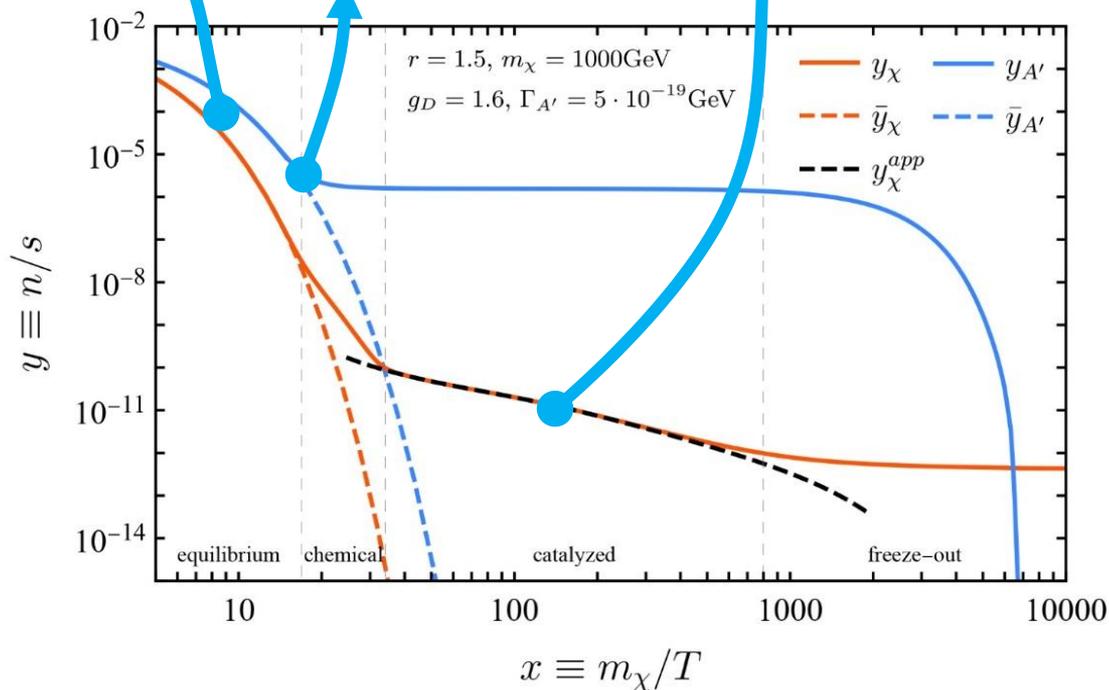
Thermal evolution of DM/Med

1) Equilibrium

2) Med decouple

3) Catalyzed annihilation

$$\langle \sigma_2 v \rangle n_\chi^2 \simeq \langle \sigma_3 v^2 \rangle n_{A'}^3$$



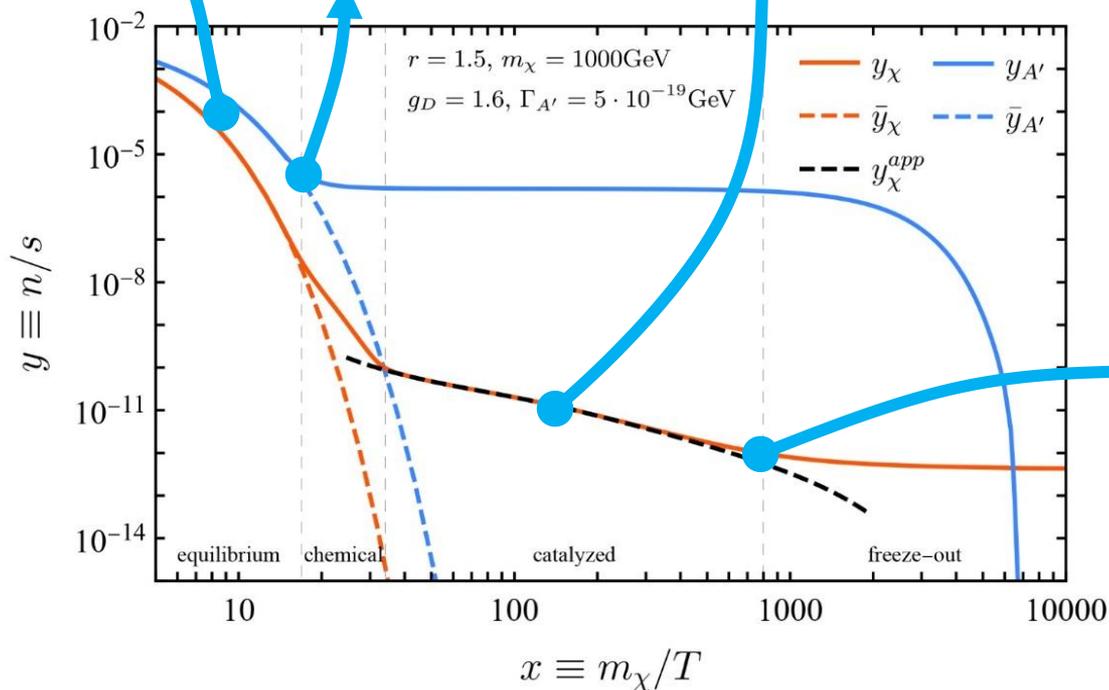
► Thermal Evolution

Thermal evolution of DM/Med

1) Equilibrium

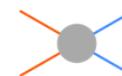
2) Med decouple

3) Catalyzed annihilation



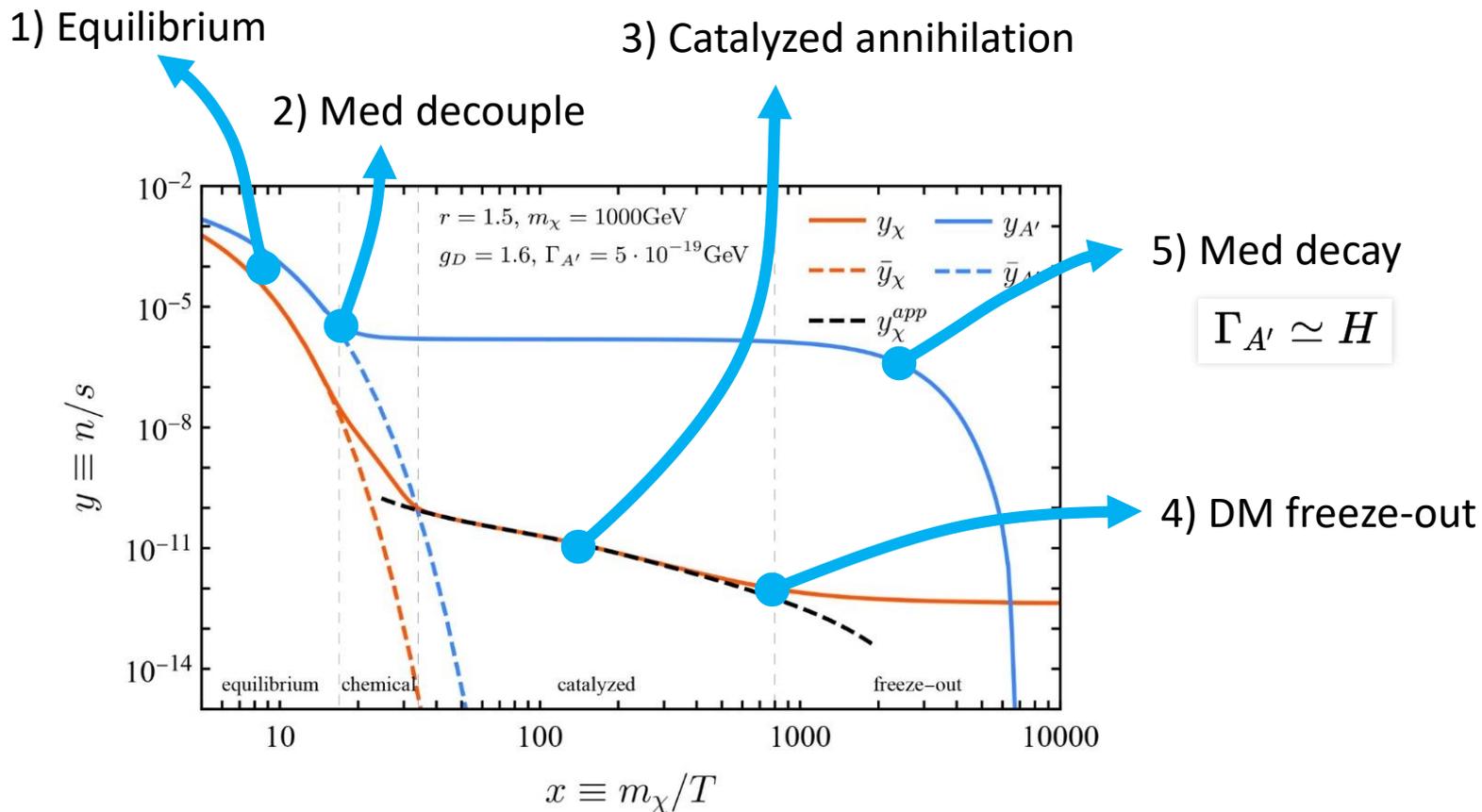
4) DM freeze-out

$$\langle \sigma_2 v \rangle n_\chi \simeq H$$



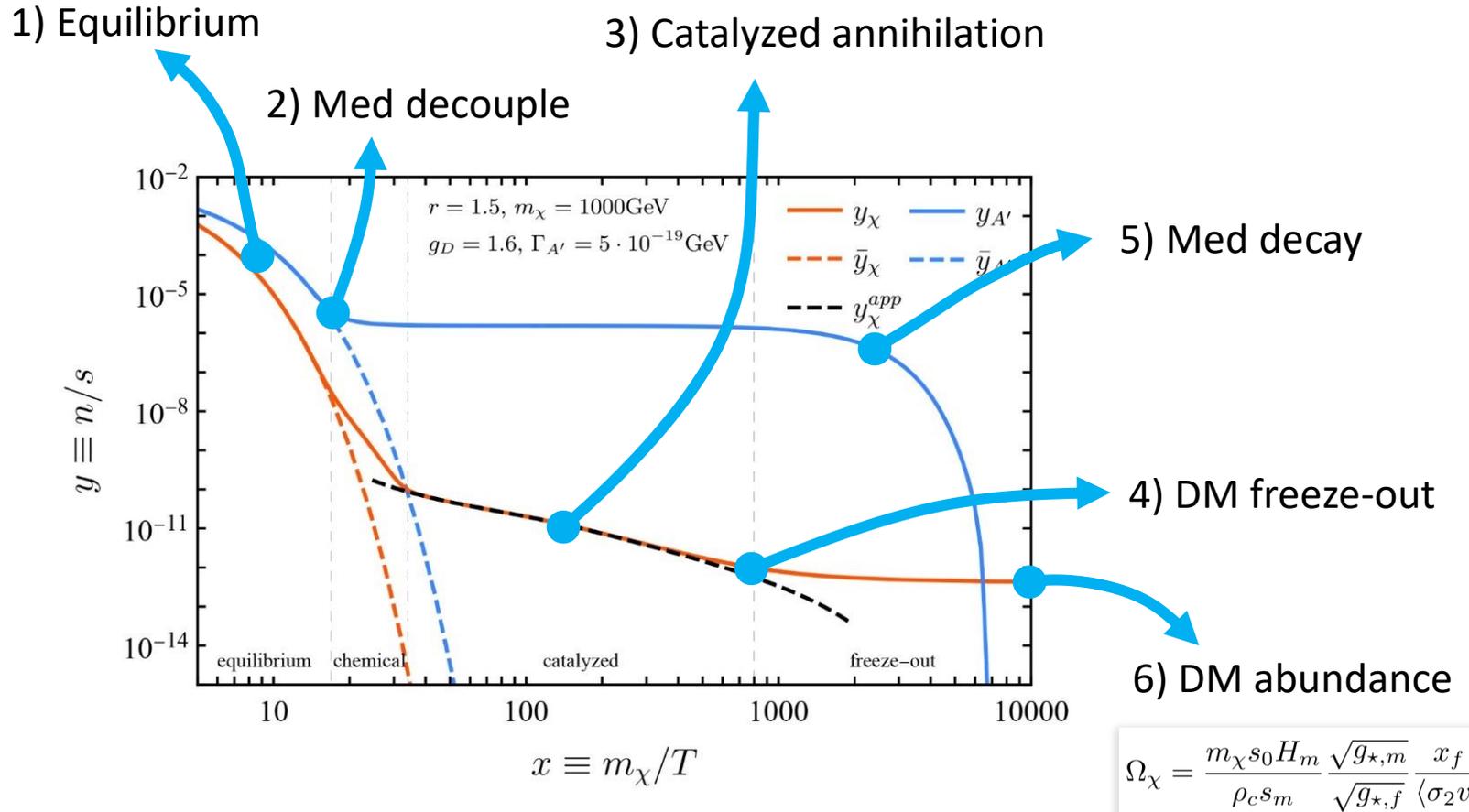
► Thermal Evolution

Thermal evolution of DM/Med



► Thermal Evolution

Thermal evolution of DM/Med



Requirements:

1/ Secluded sector.

- DM annihilates to SM is subdominant.

2/ Long-lived mediator.

- Mediator is out of equilibrium at early time.
- If mediator short-lived, back to the secluded DM.

3/ DM is slightly heavier than Med.

- Mediator is more abundant than DM.
- $3\text{Med} \rightarrow 2\text{DM}$ is not suppressed.

4/ Annihilation channels.

Features:

1/ Polynomially suppressed n_χ . $n_\chi \propto T^{9/2}$

- For WIMPs/SIMPs, it is exponentially suppressed.

2/ MeV – TeV DM mass.

3/ The freeze-out is late. $x_f \simeq 800$.

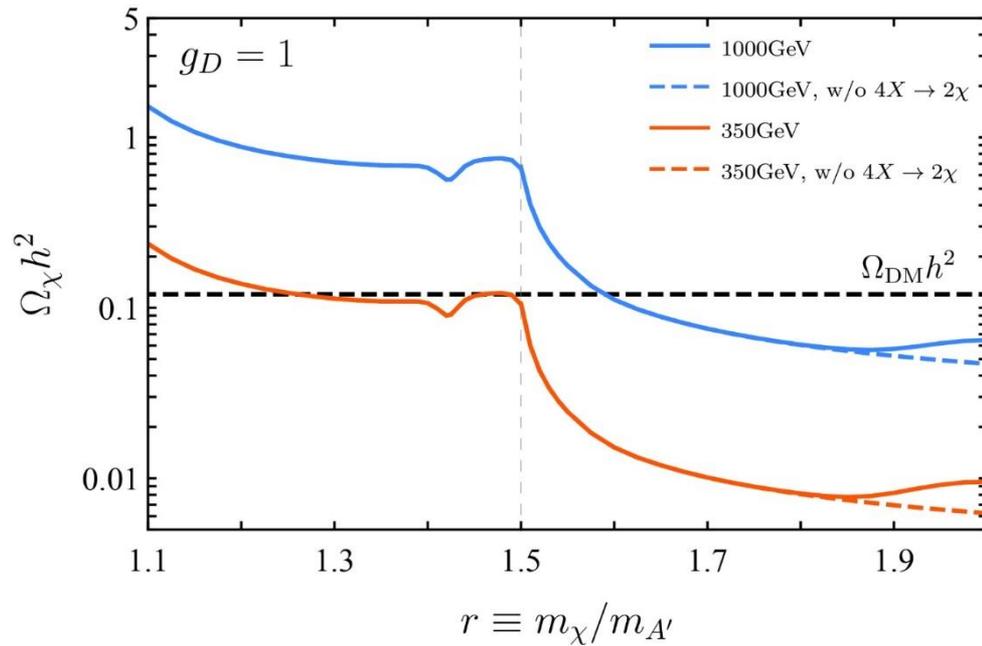
- Since the polynomially suppression, DM are consumed slowly.
- The catalyzed annihilation lasts long.

4/ Enhanced indirect detection signals.

- Since $\Omega_\chi \propto \frac{x_f}{\langle \sigma_2 v \rangle}$, late freeze-out means large annihilation.

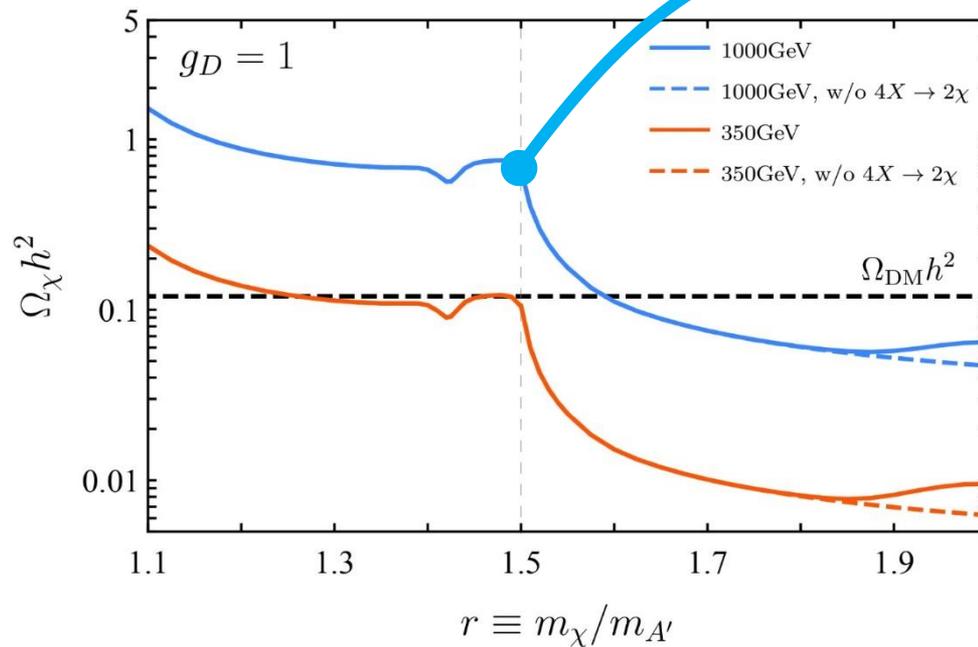
► Catalyzed Freeze-out

Varying Mass Ratio $r \equiv m_\chi/m_{A'}$



► Catalyzed Freeze-out

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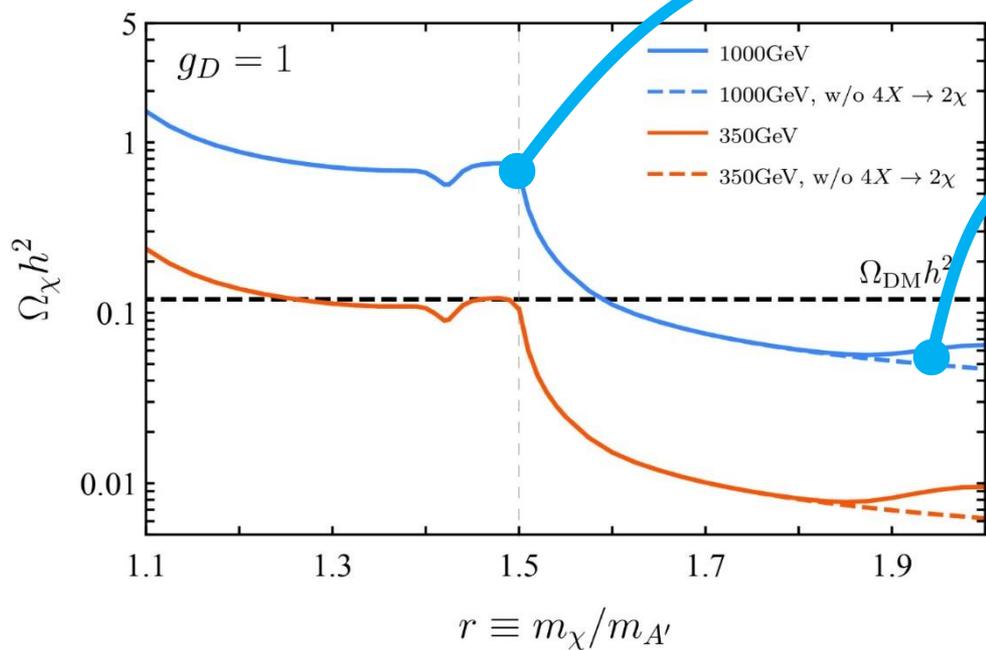
$r = 1.5$ threshold

When $3m_{A'} < 2m_\chi$,  is exponentially suppressed at low temperature.

$$\langle \sigma_3 v^2 \rangle \propto e^{-(2r-3)x/r}$$

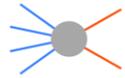
► Catalyzed Freeze-out

Varying Mass Ratio $r \equiv m_\chi/m_{A'}$

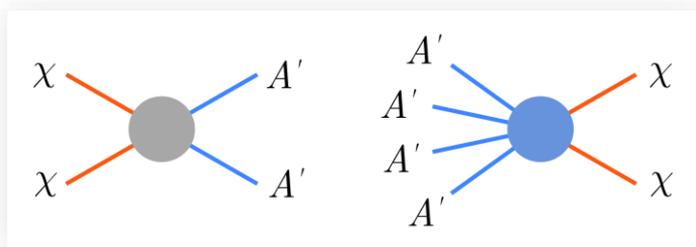


$r = 1.5$ threshold

$r \approx 2$ threshold

When $4m_{A'} \approx 2m_\chi$,  turn dominant, since it is not exponentially suppressed.

The catalyzed annihilation here:



► Model & Phenomenology

Dark Photon Model:

$$\mathcal{L}_{\text{DS}} = -\frac{1}{4}F'_{\mu\nu}F'^{\mu\nu} + \frac{1}{2}m_{A'}^2 A'_\mu A'^\mu + \bar{\chi}(i\not{D} - m_\chi)\chi,$$

$$\mathcal{L}_{\text{mix}} = -\frac{\epsilon}{2\cos\theta_W}F'_{\mu\nu}B^{\mu\nu}.$$

χ : DM
 A' : Mediator

► Model & Phenomenology

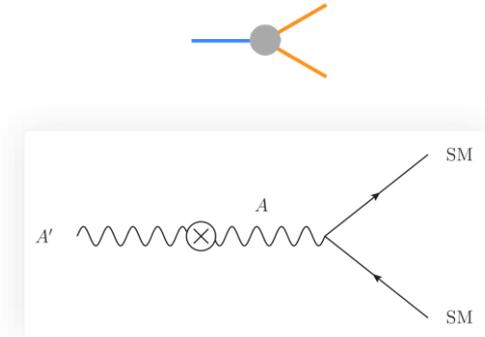
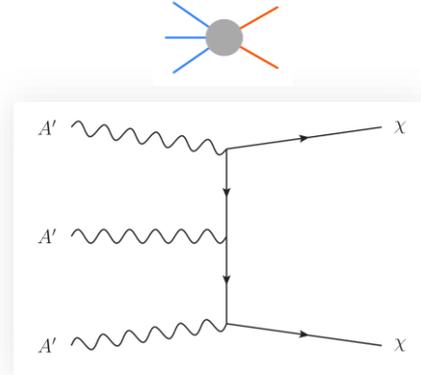
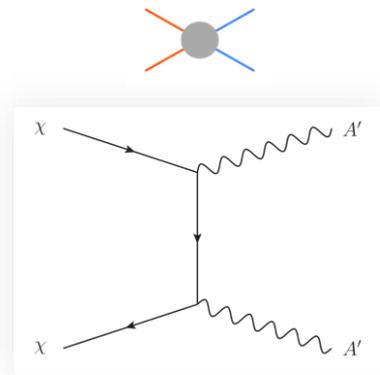
Dark Photon Model:

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$$\mathcal{L}_{\text{mix}} = -\frac{\epsilon}{2\cos\theta_W}F'_{\mu\nu}B^{\mu\nu}.$$

χ : DM
 A' : Mediator

Feynman diagrams:



► Model & Phenomenology

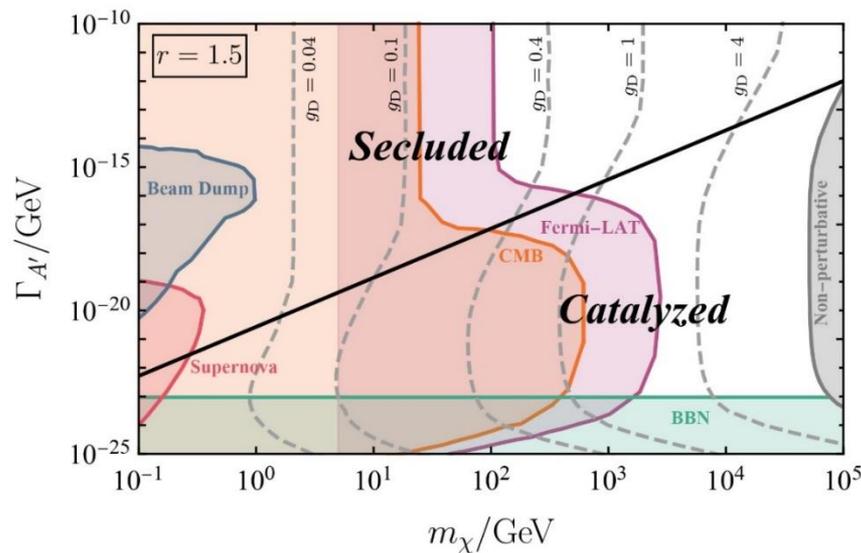
Dark Photon Model:

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$$\mathcal{L}_{\text{mix}} = -\frac{\epsilon}{2\cos\theta_W}F'_{\mu\nu}B^{\mu\nu}.$$

χ : DM
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Phase diagram and bounds:



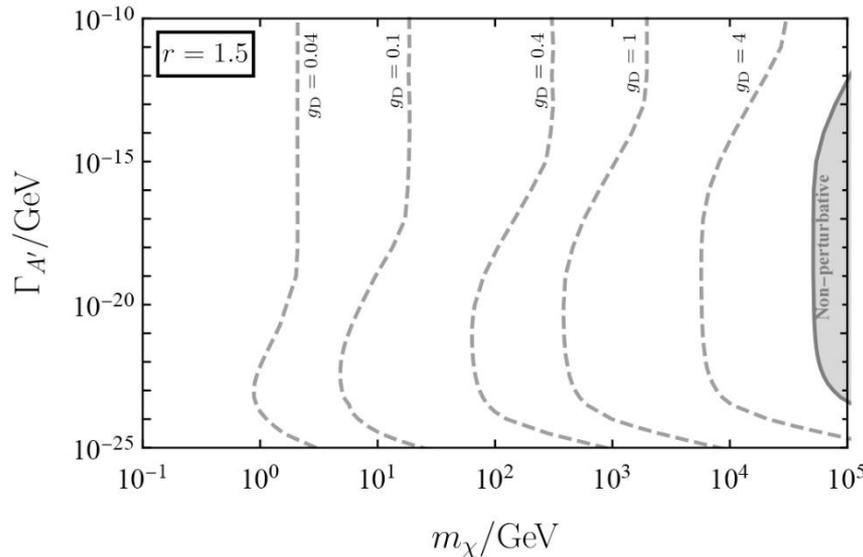
► Model & Phenomenology

Dark Photon Model:

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$$\mathcal{L}_{\text{mix}} = -\frac{\epsilon}{2\cos\theta_W}F'_{\mu\nu}B^{\mu\nu}.$$

χ : DM
 A' : Mediator



- Only four parameters.
- Mass ratio: $r = 1.5$.
- Every point gives correct abundance with different coupling g_D .
- Five curves with constant g_D shown.
- Heavy DM require strong coupling.
- Non-perturbative: $g_D < 4\pi$.

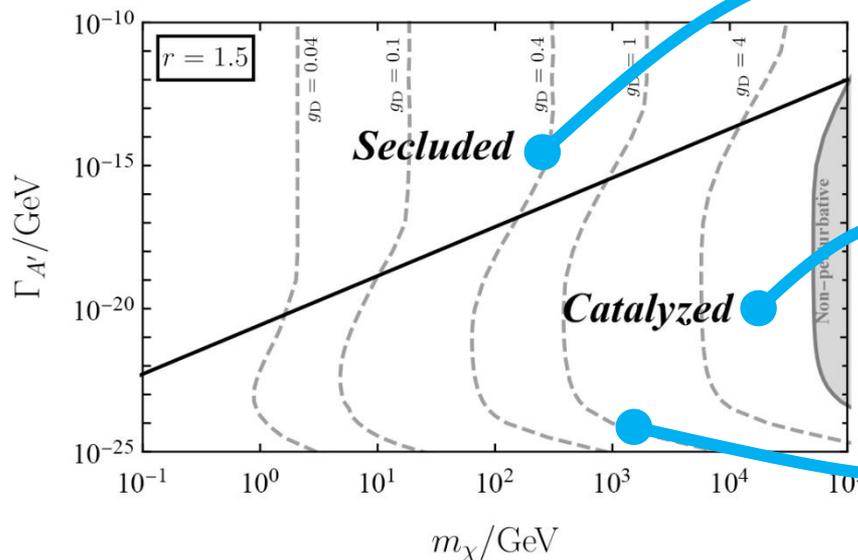
► Model & Phenomenology

Dark Photon Model:

$$\mathcal{L}_{\text{DS}} = -\frac{1}{4}F'_{\mu\nu}F'^{\mu\nu} + \frac{1}{2}m_{A'}^2 A'_\mu A'^\mu + \bar{\chi}(i\not{D} - m_\chi)\chi,$$

$$\mathcal{L}_{\text{mix}} = -\frac{\epsilon}{2\cos\theta_W}F'_{\mu\nu}B^{\mu\nu}.$$

χ : DM
 A' : Mediator



Secluded Phase

- Short-lived mediator, secluded DM.
- Mediator stays in equilibrium.

Catalyzed Phase

- Long-lived mediator, catalyzed annihilation.
- Mediator is out-of-equilibrium before freeze-out.

Long-lived mediator decay injects entropy and dilute DM abundance.

► Model & Phenomenology

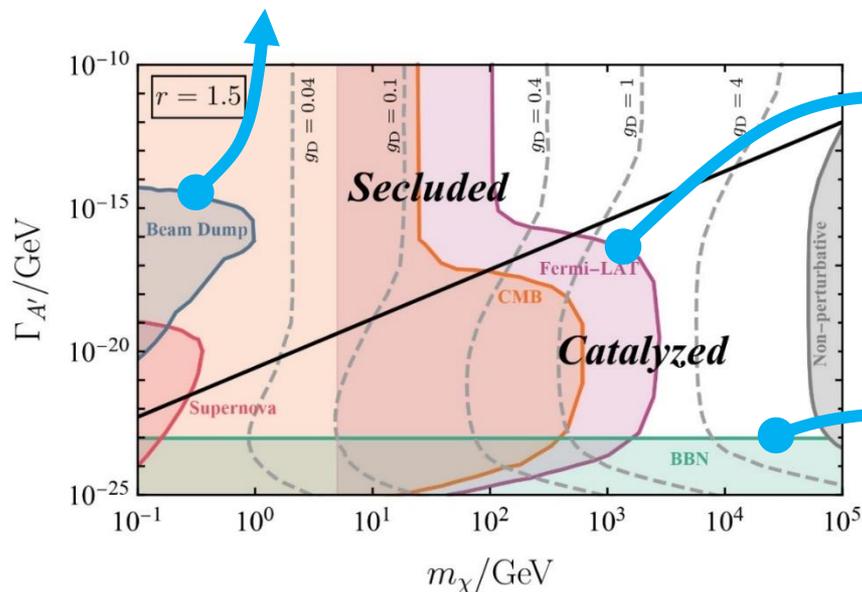
Dark Photon Model:

$$\mathcal{L}_{\text{DS}} = -\frac{1}{4}F'_{\mu\nu}F'^{\mu\nu} + \frac{1}{2}m_{A'}^2 A'_\mu A'^\mu + \bar{\chi}(i\not{D} - m_\chi)\chi,$$

$$\mathcal{L}_{\text{mix}} = -\frac{\epsilon}{2\cos\theta_W}F'_{\mu\nu}B^{\mu\nu}.$$

χ : DM
 A' : Mediator

1) Beam dump & supernova bounds on dark photon lifetime.



2) CMB & indirect detection bounds on DM annihilation.

- more stringent for catalyzed phase.
- DM below 3TeV is not favored.

3) BBN limit on dark photon lifetime.

- Late decay of A' will fail BBN.

Thermal decoupling vs. Chemical decoupling

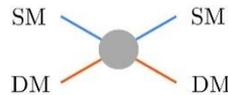
1/
WIMPs:

chemical decoupling:



$$\langle \sigma_{2v} \rangle n_{\text{DM}} \simeq H$$

thermal decoupling:



$$\langle \sigma_{\text{el}v} \rangle n_{\text{SM}} \simeq H$$

- Since $n_{\text{SM}} \gg n_{\text{DM}}$, thermal decoupling happens later.
- $T_{\text{DM}} = T_{\text{SM}}$ before freeze-out.

Thermal decoupling vs. Chemical decoupling

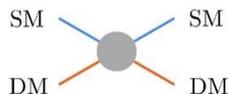
1/ WIMPs:

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$$\langle \sigma_2 v \rangle n_{\text{DM}} \simeq H$$

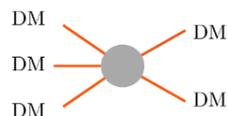
thermal decoupling:



$$\langle \sigma_{\text{el}} v \rangle n_{\text{SM}} \simeq H$$

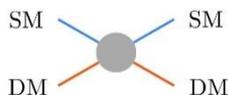
2/ SIMPs:

chemical decoupling:



$$\langle \sigma_3 v \rangle n_{\text{DM}}^2 \simeq H$$

thermal decoupling:



$$\langle \sigma_{\text{el}} v \rangle n_{\text{SM}} \simeq H$$

- Thermal decoupling can happen before chemical decoupling.
- $T_{\text{DM}} \neq T_{\text{SM}}$ at freeze-out.
- DM abundance determined by thermal decoupling. [arXiv:1512.04545](https://arxiv.org/abs/1512.04545)

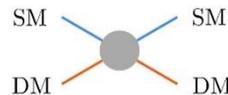
Thermal decoupling vs. Chemical decoupling

Catalyzed annihilation:

chemical decoupling:



thermal decoupling:



- The work is based on the assumption: $T_{\text{DM}} = T_{\text{SM}}$.
- Thermal decoupling can happen before freeze-out.
- DM abundance is modified with thermal decoupling considered.
- Further works are required!

Summary:

- 1/ WIMP is stringently constrained by direct detections (**the WIMP crisis**).
- 2/ We proposed novel **catalyzed freeze-out** paradigm.
- 3/ The paradigm is realized in the **dark photon model**.
- 4/ The **thermal decoupling** of the paradigm should be discussed.

Thanks.

Chuan-Yang Xing

